



UNIVERSITÀ POLITECNICA DELLE MARCHE
Repository ISTITUZIONALE

Composite fatigue failure of cold recycled material mixtures: new insights into the role of bitumen and cement

This is the peer reviewed version of the following article:

Original

Composite fatigue failure of cold recycled material mixtures: new insights into the role of bitumen and cement / Graziani, A., Spadoni, S., Ingrassia, L.P., Virgili, A., Canestrari, F.. - In: MATERIALS AND STRUCTURES. - ISSN 1871-6873. - ELETTRONICO. - 57:1(2024). [10.1617/s11527-023-02285-8]

Availability:

This version is available at: 11566/325582 since: 2023-12-30T15:45:06Z

Publisher:

Published

DOI:10.1617/s11527-023-02285-8

Terms of use:

The terms and conditions for the reuse of this version of the manuscript are specified in the publishing policy. The use of copyrighted works requires the consent of the rights' holder (author or publisher). Works made available under a Creative Commons license or a Publisher's custom-made license can be used according to the terms and conditions contained therein. See editor's website for further information and terms and conditions.

This item was downloaded from IRIS Università Politecnica delle Marche (<https://iris.univpm.it>). When citing, please refer to the published version.

(Article begins on next page)

Composite fatigue failure of cold recycled material mixtures: new insights into the role of bitumen and cement

Andrea Graziani^a, Sara Spadoni ^a, Lorenzo Paolo Ingrassia ^{a,*}, Amedeo Virgili ^a,
Francesco Canestrari ^a

^a Università Politecnica delle Marche, Via Brecce Bianche, 60131 Ancona, Italy

* Corresponding Author: l.p.ingrassia@pm.univpm.it

Abstract

In pavement engineering, cold recycled material (CRM) mixtures allow implementing circular economy concepts by maximizing the reuse of reclaimed asphalt without heating. Along with bitumen emulsion and foamed bitumen, Portland cement is often added to CRM mixtures to improve the field performance. However, the role of cement on the fatigue failure is not sufficiently investigated. The objective of this research is to provide new insights into the fatigue failure of CRM mixtures produced with bitumen emulsion and cement. To this aim, two CRM mixtures prepared with different dosages of cement (1% and 2%) were subjected to uniaxial cyclic tension fatigue tests. Empirical and energy-based failure criteria, originally developed for asphalt concrete mixtures, were used to define the fatigue failure. The results showed that the fatigue failure mechanism of CRM mixtures was of a composite type, affected by both cementitious and bituminous bonds. A new criterion was proposed to identify the failure of the cementitious bonds.

Keywords

Pavement; Cold recycling; Fatigue failure; Uniaxial test; Cement; Bitumen emulsion.

23 1. Introduction

24 Implementing circular economy concepts for achieving a sustainable development is a key goal of
25 our society [1]. In pavement engineering, such concepts are put into practice by cold recycling
26 technologies that allow reusing large amounts of reclaimed asphalt (RA) without heating. Compared
27 to traditional hot mix asphalt (HMA) mixtures, cold recycled material (CRM) mixtures allow
28 reducing greenhouse emissions and energy consumption [2][3][4][5]. Moreover, pavement structures
29 containing courses built with CRM mixtures can have excellent long-term performance
30 [6][7][8][9][10].

31 Among CRM mixtures, different families can be identified, depending on the type and amount of
32 employed binding agents. Cement treated material (CTM) mixtures are produced if recycling is
33 carried out by adding only Portland cement. Their load-related failure is normally due to fatigue
34 [11][12]. If recycling is carried out by adding a small amount of bitumen (normally between 1.5%
35 and 2.5%) bitumen stabilized materials (BSM) are produced. BSM are considered as improved
36 granular materials and may include up to 1% Portland cement or other active fillers, like hydrated
37 lime. The load-related failure of BSM is primarily due to permanent deformation [13][14]. Cement
38 bitumen treated materials (CBTM) are produced with similar bitumen dosages but with higher
39 dosages of Portland cement (normally between 1.5 and 4.0%). Load-related failure of CBTM is
40 primarily due to fatigue [15][16][17].

