

UNIVERSITÀ POLITECNICA DELLE MARCHE Repository ISTITUZIONALE

Flow instability of an axial flow pump-as-turbine using relative streamline coordinates

This is the peer reviewd version of the followng article:

Original

Flow instability of an axial flow pump-as-turbine using relative streamline coordinates / Kan, Kan; Zhang, Qingying; Feng, Jiangang; Zheng, Yuan; Xu, Hui; Rossi, Mose; Li, Haoyu. - In: PHYSICS OF FLUIDS. - ISSN 1070-6631. - 36:3(2024). [10.1063/5.0192004]

Availability:

This version is available at: 11566/328296 since: 2024-03-29T10:25:38Z

Publisher:

Published DOI:10.1063/5.0192004

Terms of use:

The terms and conditions for the reuse of this version of the manuscript are specified in the publishing policy. The use of copyrighted works requires the consent of the rights' holder (author or publisher). Works made available under a Creative Commons license or a Publisher's custom-made license can be used according to the terms and conditions contained therein. See editor's website for further information and terms and conditions. This item was downloaded from IRIS Università Politecnica delle Marche (https://iris.univpm.it). When citing, please refer to the published version.

Flow instability of an axial flow pump-as-turbine using relative

streamline coordinates

Kan Kan (阚阚),^{1,2,a)} Qingying Zhang (张清滢),¹ Jiangang Feng (冯建刚),³ Yuan Zheng (郑源),^{1,2} Hui Xu (徐辉), ³ Mosè Rossi, ⁴ and Haoyu Li (李昊宇) 1 **AFFILIATIONS**

¹ College of Energy and Electrical Engineering, Hohai University, Nanjing 211100, PR China

² College of Water Conservancy and Hydropower Engineering, Hohai University, Nanjing 210098, PR China

³ College of Agricultural Science and Engineering, Hohai University, Nanjing 210098, PR China

 Department of Industrial Engineering and Mathematical Sciences (DIISM), Marche Polytechnic

University, Ancona 60131, Italy

a)Author to whom correspondence should be addressed: kankan@hhu.edu.cn

 ABSTRACT: When axial flow pumps-as-turbines (PATs) operate under off-design conditions, unstable and unsteady flow structures appear in the internal flow field, resulting in suboptimal functioning. These operating conditions not only decrease the efficiency of the hydraulic machines but also affect their mechanical reliability. This study establishes relative streamline coordinates, based on the blade's mean camber line, to investigate flow instabilities in axial flow PATs from a new perspective. Numerical simulations on an axial flow PAT were performed and validated using experimental data. The results show that flow separation is more likely to occur due to the more curved profile at the blade's suction surface, leading to considerable fluctuations in velocity along the flow direction and enstrophy amplitude near both the hub and impeller shroud. Moreover, the poor matching of the relative inflow angle of the impeller with the blade inlet angle leads to impingement losses near their leading edge, generating unstable flows and significant pressure pulsations, which induces hydraulic instability within the impeller. In addition to rotor-stator interference effects, the curvature of the blade suction surface profile and the bend structure of inlet conduit are significant factors that influence the pressure pulsation distribution of the PAT. An analysis of the enstrophy transport equation indicates that the relative vortex generation and the Reynolds stress dissipation terms play a key role in both vortex generation and dissipation, whereas the viscous term has a lower influence. These findings can serve as a reference for the optimization and efficient design of axial flow PATs.

I. INTRODUCTION

 Reducing carbon emissions and increasing the proportion of renewable energy sources have 36 become issues of global importance.¹ With the increasing demand for renewable energy, there has been 37 considerable investment in small-scale hydropower power generation worldwide.^{2,3} However, in remote and underdeveloped areas, the operating and installation costs of conventional hydraulic turbines still pose a major challenge. Considering the availability and cost advantages of commercial hydraulic pumps, the pump-as-turbine (PAT) technology has been gaining interest as an economic alternative to conventional small-size hydraulic turbines in such areas. As a result, it has become a

Physics of Fluids

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

crucial research topic in the small-scale hydropower sector worldwide. ⁴ 42 In PATs, pumps essentially 43 behave as hydraulic turbines, offering advantages such as low investment costs, simple design, and easy maintenance.^{5,6} The prototype impeller of a PAT has been designed based on the pump theory, 45 resulting in a blade inlet angle that does not match with the original flow passage components when the 46 pump operates in the turbine mode.⁷ This often leads to a lower efficiency in reverse mode operation 47 compared to the direct one. In addition, the absence of flow regulation components, such as movable 48 guide vanes, limits the range of high-efficiency operation.⁸ When operating under off-design conditions, 49 the internal flow field within the PAT exhibits flow separation, wakes, secondary flows, and other 50 unstable flow phenomena that affect its operation stability.^{9,10} In particular, the hydraulic instability 51 leads to severe mechanical vibrations that are amplified when the PAT deviates from the design 52 conditions. Therefore, studying flow instability problems of the PAT is crucial to addressing this issue 53 as it helps prevent failures and ensures the secure and stable operation of hydraulic machines.

 In previous studies on PAT technology, researchers primarily focused on predicting the performance of PATs. Several performance prediction models have been developed through theoretical 56 derivation, experimental verification^{9,11} and artificial neural network.^{12,13} However, the general application of PAT performance conversion theory in these studies was poor, and there was a large 58 difference between the prediction and experimental results, while a few studies¹¹⁻¹³ could accurately predict PAT performance. With the development of computational fluid dynamics (CFD), numerical 60 simulations have become essential for studying the hydraulic characteristics of PATs. Nasir et al.¹⁴ performed numerical simulations on a centrifugal PAT. The numerical results were validated using 62 experimental data, indicating good agreement (with error percentages lower than 3%). Yang et al.¹⁵ numerically simulated a large vaned-voluted centrifugal pump to evaluate its performance in the pump and turbine modes. The results showed that the best efficiency point (BEP) of this centrifugal PAT presented a higher flow-rate and head compared to the direct mode. Lin et al.¹⁶ presented a theoretical method to predict the optimum efficiency point of PATs within a specific speed range, using the impeller-volute matching principle. As a result, the proposed method could forecast the BEP with an error of less than 5%.

