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Seismic Retrofit Assessment of a School Building through Operational Modal Analysis and f.e. Modeling

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1	Seismic retrofit assessment of a school building through operational
2	modal analysis and f.e. modelling
3	
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9	
10	Abstract – The paper deals with the dynamic characterisation of a RC frame school building in central Italy before and
11	after the seismic retrofitting, obtained by coupling the building with an innovative patented seismic dissipative protection
12	system. Before the retrofit, ambient vibration tests were performed to evaluate frequencies and mode shapes for developing
13	f.e. models describing the school dynamic behaviour in operational conditions. Several finite element models with
14	increasing level of detail are presented, from the bare frame model, based on the assumptions and simplifications usually
15	adopted for design purposes, to an upgraded model taking account of secondary and non-structural elements (e.g. internal
16	and external walls, screeds, roofing, floor tiles and plasters) as well as the interaction between structure and retaining walls.

17 The latter was used to develop the design model of the seismic retrofitting system, which aims to assure the immediate 18 occupancy of the building in the case of severe earthquakes limiting damage to non-structural components. Tests were 19 repeated after the retrofit to check consistency with numerical design predictions. Comparisons between experimental and 20 numerical modal parameters are shown discussing the usefulness of ambient vibration tests.

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Keywords: Building dynamic identification, ambient vibration test, operational modal analysis, RC frame building
 retrofitting, steel dissipative towers, finite element model upgrading

24 **1. Introduction**

Dynamic identification is an increasingly used technique in civil engineering, particularly for existing buildings. Generally, it is used: *i*) to calibrate structural models to be used for the design of

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27 repair, rehabilitation and retrofit works; *ii*) to assess and validate structural design models for final 28 testing; and *iii*) to monitor the structural health of buildings starting from the evaluation of changes in 29 their dynamic behaviour over time. Various testing techniques differing in terms of equipment, time 30 required, costs, and dynamic input can be adopted. However, Ambient Vibration Test (AVT) is one of 31 the most attractive method for the evaluation of the dynamic characteristics of buildings due to its 32 intrinsic advantages, such as the exploitation of ambient excitations as input instead of forced 33 vibrations, the use of portable and light instrumentation and the possibility to carry out tests without 34 disrupting buildings functionality. Due to the low amplitude range of vibrations ($\approx 10^{-5}$ g) produced by the ambient excitation, only the dynamic behaviour of the building at very small strains can be 35 36 captured through AVTs.

37 Many ambient vibration tests have been executed in the last two decades for the dynamic 38 identification of civil structures such as buildings, bridges, towers, (e.g. [1-10]) and many studies have 39 been developed to assess factors affecting modal parameters (e.g. [11-12]). However, few examples 40 can be found in literature regarding dynamic tests performed on civil structures before and after 41 retrofitting works with the aim to validate a predictive f.e. structural model and to assess the dynamic 42 behaviour variation due to the interventions (e.g. [13-19]). Indeed, data from AVTs (i.e. from tests that 43 are able to capture the building dynamics only at small strains) are affected by contributions of non-44 structural components and can be profitably used to calibrate the linear behaviour of f.e. models in 45 which nonlinearities can be later implemented to perform the seismic assessment of the retrofitted 46 structures. Numerical models should be at least modified to account for the material nonlinearity and 47 the contributions of non-structural components that during earthquake usually undergo damage that 48 reduce interaction phenomena with the structural members.

Finally, although finite element model updating based on experimentally obtained modal parameters is a largely studied and well-known issue in civil engineering, only a few systematic researches concerning the effects of non-structural elements on the overall response of buildings are available in literature (e.g. [20-25]). 53 In this paper ambient vibration tests are exploited to assess a seismic retrofit of a strategic 54 building. In details, the identification of the modal features of an existing low-rise RC frame school 55 building before and after the seismic retrofit is presented discussing the f.e. model upgrading 56 descending from the tests results. The upgraded model includes contributions of the in-plane 57 deformability of floors, internal partitions, external infills and surrounding retaining walls. The 58 specific contribution of the latter features on the overall dynamic structural behaviour is also shown 59 and discussed. The refined model is adopted to design the retrofit system that is achieved with an 60 innovative patented dissipative protection system called "Dissipative Towers" [26-28] that foresees the 61 coupling of the existing building with new external rocking steel truss towers, pinned and equipped 62 with viscous dampers at the base. The refined model, which accounts for both structural and non-63 structural components, was crucial for a proper design of the retrofitting system, which requires a 64 reliable prediction of the building displacements subjected to severe earthquakes in order to limit 65 damage to non-structural members. After the retrofit, the experimental dynamic response of the 66 building is compared with the numerical predictions in terms of modal parameters (natural frequencies 67 and mode shapes). Dynamic tests revealed important to (i) upgrade the design finite element model and (ii) to check that changes in the modal parameters due to the retrofit agreed with those predicted 68 69 through the design model.