41 The practical fatigue characterization of CRM mixtures has been routinely carried out in indirect
42 tension configuration [16][17][18][19][20]. Some Authors have also performed cyclic bending tests
43 on beam specimens [21][22][23]. The main limitation of those test configurations is that the stress-
44 strain distribution within the specimen is not homogeneous [24]. A homogeneous stress-strain
45 distribution is obtained with uniaxial tests on cylindrical specimens [25]. So far, only a couple of
46 studies have characterized the fatigue behaviour of CRM mixtures through uniaxial tests [26][27]. It

is readily apparent that very limited data are available in the literature, and none of these data refer to the case of CBTM mixtures.

Within this general context, the present research is part of a larger project that has the ultimate goal of evaluating the applicability of the viscoelastic continuum damage (VECD) theoretical-experimental framework to CRM mixtures. As a first necessary step, the objective of this paper is to provide new insights for understanding the fatigue failure of CRM mixtures. To this aim, two CRM mixtures produced with bitumen emulsion and different dosages of Portland cement were subjected to uniaxial cyclic tension fatigue tests. Empirical and energy-based failure criteria, originally developed for asphalt concrete (AC) mixtures, are used to define the fatigue failure. A fatigue failure mechanism that highlights the role of cement and a specific failure criterion are finally proposed.

2. Materials and methods

2.1 Materials

Two CRM mixtures, identified as CRM1 and CRM2, were investigated. Figure 1 shows their target gradation curve that was obtained by mixing 90 % of RA aggregate (RA 0/16) and 10 % of limestone filler [28]. The bitumen emulsion was a commercial cationic slow-setting type, modified with styrene-butadiene-rubber latex and designated C60BP10 according to EN 13808 [29]. For both mixtures, the dosage (by dry aggregate mass) of bitumen emulsion was 4.0 % (residual bitumen 2.4 %) and the total water content was 4.5 % (1.6 % bitumen emulsion water plus 2.9 % pre-wetting water).

The Portland cement was a type II/A LL, strength class 42.5 according to EN 197-1 [30]. Its dosages were 1.0 % and 2.0 % (by dry aggregate mass) for CRM1 and CRM2, respectively. CRM2 is a CBTM mixture typically produced in Europe for base and binder courses [31][32]. CRM1 may be considered a BSM and thus, in the field, its failure is expected to be caused by permanent deformation accumulation rather than fatigue. Nonetheless, it was included in the present experiment to verify if its fatigue failure characterization is possible.

71 The fatigue behaviour of the two CRM mixtures is compared to that of two typical AC mixtures for
 72 binder courses tested in a previous study [33]. One mixture (AC1) was produced with neat bitumen
 73 (PG 70-22) and the other (AC2) with styrene-butadiene-styrene (SBS) polymer modified bitumen
 74 (PG 82-16). The AC mixtures had similar aggregate gradations (dense graded, only virgin aggregates)
 75 and bitumen dosage of 4.5 % by mixture mass.