69 Many scholars have conducted various studies on the internal flow field of PATs, investigating the 70 influence of geometric parameters on hydraulic performance and optimizing certain parameters to 71 enhance efficiency. Yang et al.¹⁷ discussed the influence of blade thickness on the efficiency and 72 hydraulic loss of a PAT and found out that an increase in blade thickness leads to a decrease in 73 efficiency and an increase in energy losses within the impeller. Xu et al.¹⁸ optimized the geometric 74 design parameters of impeller blades to effectively improve the efficiency of a PAT by reducing 75 pressure pulsations and expand the operating range of the PAT. Binama et al.¹⁹ numerically analyzed 76 the influence of the blade TE position on the pressure field of a centrifugal PAT and found that 77 adjusting the TE position reduced the pulsation phenomenon of the PAT. Wang et al.²⁰ found out that forward-curved blades could significantly enhance the performance of a PAT. Xiang et al.²¹ designed a 79 forward-curved impeller of the PAT and found that the forward-curved blade can also significantly 80 reduce pressure pulsation. Adu et al.²² numerically investigated the transient characteristics of a 81 centrifugal PAT operating at different rotational speeds, revealing that the turbulent kinetic energy and 82 vortices of the PAT increased with increasing rotational speed. Xin et al.²³ investigated the distribution 83 of hydraulic losses in a centrifugal PAT by entropy production theory and found that impingement, 84 backflow, and vortices were the main hydraulic factors responsible for the irreversible hydraulic losses 85 of the PAT. Si et al.²⁴ focused on an ultra-low specific speed centrifugal PAT and studied the energy

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004** conversion ability of the impeller, conducting an in-depth analysis of the unstable flow structures 87 within the impeller and the reasons for their generation. In addition, Hu et al.²⁵ examined the performance variations and internal flows of a centrifugal PAT at variable rotational speeds. Their results indicated that rotational speed had a significant effect on the hydraulic performance and 90 operational stability of the PAT. Yin et al.²⁶ presented a numerical method capable of efficiently simulating the unsteady flow field during the runaway process of a prototype PAT. Their results showed that the instability of the turbine's S zone was caused by vortices in the inlet section of the runner, leading to severe periodic blockage of the flow in the runner channel.

 Thus far, existing research on PATs has primarily focused on the effect of impeller geometric parameters, hydraulic performance, and energy losses. To the best of the authors' knowledge, there have been few in-depth analyses of the complex flow developing inside hydraulic machines. Therefore, this study aims to establish an ideal streamline coordinate system based on the blade's mean camber line, which can reflect the hydraulic performance of the impeller within an axial flow PAT from the flow, radial, and circumferential directions. In particular, flow instability problems of the axial flow PAT are investigated to provide valuable insights for ensuring its secure and stable operation.

 The rest of this paper is organized as follows. The geometric model and numerical methods are introduced in Section II. The results of this study are presented in Section III, including a discussion on the hydraulic performance of the axial flow PAT and an analysis of flow instability in the internal flow field based on the relative streamline coordinate system. Finally, conclusions are presented in Section 105 IV.

106 **II. NUMERICAL MODEL AND METHOD**

107 **A. Governing equations**

108 Considering the incompressible flow in this paper, the continuity and momentum equations²⁷ are 109 presented in Eqs. (1) and (2) as follows

110

111

$$
\frac{\partial \overline{u_i}}{\partial x_i} = 0,\tag{1}
$$

$$
\frac{\partial \overline{u}_i}{\partial t} + \overline{u}_j \frac{\partial \overline{u}_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial \overline{p}}{\partial x_i} + \frac{1}{\rho} \frac{\partial}{\partial x_j} \left(\mu \frac{\partial \overline{u}_i}{\partial x_j} - \rho \overline{u'_i u'_j} \right) + \overline{f}_i,
$$
\n(2)

112 where ρ is the density; t is the physical time; x_i and x_j denote the Cartesian coordinate components in 113 *i* and *j* directions, respectively; \overline{u}_i and \overline{u}_j denote the corresponding components of the Reynolds-averaged velocity; \bar{p} is the Reynolds-averaged pressure; μ is the dynamic viscosity; $\rho u_i u_j$ ' 114 115 is the Reynolds stress and \overline{f}_i is the Reynolds-averaged body force.

116 **B. Turbulence model**

117 The *k* and *ω* equations are written as

118
$$
\frac{\partial(\rho k)}{\partial t} + \frac{\partial}{\partial x_j}(\rho \overline{u}_j k) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_i}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + P_k - \beta^* \rho k \omega
$$
 (3)

119
$$
\frac{\partial(\rho\omega)}{\partial t} + \frac{\partial}{\partial x_j}(\rho\overline{u}_j\omega) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_\omega} \right) \frac{\partial \omega}{\partial x_j} \right] + \alpha \frac{\omega}{k} P_k - \beta \rho \omega^2 + 2\rho (1 - F_1) \frac{\sigma_{\omega 2}}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j} \tag{4}
$$

120 The turbulent viscosity μ_t is expressed as

$$
\mu_i = \frac{a_i k \rho}{\max(a_i \omega, SF_2)}\tag{5}
$$

122 F_1 and F_2 is calculated as

121

123
$$
F_1 = \tanh\left\{ \left\{ \min\left[\max\left(\frac{\sqrt{k}}{\beta^* \omega y}, \frac{500\mu}{\rho y^2 \omega} \right), \frac{4\rho \sigma_{\omega z} k}{CD_{k\omega} y^2} \right] \right\}^4 \right\}
$$
(6)

124
$$
CD_{k\omega} = \max \left(2\rho \frac{\sigma_{\omega 2}}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j}, 10^{10} \right)
$$
 (7)

125
$$
F_2 = \tanh\left\{ \left[\max \left(\frac{2\sqrt{k}}{\beta^* \omega y}, \frac{500\mu}{\rho y^2 \omega} \right) \right]^2 \right\}
$$
 (8)

126 where *k* is the turbulent kinetic energy, ω is the turbulent frequency, P_k is the production of turbulence 127 kinetic energy, *S* denotes the mean rate of the strain tensor, and *y* is the distance from the wall. The 128 constants are as follows: $a_1 = 0.31$, $β^* = 0.09$, $β = 0.075$, $σ_k = 1.176$, $σ_\omega = 2$, and $σ_{\omega 2} = 0.856$.^{28,29}

129 **C. Geometric model**

130 The subject of this study is an axial flow PAT model, the drawing of which is shown in Fig. 1.

131 The geometric model is composed of four parts, namely the inlet conduit, guide vane, impeller, and

132 outlet conduit. The basic parameters of the PAT are presented in Table I.