70 2 School building description

The school building is located in Camerino, in a high seismicity area in central Italy, as demonstrated by the recent Central Italy earthquake that struck the municipality in 2016. Figure 1 illustrates the plan view and sections of the RC building, which is composed of three blocks (Block A, Block B, and Block C) separated by expansion joints. Block A and Block C, constituted by a 4-storey 3×2 bay frame with an almost square plan (26.0 × 19.5 m), form the front of the building. Block B, at the rear of the building, has 3-storeys and a rectangular plan (12.85 × 28.20 m), and is constituted by frames with 2 bays of 4.0 m and 8.25 m in transverse direction and 7 bays of 3.6 m in longitudinal direction (Figure 2(a)); this part of the building was erected on ancient masonry walls constituting the
lower part of a pre-existing structure.

80 The columns have 40×40 cm square cross sections rotated by 45° with respect to the frame 81 plane. The beams on the building perimeter are linearly tapered with cross sections of about 30×80 82 cm and 30×40 cm at the beam-to-column joint and at mid-span, respectively, whereas the inner 83 beams have constant rectangular cross sections with varying dimensions. The mean compressive strength of concrete is $f_{cm} = 19.71 \text{ N/mm}^2$ and is obtained from an experimental investigation on 22 84 85 core samples extracted from structural elements. The joint between the blocks (red dashed lines in 86 Figure 1(a)) regards only beams and columns (columns straddling the joint have a triangular cross 87 section) while non-structural components (e.g. screeds, floors and infill walls) are continuous through 88 the joints. RC floors are made of prefabricated beams and 20 cm high clay blocks, on which a 4 cm 89 thick slab is cast. Infills of the external frames consist of 30 cm thick brick cavity walls with 90 intermediate insulation having height of about 1.20 m from the floor (below windows), as shown in Figure 2(a). Internal partitions are mostly made with 8 cm thick hollow clay blocks, with plaster on 91 92 both sides; occasionally, very light infill plasterboard partitions are also present.

93 2.1 The retrofit system and the need of dynamic tests for the design

94 Intrinsic geometry of beams and columns, as well as of infills, makes the building vulnerable to seismic actions, despite its social and strategic value. The seismic retrofit of the building was thus 95 96 achieved through a patented dissipative protection system called "Dissipative Towers" [26-28]. In 97 details, two external rocking steel truss towers pinned and equipped with viscous dampers at the base 98 have been positioned in plan according to Figure 1(a). Towers interact with the building at the floor 99 levels, except at the first one ((Figure 1(b) and Figure 2(a)), through steel members which are 100 connected to steel plates anchored to the external frames. Steel members are erected on RC thick base 101 plates that are centrally pinned through a spherical support to the foundations. Viscous dampers are 102 arranged vertically between the base and foundation plates (one device per vertex for tower A and two

103 for tower B), so that the rocking of the tower base, due to the building horizontal displacements, can 104 activate all the devices. Dampers are included into an articulated quadrangle (Figure 2(b)) that 105 amplifies the device displacements thanks to a leverage system. Furthermore, thick steel plates duly 106 anchored to adjacent columns and beams are used to structurally connect adjacent blocks of the 107 building.

108 From a conceptual point of view, the tower stiffness promotes a linear displacement profile and 109 a constant inter-story drift, preventing soft-story collapses, while viscous dampers largely enhance the 110 building dissipative capacity. Since the energy dissipation through dampers is very high, linear 111 dynamic response spectrum analyses are not allowed to assess the seismic performance of the 112 retrofitted system [29] and dynamic nonlinear analyses, involving the use of acceleration time 113 histories, are required. However, nonlinearities are limited to dissipative devices since "Dissipative 114 Towers" are dimensioned to assure a linear elastic behaviour of structural members. For the 115 investigated case study, the retrofit system was designed not only to assure a linear behaviour of the 116 building, but also to limit damage of non-structural elements in case of severe earthquakes (e.g. for 117 actions normally corresponding to the life safety limit state) [29]. For this purpose, the design of the retrofitting system must be carried out suitably considering the overall initial stiffness of the building, 118 119 which is largely affected by contributions of both structural and non-structural components. Indeed, 120 the design numerical model should be able to accurately predict the building displacements and inter-121 storey drifts to which structural and non-structural damage are related.







125 Figure 2. (a) Front and rear view of the school building; (b) viscous dampers at the base of the towers.

Thus, an estimation of the dynamic properties of the building in its operational condition (before the retrofit) is crucial for the development of a reliable numerical model that can be used for the retrofit design and, at the same time, a validation of the design model (i.e. including the retrofit system) is important, considering that the retrofit system must guarantee the building usability (with minor and fast repair interventions) after a severe earthquake.

131 **3** Measurements and operational modal analysis

Ambient Vibration Tests (AVTs) are used to perform a dynamic characterization of the building before and after the retrofit. Modal information from tests executed before the retrofit were used to develop a numerical design model able to account for the building behaviour in its real service conditions while modal information from tests executed after the retrofit were used to validate the design model and its compliance with the real retrofitted structure.