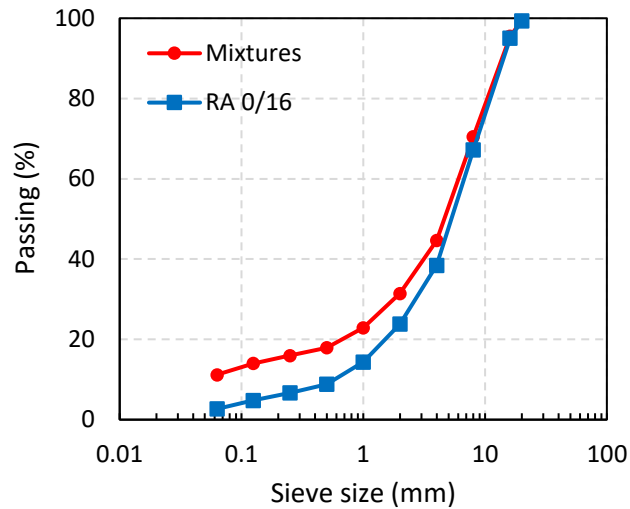


Figure 1. Gradation curves

79 2.2 CRM specimen preparation

80 The RA aggregate was initially dried at 40 °C, then the filler and part of the pre-wetting water (equal
 81 to the water absorption of the RA aggregate) were added and manually mixed. The wet blends were
 82 sealed in plastic bags for 12 h at room temperature to allow a uniform moisture distribution.
 83 Afterwards, the cement, the remaining pre-wetting water and the bitumen emulsion were gradually
 84 added and mixed, alternating manual and mechanical mixing [34].

85 From each mixture batch, one cylindrical specimen was prepared using a gyratory compactor with
 86 vertical pressure of 600 kPa, rotation speed of 30 rpm and external angle of inclination of 1.25° [35].
 87 In total, ten specimens with diameter of 150 mm and height of 180 mm were compacted at the target
 88 voids content of 14.0 % (five from CRM1 and five from CRM2). It is worth noting that voids of

89 readily compacted CRM mixtures include the volume of air and intergranular water [36]. All
90 specimens were extracted from the mould immediately after compaction.

91 A two-stage curing procedure was adopted. The gyratory specimens were cured for one day in the
92 oven at 40 °C (dry environment), and then enclosed in plastic bags and cured until 28 days in a
93 climatic chamber at 40 °C (moist environment). In the first stage, the curing of the bituminous binder
94 is facilitated thanks to the moisture loss due to evaporation, whereas in the second stage the hydration
95 of the cementitious binder is promoted using the residual water present in the mixture [37]. This
96 procedure was adopted because is somewhat similar to what happens in the field, where free
97 evaporation from the surface of the CRM layer is allowed for some hours or days, until the upper
98 layer is constructed.

99 After the 28 curing days, one test specimen with diameter of 100 mm and height of 130 mm was
100 cored and cut from the inner part of each gyratory sample. The bulk density of the cored specimens
101 was obtained with the hydrostatic method [38] and then the air void content was calculated according
102 to EN 12697-8 [39]. The average (standard deviation) value of air void content was 12.7 % (0.6 %)
103 for CRM1 and 12.6 % (0.6 %) for CRM2.

104 The AC mixtures were produced in an asphalt plant, reheated and compacted in the laboratory using
105 a gyratory compactor [33]. The compacted samples had diameter of 150 mm, height of 170 mm and
106 target air void content of 5.0 % for the inner portion of the sample. Afterwards, four “small” test
107 specimens with diameter of 38 mm and height of 110 mm were cored and cut from each gyratory
108 sample, in accordance with AASHTO PP 99 [40]. The average (standard deviation) value of air void
109 content was 5.3 % (0.4 %) for AC1 test specimens and 5.2 % (0.1 %) for AC2 test specimens.

110 It is worth underlining that, since this was one of the first experiences ever concerning axial fatigue
111 testing of CRM mixtures, the adoption of the small geometry (38 mm diameter, 110 mm height) was

112 deemed premature by the Authors. Therefore, the large specimen geometry suggested by AASHTO
113 T 400 (100 mm diameter, 130 mm height) was considered for the CRM mixtures as a first step.

114

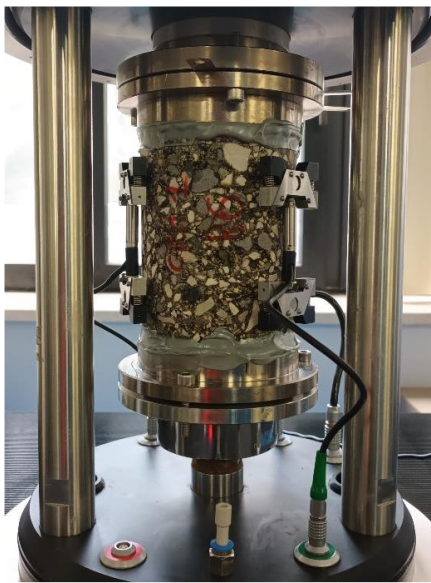
115 2.3 Complex modulus and cyclic fatigue testing