4

136 **D. Mesh generation**

ACCEPTED MANUSCRIPT

Physics of Fluids

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

 The ICEM software is used to create a hexahedral structured grid for the entire computational domain. To achieve an accurate resolution of the grid distribution in the boundary layer around the blades, an O-type topology is adopted surrounding the blades. Grids near the walls are also refined to capture small-scale flow structures in these areas. The grid independence is verified using the 141 Richardson extrapolation method.³⁰⁻³² Three sets of grids are designed, ranging from coarse to fine, with grid numbers of 4.1 million, 9.1 million, and 19.9 million, respectively. For these three sets of grids, the optimum operating condition of the PAT is simulated, and torque and efficiency are selected as evaluation parameters for the grid independence study. The grid convergence index (GCI) results are listed in Table II. Taking both torque and efficiency into consideration, as mentioned earlier, the GCI values are found to be 0.11% and 0.38%, respectively. Both these values are lower than 1%, thus, 147 meeting the grid convergence standard.³³ The number of grids is eventually determined as 9.1 million. Fig. 2 shows the mesh of the pump section and local refinement of the impeller blade.

153 **F. Numerical settings**

In this study, the SST k-ω turbulence model was chosen to better account for turbulent effects.^{34,35} 155 The finite volume method was used for spatial discretization, and the SIMPLEC algorithm was applied 156 to achieve a coupled pressure-velocity solution. The pressure inlet was adopted as the inlet boundary

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004** condition, while the outlet boundary condition was set to the pressure outlet. The impeller was set in a 158 rotating reference frame, whereas the remaining domains were set to be stationary.³⁶ For the interface between the impeller and stationary components, the frozen rotor approach was employed in the steady-state simulations, while the transient rotor-stator approach was used in the transient simulations. The steady-state simulations were used as initial data for the transient simulations, and the time step 162 was set to 1.15 × 10⁻⁴ s, corresponding to 1/360 of the impeller rotation period. All wall surfaces were set as no-slip walls. Numerical simulations were considered to have converged when the residual was below 10^{-5} .

III. RESULTS AND ANALYSIS

A. CFD validation

 Fig. 3 presents a comparison of the macroscopic performance of the axial flow PAT obtained numerically and experimentally. It is evident that the simulation results agree with the experimental 169 data, with a maximum relative difference of less than 3% , particularly near the Q_{BEP} (indicated by the blue circle in Fig. 3). This demonstrates the credibility of the chosen mesh arrangement and numerical method, ensuring the precision of the numerical simulations. The operating conditions deviate further from the optimum condition, the decrease in efficiency becomes more pronounced. It is important to note the inefficiency of the PAT under off-design operating conditions.

FIG. 3. Comparison between the experimental and simulation results.

B. Relative streamline coordinate system based on mean camber line of blade

 The ideal impeller is assumed to be composed of an infinite number of extremely thin blades, which allows for the consideration that the water flow in the impeller is uniform and axisymmetric, and its relative motion track coincides with the blade's mean camber line. To reflect the flow characteristics along the ideal streamline direction, this study establishes a relative streamline coordinate system based on the blade's mean camber line for the impeller. This system includes three directions: the flow direction *λ*, the circumferential direction *c*, and the radial direction *r*. Fig. 4(a) defines the length coefficient *λ* of the blade's mean camber line, and the flow direction is from the LE to the TE of the 184 blades. A value of $\lambda = 0$ corresponds to the LE of the blades and a value of $\lambda = 1$ corresponds to the TE of the blades. Fig. 4(b) shows the monitoring point scheme on the blade's mean camber line for the impeller. Eleven locations are selected along the ideal flow direction, marked from 0 to 1 from the blade inlet to the outlet. Three locations are selected in the circumferential direction from the suction surface (SS) to the pressure surface (PS), marked as S, M, and P. The span indicates the location of the circumferential unfolding surface in the impeller region, span=0 for the circumferential unfolding

 surface at the hub, and span=1 for the circumferential unfolding surface at the shroud. In the radial direction, three spans are selected from the impeller hub to the shroud, marked as span 0.1, span 0.5, and span 0.9. Fig. 5 shows these monitoring points in the relative streamline coordinate system.

C. Analysis of the velocity based on the streamline coordinate system

193
194

 The distribution of relative velocity along the flow direction is shown in Fig. 5. According to the 199 velocity triangle, at $0.8Q_{\text{BEP}}$, the impeller inflow strikes the suction surface when it enters the LE of the blade due to the low axial velocity. In contrast, at 1.2 *Q*BEP the impeller inflow strikes the pressure 201 surface when it enters the LE of the blade, resulting in an impact loss. Moreover, at $0.8Q_{\rm{BEP}}$, the relative velocity decreases near the LE of the blade on both the suction and pressure surfaces. Under the optimum condition, the relative velocity near the LE of the blade gradually increases along the flow direction, indicating that the relative inflow angle is in good agreement with the blade inlet angle. At Q_{BEP} , it is evident that the relative velocity drops sharply at $\lambda = 0.3$. Under all operating conditions, the relative velocity near the suction surface decreases in the TE region, demonstrating that water flow in this region is obstructed. The relative velocity near the pressure surface and the middle position of the flow channel tends to increase along the flow direction, which is more consistent with the theoretical situation compared to that the near suction surface.