137 3.1 Instrumentation and measurements

138 To measure the building vibrations due to ambient excitation, low noise piezoelectric

accelerometers with a sensitivity of 10 V/g, a frequency range (\pm 10 %) of 0.07 \div 300 Hz, and a broadband resolution of 1 µg root mean square were used. Sensors were connected to a 24-bit data acquisition system with an input range of \pm 5 V by means of low-noise coaxial cables. The maximum measurable accelerations were \pm 0.5 g. A laptop with dedicated software was adopted to store and process the signals (Figure 3).

144 Three accelerometers per floor were used (Figure 4(a)) that are enough to draw the global mode 145 shape of the building capturing the coupled roto-translational motions of floors assumed to be rigid in 146 their plane. For each configuration, 1000-second long records, sampled at a rate of 2048 Hz (the lower 147 limit allowed by the adopted acquisition system), were acquired. This time length largely exceeds the 148 limit of about 1000-2000 times the fundamental period of the building, which is the acquisition length 149 recommended to obtain an accurate estimate of the modal parameters with ambient vibration 150 measurements [30]. In Figure 4(b) the time histories registered by accelerometers 2AX, 2AY and 2BX 151 during one of the tests carried out before and after the retrofitting, are reported. The Root Mean Square 152 (RMS) values of the measured accelerations are reported to show that the excitation levels during the 153 measurements carried out before and after the retrofitting were comparable. RMS of the measured 154 accelerations were calculated considering signal bands filtered in the frequency range that mainly 155 characterise the dynamic behaviour of the building, i.e. 3-5 Hz.

For the measurements carried out before the retrofitting works, only 3 accelerometers were available, two of which, considered as references, were located at point A on the second floor (2AX and 2AY), while the third sensor (roving sensor) was moved around to all the other positions. For the analysis carried out after the retrofitting works, 12 accelerometers were available and only one configuration was necessary. However, three different acquisitions were carried out keeping the same sensor configuration, to better estimate the variability of the parameters identified thanks to data redundancy. Further details can be found by the reader in [31].

During tests, the air temperature and relative humidity were monitored outside the building; a temperature range of 19-22 °C and a relative humidity of about 60 % was observed during

- 165 measurements carried out before the retrofitting works in August 2012 while a temperature range of
- 166 17-20 °C and a relative humidity of about 74 % was registered during tests performed after the retrofit
- 167 in May 2013. Moreover, the wind velocity was quite low during both tests.

169

Figure 3. Measurement equipment during tests.

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171 Figure 4. (a) Layout of accelerometers; (b) filtered acceleration time histories with RMS values, before and after

Environmental parameters, especially wind velocity and environmental temperature, are known to affect the modal parameters of structures [32-35]; however, considering similarities of excitation levels and environmental conditions relevant to the two tests, it can be concluded that changes in the modal parameters of the building can be almost completely attributed to effects of the retrofitting works.

178 *3.2 Signal processing and operational modal analysis*

179 Standard signal processing techniques were applied to all the recorded data before carrying out 180 modal analyses. First, a correction of the spurious trends of signals was performed by subtracting the 181 contribution resulting from the signals fitting with a third-degree polynomial. Then, the records were 182 filtered with a low-pass filter with a cut-off frequency of 20 Hz to avoid aliasing phenomena. Finally, 183 the signals were down-sampled at 51.2 Hz to reduce the number of data and make subsequent analyses 184 faster. The modal parameters of the building (natural frequencies, damping ratios mode shapes) were 185 identified using two output-only techniques implemented in Matlab environment [36]: the Enhanced 186 Frequency Domain Decomposition (EFDD) method [37,38] and the Covariance-driven Stochastic 187 Subspace Identification (SSI-COV) method [39-42]. Considering that very close results have been obtained with the two methods, only results from the SSI-COV method are herein presented. In this 188 189 work, a model order of 50 is used and, in the stabilisation diagrams (Figure 5), a mode is assumed 190 consistent with reference to frequency, damping ratio and mode shape when, by increasing the model 191 order, it shows a natural frequency variation < 1% (green cross), a damping ratio variation < 2% (red 192 circle), and a Modal Assurance Criterion (defined in the following section) MAC > 0.98 (cyan star), 193 respectively.

194 *Comparison between mode shapes*

To compare mode shapes and obtained from measurements before and after the building
retrofitting, the Modal Assurance Criterion (MAC) [43], was used.

199

Figure 5. Stabilisation diagrams (SSI-COV) for measurements before and after retrofitting works.

(1)

200 This criterion is defined as

201

and provides a numeric value that assesses the correspondence between two mode shapes. MAC value is 1 for perfectly matching mode shapes (parallel vectors) and 0 for completely different mode shapes (orthogonal vectors). In the following, MAC values are presented in matrix form exploiting a greyscale ranging from white (MAC = 0) to black (MAC = 1).