116 The testing procedure followed for the CRM mixtures is standardized by AASHTO T 400 [41] for
117 conventional AC mixtures to obtain the damage characteristic curve within the VECD theoretical-
118 experimental approach. This procedure includes cyclic tension-compression stiffness tests and cyclic
119 tension fatigue tests carried out with the Asphalt Mixture Performance Tester (AMPT), using the setup
120 shown in Figure 2a. Loading platens are glued to the top and bottom of the specimens with an epoxy
121 adhesive. Three axial LVDTs are mounted approximately 120° apart in order to measure the axial
122 strain in the central 70 mm of the specimen. The fatigue tests are performed in constant crosshead
123 mode. Compared to strain-controlled tests, crosshead-controlled tests are easier to run and reduce the
124 risk of damaging the equipment if improperly performed [42]. As an example, Figure 2b shows the
125 typical stress and strain signals at the beginning of the test for an AC mixture (the actuator strain is
126 obtained as the ratio between the actuator displacement and the specimen height). The applied
127 sinusoidal axial load is adjusted to keep the actuator displacement amplitude constant throughout the
128 test. Even though the on-specimen strain remains tensile, both tensile and compressive stresses are
129 applied on the specimen due to viscous effects. The actual on-specimen strain is lower than the
130 actuator strain level due to inevitable machine compliance issues. The test is stopped when the
131 machine is no longer able to apply a well-shaped sinusoidal load.

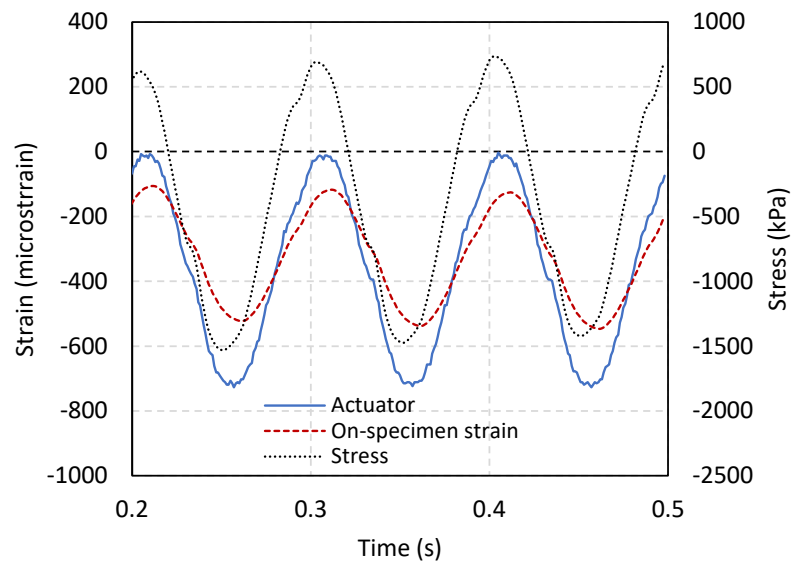
132 On CRM specimens, the complex modulus test (also known as fingerprint test) was performed at 20
133 °C and 10 Hz to evaluate the linear viscoelastic properties of each specimen. The test consisted in
134 applying 55 cycles of a sinusoidal tension-compression axial load adjusted to achieve a target peak-
135 to-peak on-specimen strain amplitude between 25 and 35 microstrain, which is a typical strain value
136 to observe a linear behaviour [43][44]. After a rest period of 5 minutes, the cyclic fatigue test was

137 performed at the same temperature and frequency. The initial peak-to-peak on-specimen tensile strain
 138 amplitude ($\epsilon_{0,initial}$) was selected between 70 and 80 microstrain, which led to test durations between
 139 2000 and 60000 cycles.

140 For the AC mixtures the testing temperature and frequency were 21 °C and 10 Hz. The target strain
 141 amplitude was between 50 and 75 microstrain in the fingerprint test, and $\epsilon_{0,initial}$ was between 380 and
 142 450 microstrain in the fatigue test, which led to test durations between 2000 and 80000 cycles [33].