213 FIG. 5. Distribution of the relative velocity on an ideal streamline: (a) $0.8Q_{\text{BEP}}$; (b) Q_{BEP} ; (c) $1.2Q_{\text{BEP}}$ In axial flow machinery, it is common to assume cylindrical layer independence, and the velocity 215 in the radial direction (V_r) is zero. Consequently, the radial velocity component can be considered as an indicator when investigating the flow instability of the PAT. Fig. 6 depicts the distribution of the radial component along the flow direction under different operating conditions. Notably, the radial velocity

Physics of Fluids

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

AIP
E Publishing

D. Enstrophy analysis based on the streamline coordinate system

 Under off-design working conditions, the water flow hits the blade inlet edge and forms vortices 228 that constitute an unstable flow. To accurately quantify the vortex evolution process, this study uses 229 enstrophy to measure vortex intensity. Enstrophy is defined as the scalar $ω^2/2$, where $ω$ denotes the 230 vorticity.³⁷

231 Fig. 7 illustrates the distribution of enstrophy $\omega^2/2$ along the blade's mean camber line for the impeller under different operating conditions. According to the figure, the enstrophy has a larger value near the suction surface, indicating that an unstable flow is more likely to occur near the suction 234 surface. At 0.8 Q_{BEP} and Q_{BEP}, the maximum enstrophy in the flow direction is concentrated at the TE of the blades. Under optimum condition, the maximum value of the enstrophy is most significant near the hub and decreases gradually along the radial direction from the impeller hub to the shroud. The greater curvature of the suction surface profiles leads to stronger vortices in the TE region of the blade. 238 At 1.2 QBEP, the maximum enstrophy in the flow direction is observed at $\lambda = 0.3$ near the impeller shroud. Fig. 8 illustrates the radial enstrophy distribution along the blade's mean camber line for the impeller under different operating conditions. The trend and distribution of enstrophy and radial enstrophy in the flow direction are generally consistent. As the flow rate increases, the percentage of radial enstrophy in total enstrophy gradually decreases.

ACCEPTED MANUSCRIPT

Physics of Fluids

AIP
E Publishing

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

249 **E. Frequency domain analysis of the pressure pulsation**

 Unstable flow structures in a flow field causes pressure pulsations. To investigate the flow characteristics within the flow field of the PAT, this study uses the fast Fourier transform (FFT) method to analyze the frequency domain characteristics of the pressure values at the monitoring points on the blade mean camber line of the impeller. *Fⁿ* represents the rotation frequency of the impeller. The horizontal coordinate in Fig. 9 scales the frequency dimensionless and represents the integral multiple of the impeller rotation frequency. The vertical coordinate represents the pressure coefficient, which is defined as

$$
C_p = \frac{(P_i - P_{\text{ave}})}{0.5 \rho u_{\text{tip}}^2}
$$
 (9)

258 where P_i is the transient pressure, P_{ave} is the average pressure over a time period, and u_{tip} represents the 259 circumferential velocity of the impeller blade tip.³⁸ The obtained frequency domain results of pressure 260 pulsation are presented in Fig. 9. The static and dynamic interfaces of CFX calculations are designed 261 according to the transient rotor-stator approach, so the monitoring points follow the overall movement 262 of the impeller, and the guide vanes rotate relative to the monitoring points. Thus, a large amplitude of 263 C_p can be observed at the guide vane passing frequency of $6f_n$. This demonstrates that the rotor-stator 264 interference between the guide vane and the impeller is a significant cause of pressure pulsations in the 265 internal flow field. Additionally, due to curved inlet conduit in this model, there are also large *Cp* 266 amplitudes at 1*fⁿ* and its multiples, specifically at 2*fn*, 3*fn*, and 4*fn*. Fig. 10 shows the distribution of the 267 main frequency amplitude of pressure pulsation along the flow direction. In a single-impeller channel, 268 the pressure pulsation in the middle of the flow channel is the smallest and the dominant frequency 269 amplitude of pressure pulsation is more evenly distributed in the flow direction. At 0.8 QBEP, pressure 270 pulsation near the pressure surface is more intense, especially at the LE of the blade. In contrast, at 271 $1.2Q_{\text{BEP}}$, the pressure pulsation amplitude near the suction surface is more intense, and the maximum 272 amplitude of pressure pulsation along the flow direction is at $\lambda = 0.3$. Compared to other conditions, the 273 optimum condition exhibits a better inflow condition and lower pressure pulsation, and the largest

257

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

 FIG. 10. Pressure fluctuation amplitude of the dominant frequency: (a) 0.8 *Q*BEP; (b) *Q*BEP; (c) 1.2 *Q*BEP . Fig. 11 shows the distribution of the pressure coefficient under different operating conditions. At 286 0.8 Q_{BEP}, the impeller inlet flow impinges on the suction surface at the blade inlet edge of the blade, resulting in a local high-pressure region near the blade's LE. At 1.2 *Q*BEP, the impeller inlet flow at the blade inlet edge impacts the pressure surface of the blade, leading to impact loss, which hinders smooth water flow. Under the optimum operating conditions, the relative inflow angle of the blade inlet matches the blade inlet angle. Thus, the pressure distribution at the LE of the pressure and suction surfaces is relatively uniform, and the impeller inflow impingement loss is minimized. At low flow rates and under optimum conditions, localized low pressure exists near the blade's TE of the suction surface, where flow separation occurs in the TE region, thus generating a vortex flow.

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

298 **F. Frequency domain analysis of Reynolds-averaged enstrophy transport equation**

 To further analyze the unstable flow structures, the generation and development of vortices are studied using the enstrophy transport equation. Many previous studies employed transport equations derived from direct numerical simulations and did not consider the effect of the Reynolds stress, which renders them inapplicable to the analysis conducted under the Reynolds-averaged Navier-Stokes (RANS) method. In this study, the Reynolds-averaged enstrophy transport equation is derived on the 304 basis of RANS equations. Eq. (2) can be written as follows³⁴

305
$$
\frac{\partial \overline{u}_i}{\partial t} + \overline{u}_j \frac{\partial \overline{u}_i}{\partial x_j} = \frac{1}{\rho} \frac{\partial}{\partial x_j} \left(-\delta_{ij} \overline{p} + 2\mu \overline{S}_{ij} - \rho \overline{u'_i u'_j} \right) + \overline{f}_i
$$
(10)

306 $\rho u_i u_j$ can be expressed as '

294

$$
-\rho \overline{u'_i u'_j} = 2\mu_i \overline{S}_{ij} - \frac{2}{3} \delta_{ij} \rho k \tag{11}
$$

308 where \bar{S}_{ij} is the mean strain tensor, and δ_{ij} is Kronecker delta.³⁹ By substituting the Reynolds stress 309 formula into the RANS equation, Eq. (10) can be written in the vector form as