206 4 Modal features from ambient vibration tests

207 4.1 Tests before retrofitting

208 The left half side of Table 1 presents the resonance frequencies f and damping ratios ξ of the first 209 seven modes identified before retrofitting. The values of damping ratios ξ relevant to the first seven 210 modes vary between 0.9 and 2.6%, showing a quite high variability, which is rather usual for 211 buildings and civil engineering structures when identified through ambient vibration testing. As for 212 mode shapes, a 3D isometric view is reported in Figure 6(a) (the last floor of block A is not included 213 because it was not monitored). Furthermore, the basement results to be practically fixed since its 214 modal displacements are negligible compared to those of the upper floors. The first three modes are 215 those typical for low-rise RC frame buildings and can be assimilated to a first transverse mode with

torsional component, a first torsional mode, and a first longitudinal mode with torsional component. A
significant torsional component is always present due to the L-shaped plan of the building. The
subsequent two mode shapes cannot be clearly assimilated to standard mode shapes while the sixth and
the seventh are similar to the second torsional and transverse modes, respectively.

220 4.2 Tests after retrofitting

The right half side of Table 1 reports values of the natural frequencies f and the damping ratios ξ of the first seven modes identified while the identified mode shapes are shown in Figure 6(b). The latter appear like those obtained from tests executed before retrofitting and small differences cannot be clearly recognised through the graphical representation. The first three modes are again those typical of low-rise RC frame buildings: a first transverse mode, a first torsional mode, and a first longitudinal mode, all with a significant torsional component. The fifth and the sixth modes are assimilable to second modes, longitudinal and transverse, respectively.

228 4.3 Comparison between the results of the tests performed before and after retrofitting

Despite above mentioned similarities, significant changes in the building dynamic behaviour are found from the comparison of results obtained from tests performed before and after the seismic retrofit, denoted with subscripts b and a, respectively. It is worth noting that the modal parameters of real buildings identified by means of operational modal analysis at different times are generally affected by a certain variability.

Table 1. Modal parameters before and after retrofitting.

	Before		Af	ter	-
mode	mode $f_{ex,b}$ $\xi_{ex,b}$		f _{ex,a}	$\xi_{ex,a}$	Mode shape
	[Hz]	[%]	[Hz]	[%]	
1 st	3.61	1.46	3.60	1.49	first transverse
2^{nd}	3.70	1.69	3.82	1.96	first torsional
3 rd	4.00	1.14	4.14	1.49	first longitudinal
4^{th}	4.41	0.92	5.00	1.17	/
5^{th}	7.25	1.16	7.69	1.15	/
6^{th}	8.69	2.58	9.54	2.18	/
7^{th}	9.89	2.41	10.50	3.30	/

237

Figure 6. Resonance frequencies and mode shapes (a) before and (b) after retrofitting.

This is due not only to signal acquisition and processing but also to random changes in a number of factors such as amount and distribution of masses inside the building as well as environmental conditions (e.g. wind, temperature, humidity). However, these uncertainties generally induce much smaller variations in modal parameter values than those identified for the case under discussion.

242 Interesting considerations can arise when observing the changes in the values of resonance 243 frequencies and damping ratios, as well as when comparing mode shapes [44]. To facilitate the reader, 244 the values of the first seven resonance frequencies identified before and after the building retrofit are 245 listed in Table 2. Except for the first mode, a general increase, ranging between 0.12 and 0.85 Hz, with 246 an average value of about 6 % can be observed after the retrofit. This can be interpreted as a 247 consequence of a general increase in the stiffness of the building coupled with steel towers. In 248 particular, it is worth observing that the first resonance frequency is practically unchanged and that the 249 second and the third frequencies undergo a small increment.

Table 2. Experimental resonance frequencies before $(f_{ex,b})$ and after $(f_{ex,a})$ the building retrofit.

mode	f _{ex,b} [Hz]	f _{ex,a} [Hz]	(fex,b-fex,a) / fex,b [%]
1^{st}	3.61	3.60	-0.2
2^{nd}	3.70	3.82	3.0
3 rd	4.00	4.14	3.6
4^{th}	4.41	5.00	13.4
5^{th}	7.25	7.69	6.1
6 th	8.69	9.54	9.8
7 th	9.89	10.45	5.7

251 Conversely, the higher frequencies present greater increments, particularly the fifth, the sixth and 252 the seventh increase by about 6.1 %, 9.8 % and 5.7 %, respectively. This behaviour is consistent with 253 the adopted retrofitting system that foresees stiff steel towers free to rotate at their base and only 254 connected to the building in correspondence of the floors. As a consequence, towers do not add much 255 stiffness with respect to modes that involve an almost-linear deflection of the building, i.e. the first 256 three modes. Conversely, they strongly increase the stiffness with respect to higher modes that imply a 257 non-linear deflection of the building vertical profile, i.e. with non-uniform values of inter-storey drift. 258 Furthermore, the increase in the resonance frequency values is also partially due to the stitching of 259 joints separating the building blocks (before the retrofit the interactions among blocks are only due to 260 non-structural components). This effect is more pronounced for modes involving relative movements 261 between blocks (e.g. the fourth), as will be shown later through a refined f.e. model of the structure.