(a)



(b)

Figure 2. Testing: (a) setup for complex modulus and cyclic fatigue tests, (b) stress and strain at the beginning of the fatigue test (in the figure, tension is negative while compression is positive)

2.4 Examined fatigue failure criteria

148 Fatigue failure criteria that have been developed for AC mixtures can be grouped into two main
 149 categories: empirical and energy-based [45][46][47][48].

150 The most common empirical criterion consists in arbitrarily defining the specimen failure based on
 151 the 50 % reduction of the initial stiffness modulus [49][50]. Another common empirical criterion is
 152 based on the observation of the phase angle evolution that typically shows an increase followed by a

153 sharp drop. It is assumed that the maximum phase angle corresponds to the formation of macrocracks,
154 and thus to the specimen failure [51].

155 Energy-based failure criteria rely on the calculation of the dissipated energy per unit volume per cycle
156 (W), i.e., the area of the stress-strain hysteresis loop, using the following linear approximation:

$$W = \pi \cdot \sigma \cdot \varepsilon \cdot \sin \delta = \pi \cdot \varepsilon^2 \cdot E \cdot \sin \delta \quad (1)$$

157 where σ is the stress amplitude, ε is the strain amplitude, E is the stiffness modulus and δ is the phase
158 angle at a given cycle.

159 Pronk and Hopman [52] introduced the dissipated energy ratio (DER) parameter to identify the fatigue
160 failure, based on the previous work by Van Dijk [53] and Van Dijk and Visser [54]. DER is defined
161 as the ratio between the total cumulated dissipated energy up to cycle n and the dissipated energy at
162 cycle n :

$$DER = \frac{\sum_{i=1}^n W_i}{W_n} \quad (2)$$

163 The relationship between DER and number of load cycles follows the line of equality (slope equal to
164 1) when the specimen is undamaged. As damage develops, the DER curve progressively bends
165 upwards (strain-controlled tests) or downwards (stress-controlled tests).

166 The criterion currently adopted by the reference standard AASHTO T 400 [41] is the so-called stress
167 degradation ratio criterion, which is a simplification of the DER criterion. Fatigue failure is identified
168 by the peak value of the product of stress amplitude and cycle number ($\sigma \cdot N$). The main advantage of
169 this criterion is that phase angle measurement is not needed.

170 The abovementioned criteria, typically adopted for traditional AC mixtures, were applied to the
171 investigated CRM mixtures.

3. Results and analysis

3.1 Complex modulus results

Figure 3 summarizes the results of the complex modulus fingerprint tests in terms of stiffness modulus and phase angle. The average (standard deviation) values of the stiffness modulus were 4496 MPa (572 MPa) and 7050 MPa (453 MPa) for CRM1 and CRM2, respectively. Instead, the average (standard deviation) values of the phase angle were 9.1° (0.7°) and 6.9° (0.4°) for CRM1 and CRM2, respectively. Such differences are statistically significant and were expected due to the higher cement content of CRM2 with respect to CRM1 (2 % vs 1 %).

Figure 3 also summarizes the results observed for the AC mixtures. The average (standard deviation) values of the stiffness modulus were 6755 MPa (298 MPa) and 7671 MPa (484 MPa) for AC1 and AC2, respectively. Instead, the average (standard deviation) values of the phase angle were 21.9° (0.7°) and 21.8° (0.4°) for AC1 and AC2, respectively.

The main difference between the CRM and AC mixtures lies in the phase angle values, which were significantly higher for the AC mixtures. This expected difference denotes a more pronounced dissipation behaviour for AC mixtures with respect to the CRM mixtures (especially CRM2).