310
$$
\frac{\partial \overline{u}}{\partial t} + (\overline{u} \cdot \nabla) \overline{u} = -\frac{1}{\rho} \nabla \overline{p} + \nu \nabla^2 \overline{u} + \nu_t \nabla^2 \overline{u} - \frac{2}{3} \nabla k + \overline{f}
$$
 (12)

311 where \bar{u} is the Reynolds-averaged velocity vector, v is the kinematic viscosity, v_t is the eddy

312 viscosity, ∇ is the Hamiltonian operator, $\vec{f} = -2(\vec{c} \times \vec{u})$, and \vec{c} is the Reynolds-averaged angular 313 velocity. According to the vector equation,

314
$$
\nabla \left(\frac{\overline{\boldsymbol{u}}^2}{2} \right) = (\overline{\boldsymbol{u}} \cdot \nabla) \overline{\boldsymbol{u}} + \overline{\boldsymbol{u}} \times (\nabla \times \overline{\boldsymbol{u}})
$$
(13)

315 Eq. (12) can be then rewritten as:

316
$$
\frac{\partial \overline{u}}{\partial t} + \nabla \left(\frac{\overline{u}^2}{2} \right) - \overline{u} \times \overline{\omega} = -\frac{1}{\rho} \nabla \overline{p} + \nu \nabla^2 \overline{u} + \nu_t \nabla^2 \overline{u} - \frac{2}{3} \nabla k - 2(c \times \overline{u})
$$
(14)

317 Taking the curl of Eq. (14), the following is obtained:

318
$$
\frac{\partial \overline{\omega}}{\partial t} - (\overline{\omega} \cdot \nabla) \overline{\mathbf{u}} + (\overline{\mathbf{u}} \cdot \nabla) \overline{\omega} = \frac{\nabla \overline{p} \times \nabla \rho}{\rho^2} + \nu \nabla^2 \overline{\omega} + \nu_t \nabla^2 \overline{\omega} - \frac{2}{3} \nabla \times (\nabla k) - 2 \nabla \times (\mathbf{c} \times \overline{\mathbf{u}}) \tag{15}
$$

319 where $\bar{\omega}$ is the Reynolds-averaged vorticity. The Reynolds-averaged enstrophy transport equation 320 can be obtained by taking the dot product between Eq. (15) and the Reynolds-averaged vorticity. The 321 enstrophy transport equation is written as

$$
\frac{\partial(\overline{\omega}_{i}\overline{\omega}_{i}/2)}{\partial t} = \overline{\omega}_{i}\overline{S}_{ij}\overline{\omega}_{j} - \overline{u}_{j}\frac{\partial(\overline{\omega}_{i}\overline{\omega}_{i}/2)}{\partial x_{j}} + \frac{1}{\rho^{2}}\varepsilon_{ijk}\overline{\omega}_{i}\frac{\partial\rho}{\partial x_{j}}\frac{\partial\rho}{\partial x_{k}} + \frac{\partial^{2}\overline{\omega}_{i}}{\partial x_{j}\partial x_{j}}\overline{\omega}_{i} + \nu\frac{\partial^{2}\overline{\omega}_{i}}{\partial x_{j}\partial x_{j}}\overline{\omega}_{i} - \frac{2}{3}\varepsilon_{ijk}\frac{\partial^{2}k}{\partial x_{i}\partial x_{j}}\overline{\omega}_{k} - 2\left(\frac{\partial\left(c_{i}\overline{u}_{j}\right)}{\partial x_{j}}\overline{\omega}_{i} - \frac{\partial\left(c_{i}\overline{u}_{j}\right)}{\partial x_{i}}\overline{\omega}_{i}\right)^{(16)}
$$

323
$$
G_{\omega} = \overline{\omega}_i \overline{S}_{ij} \overline{\omega}_j - \overline{u}_j \frac{\partial (\overline{\omega}_i \overline{\omega}_i/2)}{\partial x_j}
$$
(17)

324
$$
B_{\omega} = \frac{1}{\rho^2} \varepsilon_{ijk} \overline{\omega}_i \frac{\partial \rho}{\partial x_j} \frac{\partial p}{\partial x_k}
$$
 (18)

$$
V_{\omega} = V \frac{\partial^2 \overline{\omega}_i}{\partial x_j \partial x_j} \overline{\omega}_i
$$
 (19)

326
$$
R_{\omega} = V_t \frac{\partial^2 \overline{\omega}_i}{\partial x_j \partial x_j} \overline{\omega}_i - \frac{2}{3} \varepsilon_{ijk} \frac{\partial^2 k}{\partial x_i \partial x_j} \overline{\omega}_k
$$
(20)

327
$$
C_{\omega} = -2 \left(\frac{\partial (c_i \overline{u}_j)}{\partial x_j} \overline{\omega}_j - \frac{\partial (c_i \overline{u}_j)}{\partial x_i} \overline{\omega}_j \right)
$$
(21)

328 where $\overline{\omega}_i$ is the average vorticity, ε_{ijk} is the permutation symbol, and c_i is the angular velocity. G_{ω} is a 329 relative vortex generation term, which accounts for the stretching and bending of vorticity owing to the 330 velocity gradient. B_{ω} is a baroclinic torque term that represents the vorticity change caused by the 331 non-parallel pressure gradient and the density gradient. Due to the incompressibility of the fluid, this 332 term is ignored in this study. V_ω is the viscous term that represents the vorticity change due to the 333 viscous effect of the fluid, R_{ω} is the Reynolds stress dissipation term, and C_{ω} is the Coriolis force term 334 that is associated with the rotational motion of the impeller. $40,41$

335 The frequency domain characteristics of each item at the monitoring points on the blade's mean 336 camber line for the impeller are analyzed using the FFT. Fig. 12 displays the frequency domain

ACCEPTED MANUSCRIPT

Physics of Fluids

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

 characteristics of the enstrophy transport equation at 0.8 *Q*BEP. As shown in the figure, the relative vortex generation term and the Reynolds stress dissipation term play a significant part in the vortex 339 generation and dissipation processes, and the viscous term has the least influence. At 0.8 $Q_{\rm BEP}$, the 340 relative vortex generation term G_{ω} , the Reynolds stress dissipation term R_{ω} , and the Coriolis force term *C^ω* exhibit the most intense pulsation on the pressure surface near the impeller shroud where the largest 342 pulsation amplitude is distributed near the LE of the blade and extends to $\lambda = 0.6$. However, the viscous term *V^ω* exhibits the most intense pulsation amplitude on the suction surface. Near the suction surface, the maximum value of the pulsation amplitude is located at the TE of the blade, while at the middle of the flow channel and near the pressure surface, this maximum value is located at the LE of the blade. This indicates that, close to the impeller hub, unstable flow structures near the pressure surface are mainly affected by impeller inflow impingement. In contrast, the occurrence of flow separation in the TE region near the suction surface and the resulting generation of vortex flow is the main cause of unstable flow near the suction surface.