Regarding damping ratios, typical values ranging between 1.5-3.0% are obtained, as usual for 262 263 AVTs on RC low-rise buildings. It should be remarked that the dissipative contribution of the towers 264 cannot be captured with AVTs, because dissipative devices are not activated by low amplitude 265 vibrations. Finally, mode shapes identified before and after the building retrofit remain quite similar and the differences cannot be clearly identified graphically; thus, differences are captured analytically 266 267 by means of MAC in Figure 7a. Very little differences can be observed for the first four modes while a 268 variation in the higher modes (especially the fifth and the sixth) appears evident; this confirms 269 considerations already made about changes of the natural frequencies, which are more evident for 270 higher modes. Indeed, the rigid steel towers connected at the base through a spherical hinge contribute 271 to linearize the profiles of horizontal displacements of the building. Thus, the tower-building 272 interactions are more evident for higher modes, which are characterised by nonlinear profiles of 273 horizontal displacements whereas effects on lower modes are less pronounced, since displacement 274 profiles are closer to linearity. For lower modes, the contribution of the towers to the regularisation of 275 mode shapes can be better appreciated by means of the MAC between the experimental mode shapes 276 and a perfectly linear deflection.

Figure 7. (a) MAC between mode shapes before and after retrofitting; (b) profile of modal displacements at AX
and AY before and after retrofitting, and MAC values with an ideal linear deflection of the building.

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Figure 7b shows components of modal displacements of the first three modes in the two principal directions of the building in correspondence of alignments AX and AY for both the pre-retrofitted (blue lines) and retrofitted (red lines) conditions. In order to compare the profiles of modal displacements with respect to an ideal linear deflection of the building, MAC values between the experimental modal displacements and a linear trend are computed and reported in the figure with the relevant colour. A general increase in the MAC value, corresponding to a regularisation of the modes (i.e. mode shapes closer to a linear shape), is obtained, especially for the second and the third modes.

288 **5 3D finite element models**

289 5.1. Building before retrofitting

A predictive refined finite element model for the seismic retrofit design of the existing building was developed in SAP2000 code [45]. The numerical model is based on available structural drawings of the building and in-situ measurements as well as destructive and non-destructive tests on the structural materials, i.e. extraction of concrete core samples to estimate the strength and elastic 294 modulus of concrete, sonic tests to control the homogeneity of concrete elements and surveys using an
295 electromagnetic cover meter to investigate position, depth and size of steel reinforcement.

296 Beams and columns are modelled with 2-nodes frame elements while slabs and walls are 297 schematised with 4-nodes shell elements having six degrees of freedom (dof) per node. Prismatic 298 frame elements are used for columns and internal beam sections, whereas non-prismatic frame 299 elements are chosen for tapered external beams. About the latter, the major moment of inertia (bending 300 in vertical plane) of the cross section is assumed to vary along the beam axis with a parabolic law, 301 whereas the minor moment of inertia (bending in horizontal plane) varies linearly. The shell elements are discretised into almost rectangular elements with an area of about 0.1 m². This value was obtained 302 303 according to preliminary convergence analysis, by gradually reducing the shell size up to a non-304 significant variation in the values of the natural frequencies. To consider the stiffening effect due to the 305 intersection of the members at the beam-to-column joints, rigid-end offsets equal to the 70% of the 306 nominal overlapping length are assumed for frame elements connecting to the nodes. The columns of 307 Block A and Block C are fully restrained at the building basement. Being the building founded on 308 cemented sandstone, this assumption is assumed to be quite representative of the structural behaviour 309 of the building at operational condition. The columns of Block B are, instead, rigidly connected to the 310 shells of the masonry walls constituting the foundations.

311 The masses of the structural elements (i.e. RC beams and columns) are automatically computed 312 by the software according to assigned frame element cross sections and material properties. The 313 masses of the external walls are uniformly distributed along the perimeter beams, whereas the masses 314 of the floors, composed of structural slabs and non-structural elements (screeds, roofing, floor tiles and 315 plasters), as well as those of the internal partition walls and furniture (considered as equivalent 316 distributed loads) are considered lumped at beams that are orthogonal to the slabs orientation. Live 317 loads are not considered initially, in order to simulate the real condition of the building during the test 318 and to allow the model validation through comparisons of numerical and experimental results; in Table 3 the values of self-weight of both structural and non-structural elements are listed forcompleteness.

321 Materials are assumed to behave elastically, with properties reported in Table 4; the static Young's modulus of concrete is derived from the mean value of the concrete strength ($f_{cm} = 19.71$ 322 N/mm²) as suggested by the Italian Standards [29]. The reduced modulus of elasticity, $E_{c,red}$, is 323 assumed to be 65% of the static modulus, while the dynamic modulus of elasticity is obtained by 324 325 increasing the static modulus by about 20% [46], to capture the dynamic behaviour at very low 326 amplitude vibrations. The values of the static elastic modulus and mass of the retaining walls, as well 327 as those of internal and external walls, are chosen according to the Italian Standards [47], depending 328 on the masonry typology. Due to the lack of information available in the literature, the dynamic 329 modulus of elasticity is obtained by increasing the static modulus by 20%, analogously to the concrete. 330 The following six different models with increasing degree of accuracy are developed.