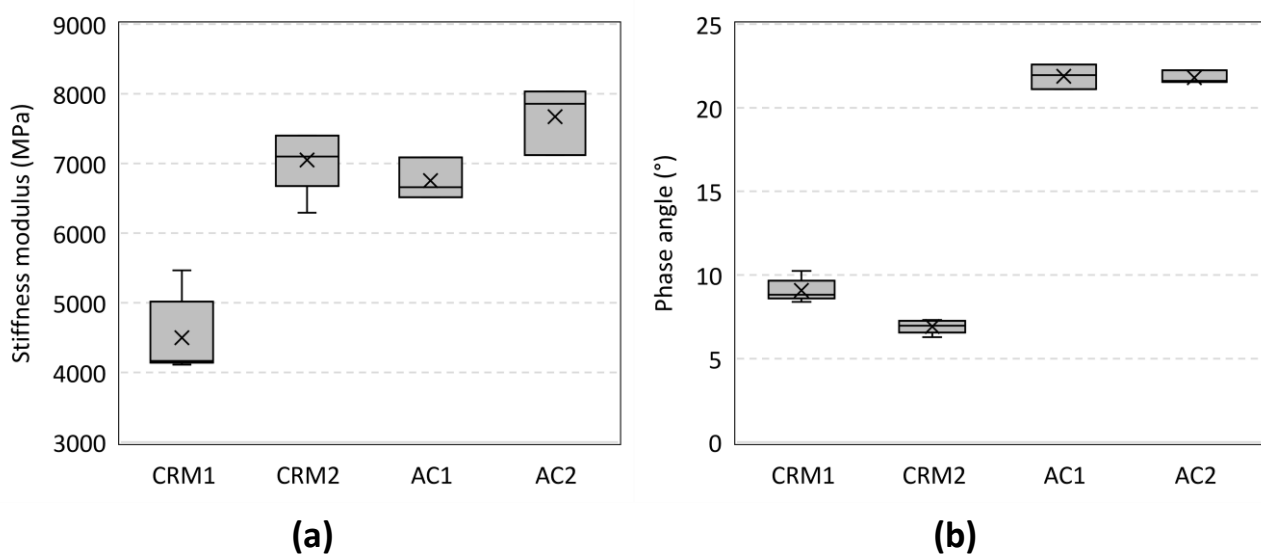


Figure 3. Complex modulus results: (a) stiffness modulus, (b) phase angle

190 3.2 Evolution of stress and strain during the fatigue test

191 Figure 4a shows the evolution of stress and on-specimen strain during the fatigue test for
 192 representative specimens of CRM1 (specimen R15, $\varepsilon_{0,initial} = 75$ microstrain) and CRM2 (specimen
 193 R1, $\varepsilon_{0,initial} = 80$ microstrain). For comparison purposes, Figure 4c shows the same data for
 194 representative specimens of AC1 (specimen #3, $\varepsilon_{0,initial} = 380$ microstrain) and AC2 (specimen #3,
 195 $\varepsilon_{0,initial} = 450$ microstrain). In these figures, both stress and strain are normalised with respect to their
 196 initial value. In addition, Figure 4b and Figure 4d show the evolution of the mode factor (MF) defined
 197 by Monismith and Deacon [55]:

$$MF = \frac{|A| - |B|}{|A| + |B|} \quad (3)$$

198 where $|A|$ and $|B|$ are the percentage variation in stress and strain, respectively, for an arbitrary but
 199 fixed reduction in mixture stiffness. MF is equal to -1 for purely stress-controlled tests and $+1$ for
 200 purely strain-controlled tests.

201 Figure 4a shows the different behaviour of mixtures CRM1 and CRM2. All CRM1 specimens (plus
 202 one CRM2 specimen) exhibited a progressive stress decrease and strain increase until reaching a sub-
 203 horizontal asymptote. Instead, for most CRM2 specimens (4 out of 5), both stress and strain followed
 204 a S-shape evolution during the test. For the AC mixtures (Figure 4c), the stress reduced rapidly while
 205 the strain increased rapidly in the very first phase of the test, then the stress decreased while the strain
 206 increased in a steady quasi-linear manner in the second phase, and finally the stress rapidly decreased
 207 and the strain rapidly increased in the third phase.