358 FIG. 12. Pulsation frequency domain of the transport equation of enstrophy at $0.8Q_{\text{BEP}}$: (a) G_{ω} ; (b) R_{ω} ; (c) *Cω*; (d) *V^ω* .

 Fig. 13 shows the distribution of the components of the enstrophy transport equation at $0.8Q_{\text{BEP}}$. Near the suction surface, the region with large values of the enstrophy transport equation is concentrated in the TE of the blade. Meanwhile, the region near the impeller hub is considerably affected by the wake of the guide vanes, leading to a high enstrophy region near the blade inlet that subsequently develops downstream. Near the impeller shroud, the high enstrophy region is generated

366
367

 Fig. 14 displays the frequency domain characteristics of the enstrophy transport equation under optimum operating conditions. It is evident that the pulsation amplitudes of the enstrophy transport equation close to the suction surface are the most significant, and the region with the maximum pulsation amplitudes is concentrated at the TE of the blade. Meanwhile, the pulsation amplitudes of the enstrophy transport equation gradually decrease along the radial direction from the impeller hub to the shroud. As the suction surface profile becomes more curved closer to the hub, it results in a stronger swirling flow. In the middle of the flow channel and close to the pressure surface, the region with the largest pulsation amplitude is located at the blade inlet edge, and the amplitude gradually decreases along the flow direction.

ACCEPTED MANUSCRIPT

Physics of Fluids

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

AIP
E Publishing

 Fig. 15 shows the distribution of the enstrophy transport equation under optimum operating conditions. Near the suction surface, the region with the large enstrophy amplitudes is mainly distributed at the TE of the blade. Near the impeller hub, enstrophy is considerably affected by the wake of the guide vanes, with a high enstrophy area forming near the blade inlet, which then develops downstream of the wake.

FIG. 15. Distribution on blade-to-blade surfaces at *Q*BEP .

394 The frequency domain diagram of the enstrophy transport equation at $1.2Q_{\text{BEP}}$ is shown in Fig. 16. Notably, the pulsation amplitudes of the enstrophy transport equation near the suction surface are the most significant, especially near the impeller shroud. At Span 0.5 and Span 0.9, the region where the 397 pulsation is most intense is located at $\lambda = 0.3$. Near the hub, the pulsation amplitude is more evenly distributed along the flow direction. Compared to the suction surface, the pulsation amplitudes of the enstrophy transport equation in the middle of the flow channel and near the pressure surface are almost

ACCEPTED MANUSCRIPT

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset

Physics of Fluids

AIP
E Publishing

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

 $\frac{401}{402}$

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

409 FIG. 16. Pulsation frequency domain of the transport equation of enstrophy at $1.2Q_{\text{BEP}}$: (a) G_{ω} ; (b) R_{ω} ; (c) *Cω*; (d) *V^ω* .

411 Fig. 17 shows the distribution of the enstrophy transport equation at 1.2 Q_{BEP} . The relative vortex generation term and the Reynolds stress dissipation term are the main factors affecting vortex generation and dissipation. Meanwhile, near the impeller hub, which is more impacted by the wake of the guide vanes, the region with high values of enstrophy is formed near the blade inlet, which then develops downstream the wake to the neighboring blades. Near the impeller shroud, this high-enstrophy region is generated near the suction surface and develops along the flow direction.

IV. CONCLUSIONS

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

 rate conditions close to the BEP. The flow instability of the PAT was investigated based on the relative streamline coordinate system. The following conclusions were drawn from the simulation results:

 (1) Under off-design conditions, the mismatch between the relative inflow angle of the impeller and the blade inlet angle leads to impingement losses that generate an unstable flow near the LE of the blade. At low flow rate conditions, the impeller inflow impinges on the blade suction surface upon entering the LE of the blade. At high flow rate conditions, the impeller inflow impinges on the blade pressure surface, hindering smooth water flow into the impeller and causing a decrease in the relative velocity near the LE of the blade.

 (2) The greater curvature of the suction surface profile leads to flow separation and vortex formation in the TE regions of the blade. Near the hub, the blade profile is more curved, and the maximum enstrophy in the flow direction is concentrated at the TE of the suction surface under all operating conditions. Under the optimum conditions, the maximum enstrophy at different span surfaces is focused on the TE of the suction surface, gradually decreasing along the radial direction from the impeller hub to the shroud. At low flow rate conditions, the maximum enstrophy is close to the pressure surface, while at high flow rate conditions, it is located near the suction surface.

 (3) The unstable flow is generated near the LE of the blade under off-design conditions, resulting in significant pressure pulsations. Moreover, the unstable flow at the suction surface leads to larger amplitude pressure pulsations near the suction surface. In addition to the rotor-stator interference effects, the curvature of the blade suction surface profile and the bend structure of the inlet conduit are important factors affecting the distribution of pressure pulsations in the PAT.

 (4) The relative vortex generation term and the Reynolds stress dissipation term play a significant role in both vortex generation and dissipation, while the viscous term has a lower effect. Regions with high amplitudes of the enstrophy transport equation are mainly distributed at the TE of the blade. In addition, in the impeller shroud, a region with large enstrophy amplitudes is generated close to the pressure surface at low flow rate conditions, while at high flow rate conditions, a large enstrophy amplitude region exists near the suction surface and develops downstream along the flow direction.