331 - Mod. 0a and Mod. 0b (Figure 8(a)) are the bare frame models usually developed for design 332 purposes. The internal partitions and external walls are not modelled, a rigid diaphragm is considered 333 for each floor (i.e. infinite in-plane stiffness and null out-of-plane stiffness of the slabs), stairs and foundation walls at the base of Block B are modelled with shells. For the verifications in terms of 334 335 Ultimate Limit States (ULS), the reduced value of the static modulus of the elasticity of concrete, $E_{c,red}$, is considered to account for concrete cracking (Mod 0a), whereas, for the verifications in terms 336 337 of Service Limit States, the full static value is usually adopted to consider uncracked concrete 338 conditions. In this case, to detect the behaviour at very low strain levels during operational conditions 339 (ambient vibrations), the dynamic elastic modulus $E_{c,dyn}$ is adopted (Mod 0b).

- **Mod. 1** takes account of the contribution of the external retaining wall by modelling the basements of Blocks A and C with shell elements, having dynamic modulus of elasticity $E_{rw,dyn}$, and by considering the stiffness contribution given by the soil surrounding the wall. The latter is included by means of supports restraining horizontal displacements and located at the first level in the front part of Blocks A and C.

Table 3. Loads of structural and non-structural members.

	Typical floor	Last floor	Roof	Stairs of block C	Stairs of block B
Structural [kN/m ²]	3.20	3.20	2.80	3.75	3.00
Non-structural [kN/m ²]	1.80	0.60	0.60	1.20	1.20
Non-structural [kN/m]	4.60				

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Table 4. Elastic modulus [N/mm²] and weight [kN/m³] of concrete members and walls.

Concrete		Retaining wall		Exter	External wall		Internal wall	
$E_{c,st}$	25497	$E_{rw,st}$	3360	$E_{w,st}$	4583	$E_{w,st}$	3208	
$E_{c,dyn}$	30720	$E_{rw,dyn}$	4032	$E_{w,dyn}$	5500	$E_{w,dyn}$	3850	
$E_{c,red}$	16573	$E_{rw,red}$	/	$E_{w,red}$	/	$E_{w,red}$	/	
W	25	W	22	W	20	W	12	

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- Mod. 2 considers the in-plane deformability and bending stiffness of the floors by removing diaphragms and modelling slabs with anisotropic shells, which have inertia and stiffness characteristics equivalent to those of the reinforced concrete slab with a T-cross section coupled with screed and tiles, in the longitudinal direction, and to those of the slab flange coupled with screed and tiles, in the transverse direction. Furthermore, the self-weight plus other loads imposed on the floor are considered as uniform loads applied to the shells.

- Mod. 3 takes into account the contributions of the internal partitions and external walls, which are modelled with shell elements having elastic modulus $E_{w,dyn}$ and thickness (masonry and plaster) of 0.12 m and 0.2 m, for internal partitions and external walls, respectively.

- **Mod. 4** (Figure 8(b)) accounts for the contribution of the soil surrounding the building; the supports located at the floor level are replaced with springs that are orthogonal to shells representative of the retaining walls. The spring stiffness is 8144 kN/m, corresponding to a subgrade reaction value of 80000 kN/m³, according to Bowles [48], who suggests the range 80000-96000 kN/m³ for a mediumdense sand. This final model is very accurate and rather complex, involving 2403 frame elements, 69291 shells, and 70743 nodes. Numerical natural frequencies and mode shapes are obtained through an eigenvalue analysis and are compared with the experimental ones. Values of the natural frequencies of the first four modes of each model are graphically shown in Figure 9 proving a direct comparison with the corresponding experimental modes. For each model, the type of mode shape is also indicated, when it is clearly similar to a standard mode for buildings, i.e. transverse, longitudinal, and torsional modes, with reference to the directions *x* and *y* and to the rotation φ (around *z*), respectively.



Figure 8. 3D f. e. model of the building pre-retrofitting: (a) extruded view of the global model Mod.0a; (b)
global model Mod. 4 (links not in view).

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Figure 9. Natural frequencies obtained with f.e. models.

377 The bare frame model (Mod. 0a), usually adopted for structural design, shows values of natural 378 frequencies much lower than the experimental ones (e.g. the first frequency is about one fifth). A 379 significant increase in these theoretical values of about 30 % is obtained with Mod. 0b, thanks to a 380 much higher value of the modulus of elasticity assumed for the concrete, $E_{c,dyn}$ instead of $E_{c,red}$ 381 (increment of about 85%). It is worth noting that also the sequence of the modes disagrees with the 382 experimental one: the first theoretical mode is mainly a transverse mode, the second is a longitudinal 383 mode, and the third a torsional mode, whereas the first three experimental modes were mainly 384 transverse, torsional and longitudinal modes, respectively. A further significant increase in the values 385 of the first three natural frequencies (of about 63 %, 45 % and 28 %, respectively) is obtained with 386 Mod. 1, thanks to the stiffening contribution given by the retaining walls and supports positioned at the 387 ground level in the front part of the building.