208 Figure 4a and Figure 4c confirm that the test is neither in stress control mode (constant stress) nor in
 209 strain control mode (constant strain). For the selected representative specimens, the MF values
 210 oscillated between -0.7 and -1 for the CRM mixtures, and between 0 and -0.5 for the AC mixtures.

211 In fact, for the CRM mixtures, the strain variation was predominant over the stress variation and the
 212 test was almost in stress control mode, especially for CRM2 specimens with higher cement content
 213 ($MF \approx -1$). For the AC mixtures, the test can be considered in mixed mode of loading, even though
 214 the strain variation was still predominant over the stress variation ($MF < 0$).

215 It can be concluded that the test was more severe for CRM mixtures than for conventional AC
 216 mixtures. Moreover, the common fatigue failure criteria that are employed in the case of constant
 217 stress or constant strain may not be applicable, especially for CRM mixtures.

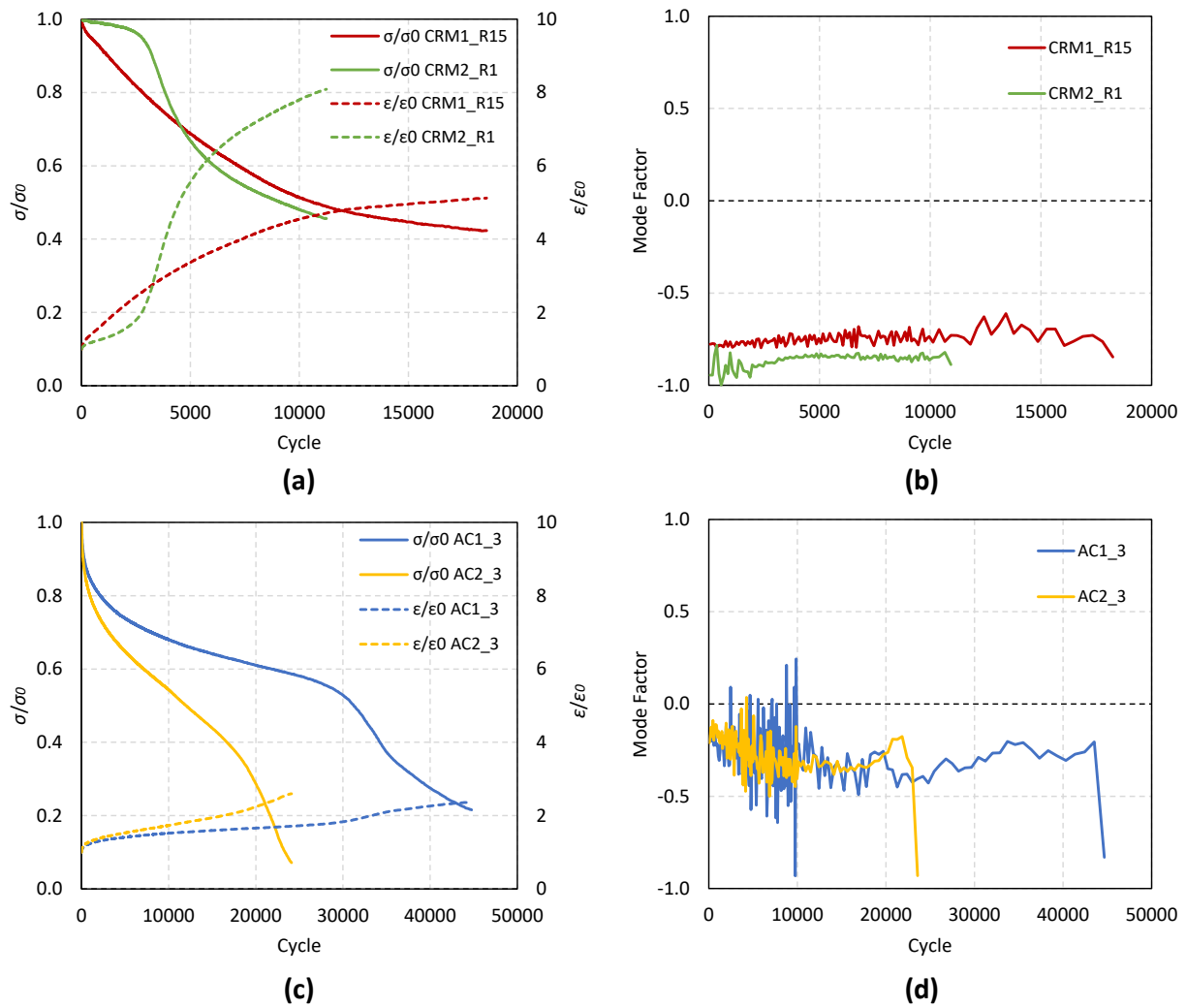


Figure 4. Evolution of: (a) stress and strain and (b) mode factor for CRM1 and CRM2; (c) stress and strain and (d) mode factor for AC1 and AC2

3.3 Empirical fatigue failure criteria

Figure 5 shows the evolution of stiffness modulus and phase angle (both normalised with respect to the initial value) during the fatigue test for the same four representative specimens shown above.

For the AC mixtures (Figure 5b), the three typical phases can be identified [48][56]. In the initial loading cycles (adaptation phase) the stiffness reduces rapidly while the phase angle increases rapidly due to the combined effect of fatigue damage, heat development and thixotropy. In the second phase (quasi-stationary phase) the stiffness keeps decreasing while the phase angle keeps increasing, both with a steady quasi-linear trend. This behaviour is normally associated with the development of damage due to the formation of microcracks. This second phase ends with an inflection point that denotes the beginning of the transition towards the third phase (failure phase), which is characterised by a fast decrease in stiffness and phase angle and is associated with the formation and propagation of macrocracks leading to the specimen physical failure.