ACKNOWLEDGMENTS

 This work was supported by the National Natural Science Foundation of China (52379086, 52009033), the Jiangsu Innovation Support Programme for International Science and Technology Cooperation (BZ2023047), the Postdoctoral Research Foundation of China (2022T150185; 2022M711021), and the Project on Excellent Post-graduate Dissertation of Hohai University (422003478).

AUTHOR DECLARATIONS

- **Conflict of Interest**
- The authors have no conflicts to disclose.

Author Contributions

Kan Kan: Conceptualization (lead); Formal analysis (equal); Funding acquisition (lead); Methodology

(supporting); Resources (lead); Supervision (supporting); Writing - original draft (equal); Writing -

review & editing (supporting). **Qingying Zhang:** Data curation (equal); Investigation (equal);

Validation (lead); Writing - original draft (equal). **Jiangang Feng:** Methodology (equal); Resources

(equal); Supervision (equal); Writing - review & editing (supporting). **Yuan Zheng:** Resources

AIP
E Publishing

AIP
E Publishing

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004** (supporting); Supervision (equal); Visualization (equal); Writing - review & editing (equal). **Hui Xu:** Resources (supporting); Supervision (equal); Visualization (equal); Writing - review & editing (equal).

Mosè Rossi: Supervision (supporting); Visualization (equal); Writing - review & editing (equal).

 Haoyu Li: Data curation (equal); Formal analysis (equal); Methodology (supporting); Software (equal).

DATA AVAILABILITY

 The data that support the findings of this study are available from the corresponding author upon reasonable request.

REFERENCES

 ¹G. A. M. Castorino, L. Manservigi, S. Barbarelli, E. Losi, and M. Venturini, "Development and validation of a comprehensive methodology for predicting pat performance curves," Energy 274, 127366 (2023).

 M. Stefanizzi, T. Capurso, G. Balacco, M. Binetti, S. M. Camporeale, and M. Torresi, "Selection, control and techno-economic feasibility of pumps as turbines in water distribution networks," Renewable Energy 162, 1292-1306 (2020).

 M. H. S. Haghighi, S. M. Mirghavami, M. M. Ghorani, A. Riasi, and S. F. Chini, "A numerical study on the performance of a superhydrophobic coated very low head (VLH) axial hydraulic turbine using entropy generation method," Renewable Energy 147, 409-422 (2020).

⁴ F. A. Plua, F. J. Sánchez-Romero, V. Hidalgo, P. A. López-Jiménez, and M. Pérez-Sánchez, "Variable speed control in PATs: theoretical, experimental and numerical modelling," Water 15(10), 1928 (2023).

 ⁵M. Tahani, A. Kandi, M. Moghimi, and S. D. Houreh, "Rotational speed variation assessment of centrifugal pump-as-turbine as an energy utilization device under water distribution network condition," Energy 213, 118502 (2020).

 K. Kan, Q. Zhang, Z. Xu, Y. Zheng, Q. Gao, and L. Shen, "energy loss mechanism due to tip leakage flow of axial flow pump as turbine under various operating conditions," Energy 255, 124532 (2022).

 H. Yu, T. Wang, Y. Dong, Q. Gou, L. Lei, and Y. Liu, "Numerical investigation of splitter blades on the performance of a forward-curved impeller used in a pump as turbine," Ocean Engineering 281, 114721 (2023).

 X. Li, T. Ouyang, Y. Lin, and Z. Zhu, " Interstage difference and deterministic decomposition of internal unsteady flow in a five-stage centrifugal pump as turbine," Physics of Fluids 35(4), 045136 (2023).

 Y. Zhang, W. Jiang, S. Qi, L. Xu, Y. Wang, and D. Chen, "Clocking effect on the internal flow field and pressure fluctuation of pat based on entropy production theory," Journal of Energy Storage 69, 107932 (2023).

 ¹⁰K. Kan, Z. Yang, P. Lyu, Y. Zheng, and L. Shen, "Numerical study of turbulent flow past a rotating axial-flow pump based on a level-set immersed boundary method," Renewable Energy 168, 960-971 (2021).

 ¹¹M. Rossi, A. Nigro, and M. Renzi, "Experimental and numerical assessment of a methodology for performance prediction of pumps-as-turbines (PATs) operating in off-design conditions," Applied Energy 248, 555-566 (2019).

- ¹²M. Rossi, and M. Renzi, "A general methodology for performance prediction of pumps-as-turbines using artificial neural networks," Renewable Energy 128, 265-274 (2018).
- ¹³A. Telikani, M. Rossi, N. Khajehali, and M. Renzi, "Pumps-as-Turbines'(PATs) performance prediction improvement using evolutionary artificial neural networks," Applied Energy 330, 120316 (2023).
- ¹⁴A. Nasir, E. Dribssa, M. Girma, and H. B. Madessa, "Selection and performance prediction of a pump as a turbine for power generation applications," Energies 16(13), 5036 (2023).
- 512 ¹⁵ S. Yang, P. Li, Z. Lu, R. Xiao, D. Zhu, K. Lin, and R. Tao, "Comparative evaluation of the pump mode and turbine mode performance of a large vaned-voluted centrifugal pump,"

Frontiers in Energy Research 10, 1003449 (2022).