With Mod. 2 a slight increase in the values of the first two natural frequencies is obtained, due to the bending stiffness of the shells introduced to model the floor. Vice versa, there is a decrease of about 13-17 % in the values of the third and the fourth natural frequencies that, being related to modes involving in-plane deformations of floors, are much more affected by the removal of the diaphragms that constrain the floor nodes avoiding in-plane deformations. It is worth noting that for all the models discussed so far, the longitudinal mode anticipates the torsional one in disagreement with the experimental results.

With Mod. 3 important modifications to the modal properties of the building are observed: the sequence of the modes now agrees with the experimental one, the values of the first three natural frequencies become almost twice those of Mod. 2 and quite close, even if slightly higher, to the experimental ones. These evidences confirm that the contribution of internal partitions and perimeter walls is of primary importance in the dynamic behaviour of the building for low-level vibrations.

Finally, Mod. 4, in which the supports located at the ground level are removed and the contribution of the soil surrounding the retaining wall is modelled with elastic springs, shows values of the natural frequencies that are slightly lower than those of Mod. 3 and close to the experimental ones. Figure 10 shows the first seven mode shapes obtained with Mod. 4, whereas Table 5 illustrates the comparison between numerical (Mod. 4) and experimental modal parameters, i.e. the percentage difference between the values of natural frequencies and MAC values between mode shapes. A good agreement between numerical and experimental values of the natural frequencies is obtained, with a difference of about -5 % and -0.54 % for the values relevant to the first and the second modes and ranging between 2.50 % and 10.41 % for the higher modes.



409 410

Figure 10. Mode shapes of Mod. 4 (shells and links not in view).

411

412 Table 5. Comparison between experimental and numerical (Mod. 4) modal parameters of the building before

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	Experimental <i>f</i> _{ex,b} [Hz]	Numerical $f_{n,b}$ [Hz]	$(f_n - f_{ex})_b / f_{ex,b}$ [%]	MAC	
1 st mode	3.61	3.43	-4.99	0.93	
2 nd mode	3.70	3.68	-0.54	0.99	
3 rd mode	4.00	4.10	2.50	0.97	
4 th mode	4.41	4.72	7.03	0.98	
5 th mode	7.25	7.55	4.14	0.75	
6 th mode	8.69	9.07	4.37	0.72	
7 th mode	9.89	10.92	10.41	0.94	

retrofitting.

The MAC values show a very good correspondence with values ranging between 0.93 and 0.99 for the first four mode shapes and the seventh one, while higher modes present slightly lower values. It is worth mentioning that in practical applications the dynamic response of low-rise RC buildings is usually accurately estimated considering the contribution of the first modes.

418 5.2. Building after retrofitting

Starting from Mod. 4, a numerical finite element model that includes external towers and plates used to connect adjacent structural members close to the separating joints (Figure 11(a)) is developed and used for the retrofit design Hereafter, this model is referred to as Mod. 5 and is used for the estimation of the dynamic parameters of the retrofitted structure, which will be compared with results of experimental tests executed after the retrofit.

424 The steel towers are modelled with frame elements, while 0.5 m thick shell elements are used for 425 the base plate. A hinge at the centroid of the intrados of the base plate restrains possible tower 426 translations, while rotations are free. Articulated quadrangles that include dissipative devices, each 427 modelled with two elastic frames (one horizontal and one vertical) and one link element, simulating 428 the damper, are located at the vertexes of the base plate. The horizontal elastic frame is pinned at 1/3 of 429 its length, while the vertical frame that includes the link is pinned both at the base plate and the 430 horizontal frame (Figure 11(b)). Considering that the viscous dampers are not activated by very low 431 amplitude vibrations as those registered during ambient vibration tests, the dissipative contribution of 432 the devices is not accounted for. On the other hand, their elastic stiffening contribution is modelled by 433 means of link elements. Assuming that the fluid inside the device does not flow between the two 434 chambers of the device, the elastic stiffness K can be estimated, considering the fluid compressibility, 435 as

437 where *A* (70.04 cm²) and *h* (5.5 cm) are the cross section and the height of the fluid chamber, 438 respectively, and *B* (105500 N/cm²) is the bulk modulus of the viscous fluid. The towers are connected 439 at each floor level, except for the first, by means of elastic elements hinged at the ends. Moreover, to 440 model the intervention aimed at the structural connection of the three building blocks, frame elements 441 are introduced to simulate the stiffness characteristics of the steel plates positioned on adjacent 442 columns and beams, straddling the joints between two blocks. With regard to the materials, the values 443 of the elastic moduli are assumed accordingly to the design parameters: $E_a = 200000$ MPa for the steel 444 elements of the towers and $E_{c,d} = 38770$ MPa for the concrete of the base plates.