- ¹⁶ T. Lin, Z. Zhu, X. Li, J. Li, and Y. Lin, "Theoretical, experimental, and numerical methods to
- predict the best efficiency point of centrifugal pump as turbine," Renewable Energy 168, 31-44 (2021).
- 518 ¹⁷S. S. Yang, C. Wang, K. Chen, and X. Yuan, "Research on blade thickness influencing pump as turbine," Advances in Mechanical Engineering 6, 190530 (2014).
- 520 ¹⁸J. Xu, L. Wang, S. Ntiri Asomani, W. Luo, and R. Lu, "Improvement of internal flow performance of a centrifugal pump-as-turbine (PAT) by impeller geometric optimization," Mathematics 8(10), 1714 (2020).
- ¹⁹M. Binama, W. T. Su, W. H. Cai, X. B. Li, A. Muhirwa, B. Li, and E. Bisengimana, "Blade trailing edge position influencing pump as turbine (PAT) pressure field under part-load conditions," Renewable Energy 136, 33-47 (2019).
- 526 ²⁰T. Wang, R. Xiang, H. Yu, and M. Zhou, "Performance improvement of forward-curved impeller with an adequate outlet swirl using in centrifugal pump as turbine," Renewable Energy 204, 67-76 (2023).
- ²¹R. Xiang, T. Wang, Y. Fang, H. Yu, M. Zhou, and X. Zhang, "Effect of blade curve shape on the hydraulic performance and pressure pulsation of a pump as turbine," Physics of Fluids 34(8), 085130 (2022).
- ²²D. Adu, J. Zhang, M. Jieyun, S. N. Asomani, and M. O. Koranteng, "Numerical investigation of transient vortices and turbulent flow behaviour in centrifugal pump operating in reverse mode as turbine," Materials Science for Energy Technologies 2(2), 356-364 (2019).
- 535 ²³T. Xin, J. Wei, L. Qiuying, G. Hou, Z. Ning, W. Yuchuan, and C. Diyi, "Analysis of hydraulic loss of the centrifugal pump as turbine based on internal flow feature and entropy generation theory," Sustainable Energy Technologies and Assessments 52, 102070 (2022).
- ²⁴Q. Si, J. He, S. Miao, J. Liu, A. Asad, and P. Wang, "Study on the energy conversion characteristics in the impeller of USSPAT based on velocity triangle space decomposition," Journal of Energy Storage 72, 108429 (2023).
- 541 ²⁵J. Hu, W. Su, K. Li, K. Wu, L. Xue, and G. He, "Transient hydrodynamic behavior of a pump as 542 turbine with varying rotating speed," Energies 16(4), 2071 (2023).
- 543 ²⁶J. Yin, D. Wang, D. K. Walters, and X. Wei, "Investigation of the unstable flow phenomenon in
- a pump turbine," Science China Physics, Mechanics & Astronomy 57, 1119-1127 (2014).
- 545 ²⁷F. Zhang, D. Appiah, F. Hong, J. Zhang, S. Yuan, K. A. Adu-Poku, and X. Wei, "Energy loss evaluation in a side channel pump under different wrapping angles using entropy production method," International Communications in Heat and Mass Transfer 113, 104526 (2020).
- 548 ²⁸L. Ji, W. Li, W. Shi, F. Tian, and R. Agarwal, "Diagnosis of internal energy characteristics of

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset.

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004 **PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004**

AIP
E Publishing

- - mixed-flow pump within stall region based on entropy production analysis model," International Communications in Heat and Mass Transfer 117, 104784 (2020).
	- 551 ²⁹J. Zhang, D. Appiah, F. Zhang, S. Yuan, Y. Gu, and S. N. Asomani, "Experimental and numerical investigations on pressure pulsation in a pump mode operation of a pump as turbine," Energy Science & Engineering 7(4), 1264-1279 (2019).
	- ³⁰A. Meana-Fernández, J. M. Fernández Oro, K. M. Argüelles Díaz, M. Galdo-Vega, and S. Velarde-Suárez, "Application of Richardson extrapolation method to the CFD simulation of vertical-axis wind turbines and analysis of the flow field," Engineering Applications of Computational Fluid Mechanics 13(1), 359-376 (2019).
	- ³¹X. Sun, G. Xia, W. You, X. Jia, S. Manickam, Y. Tao, S. Zhao, J. Y. Yoon, and X. Xuan, "Effect of the arrangement of cavitation generation unit on the performance of an advanced rotational hydrodynamic cavitation reactor," Ultrasonics Sonochemistry 99, 106544 (2023).
	- ³²X. Sun, W. You, X. Xuan, L. Ji, X. Xu, G. Wang, S. Zhao, G. Boczkaj, J. Y. Yoon and S. Chen," Effect of the cavitation generation unit structure on the performance of an advanced hydrodynamic cavitation reactor for process intensifications," Chemical Engineering Journal412, 128600 (2021).
	- 565 ³³S. J. Daniels, A. A. M. Rahat, G. R. Tabor, J. E. Fieldsend, and R. M. Everson, "Shape optimisation of the sharp-heeled Kaplan draft tube: performance evaluation using computational fluid dynamics," Renewable Energy 160, 112-126 (2020).
	- 568 ³⁴ L. Ji, W. Li, W. Shi, F. Tian, amd R. Agarwal, "Effect of blade thickness on rotating stall of mixed-flow pump using entropy generation analysis," Energy 236, 121381 (2021).
	- 570 ³⁵L. Ji, W. Li, W. Shi, H. Chang, and Z. Yang, " Energy characteristics of mixed-flow pump under different tip clearances based on entropy production analysis," Energy 199, 117447 (2020).
	- ³⁶D. Zhang, W. Shi, D. Pan, and M. Dubuisson, "Numerical and experimental investigation of tip leakage vortex cavitation patterns and mechanisms in an axial flow pump," Journal of Fluids Engineering 137(12), 121103 (2015).
	- 575 ³⁷S. K. Ghai, N. Chakraborty, U. Ahmed, and M. Klein, "Enstrophy evolution during head-on wall interaction of premixed flames within turbulent boundary layers," Physics of Fluids 34(7), 075124 (2022).
	- ³⁸Y. Liu, X. Li, W. Wang, L. Li, and Y. Huo, "Numerical investigation on the evolution of forces and energy features in thermo-sensitive cavitating flow," European Journal of Mechanics-B/Fluids 84, 233-249 (2020).
	- 581 ³⁹ T. Yu, Z. Shuai, X. Wang, J. Jian, J. He, W. Li, and C. Jiang, " Research on wake and potential flow effects of rotor-stator interaction in a centrifugal pump with guided vanes," Physics of Fluids 35(3), 037107 (2023).
	- ⁴⁰K. Kan, Y. Xu, H. Xu, J. Feng, and Z. Yang, "Vortex-Induced energy loss of a mixed-flow waterjet pump under different operating conditions," Acta Mechanica Sinica 39(9), 323064 (2023).
	- ⁴¹A. Kazbekov, K. Kumashiro, and A. M. Steinberg, "Enstrophy transport in swirl combustion," Journal of Fluid Mechanics 876, 715-732 (2019).

ACCEPTED MANUSCRIPT

This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset This is the author's peer reviewed, accepted manuscript. However, the online version of record will be different from this version once it has been copyedited and typeset. PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0192004