445 Table 6 presents a comparison between the modal parameters obtained from the numerical model 446 and the experimental tests executed after the building retrofit in terms of percentage difference for 447 frequencies and MAC values for the identified mode shapes (Figure 12). A good agreement between 448 the numerical and experimental values of the natural frequencies is obtained, with a difference of less 449 than 5% for values relevant to the first three modes as well as the fifth and the sixth. More scattered 450 values are obtained for the fourth and the seventh modes. The MAC values show a very good 451 correspondence for the first four mode shapes, with values ranging between 0.97 and 0.99, and a good 452 agreement for the higher mode shapes, with values ranging between 0.80 and 0.86.



454 Figure 11. 3D f. e. model of the building post-retrofitting: (a) global model Mod. 5 (links not in view); (b) detail
455 of the dissipative system.

(a)

456 Table 6. Comparison between the experimental and numerical (Mod. 5) modal parameters of the building after

	retrofitting.						
mode	Experimental	Numerical	$(f_{n,a} / f_{ex,a}) / f_{ex,a}$	MAC			
	[Hz]	[Hz]	[%]				
1^{st}	3.60	3.48	-3.33	0.99			
2^{nd}	3.82	3.85	0.79	0.99			
3^{rd}	4.14	4.23	2.17	0.98			
4 th	5.00	5.57	11.40	0.97			
5^{th}	7.69	8.06	4.81	0.86			
6 th	9.54	9.41	-1.36	0.80			
7^{th}	10.45	11.87	13.59	0.86			

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460

461 5.3 Comparison between results of FE models before and after retrofitting

When comparing the numerical results obtained with Mod. 4 and Mod. 5 (building before and after retrofitting, respectively) in terms of natural frequencies (Table 7) and mode shapes by means of the MAC criterion, considerations analogous to those already made when discussing the experimental results hold. Due to the tower flexural stiffness and the structural connections of the building blocks, an increase in the natural frequencies of the building is observed.

Figure 12. Mode shapes of Mod. 5 (shells and links not in view).

mode	$f_{n,b}$ [Hz]	$f_{n,a}$ [Hz]	$(f_{n,a,-}f_{n,b}) / f_{n,b}$ [%]	MAC
1 st	3.43	3.48	1.46	0.97
2^{nd}	3.68	3.85	4.62	0.99
3^{rd}	4.10	4.23	3.17	0.99
4 th	4.72	5.57	18.01	1.00
5^{th}	7.55	8.06	6.75	0.99
6 th	9.07	9.41	3.75	0.99
7^{th}	10.92	11.87	8.70	0.96

retrofitting (Mod. 5).

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This increase is low for the first three modes ("linear" modes), ranging between 1.46 and 4.62 %, while it becomes more important for higher modes, with an increment ranging between 3.75 and 8.70 %. Finally, a significant increase of 18.01 % is observed for the fourth mode, as it involves inplane relative rotations between the building blocks, which are more restrained after the retrofitting. With reference to mode shapes, values of MAC greater than 0.95 demonstrate that very small differences are observed for the first seven modes, consistently with the features of the protection system.

477 **6** Conclusions

478 In this paper, the experimental and numerical modal properties of a school building before and 479 after seismic retrofitting with external steel towers equipped with dissipative devices have been 480 presented. Since the retrofitting system must guarantee the building usability after severe earthquakes, 481 the design must be carried out with a model addressing the actual dynamic properties of the building, 482 which strongly depends on both structural and non-structural members. In this framework, experimental modal parameters obtained from ambient vibration measurements are used to upgrade a 483 conventional structural f.e. model of the building to be used for the retrofit design, including 484 485 contributions of the in-plane deformability of floors, internal partitions, the external infills and the

486 surrounding retaining walls. The role of the above usually neglected aspects on the overall dynamic487 structural behaviour is shown by progressively refining the building modelling.

Natural frequencies and mode shapes of the refined f.e. model are in good agreement with the experimental ones, with both reference to fundamental and higher modes, demonstrating the reliability of the model. The model was used for the design of the seismic protection system and provides the expected modal parameters of the retrofitted building that are used to assess the actual stiffening contributions of the retrofit.

493 By comparing the modal parameters of the building before and after retrofitting, an overall 494 increase in the resonance frequencies has been observed. This increase is low for the first three modes 495 (predominantly the first transverse, torsional and longitudinal modes), while it is more pronounced for 496 the higher modes, as expected by numerical predictions. Furthermore, by comparing the mode shapes 497 obtained before and after the building retrofit by means of the modal assurance criterion, it resulted 498 that the first mode shapes remain almost unchanged while those related to the higher modes undergo 499 greater variations, consistently with the peculiarities of the adopted protection system and the 500 numerical expectations.

501 Overall, the dynamic identification of the building through ambient vibration tests revealed 502 crucial for the development of a refined reliable f.e. model for the seismic protection system design, 503 and the subsequent assessment of the actual stiffening contribution of the retrofit (dynamic proof test). 504 This is of paramount importance when the seismic retrofit is designed to limit damage to non-505 structural components under seismic actions, because both structural and non-structural elements 506 contribute to the overall dynamic response of the construction.

507 Data availability statement

508 Some or all data, models, or code that support the findings of this study are available from the 509 corresponding author upon reasonable request.

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