The evolution of stiffness modulus and phase angle was similar between CRM1 and CRM2 mixtures, but different from the one described above (Figure 5a). Specifically: a) in both the stiffness and phase angle curves the quasi-stationary phase was not present; b) the phase angle evolution showed a sharper maximum value (the maximum δ/δ_0 value was around 1.5 for the AC specimens, higher than 2.0 for the CRM2 specimens and intermediate for the CRM1 specimens); c) the stiffness modulus curves were characterized by a relatively long and almost flat final part (without the inflection point that typically denotes the transition between the second and third phases for AC mixtures). This behaviour suggests different fatigue damage mechanisms for CRM mixtures, as compared to traditional AC mixtures.

Figure 5 also shows the fatigue failure points identified using the two most common empirical criteria: 50 % reduction in the stiffness modulus ($N_{f,E}$) and maximum phase angle ($N_{f,\delta}$). Table 1 summarizes the values of $N_{f,E}$ and $N_{f,\delta}$, along with the ratio $N_{f,\delta} / N_{f,E}$ and the normalised value of the stiffness modulus at the number of cycles $N_{f,\delta}$.

247 For all specimens, $N_{f,\delta}$ is higher than $N_{f,E}$. However, the $N_{f,\delta} / N_{f,E}$ ratio is generally lower for CRM
 248 mixtures (especially CRM2) as compared to AC mixtures, indicating that $N_{f,\delta}$ is closer to $N_{f,E}$ for CRM
 249 mixtures. Nevertheless, it should be recalled that CRM and AC specimens were tested at significantly
 250 different strain levels (see the values of $\varepsilon_{0,initial}$ in Table 1). An interesting common feature between
 251 CRM and AC mixtures is that the maximum phase angle broadly occurs when the stiffness modulus
 252 is approximately 20 % of the initial value E_0 , as denoted by the values of $E/E_0 @ N_{f,\delta}$ in Table 1.

253 The $N_{f,E}$ and $N_{f,\delta}$ values are plotted in Figure 6. In particular, the data related to the two ACs are plotted
 254 together as a single data set, because AC1 and AC2 exhibited the same macroscopic behaviour. Figure
 255 6 clearly highlights that the maximum phase angle criterion leads to higher N_f values with respect to
 256 the 50 % modulus reduction criterion. The parameters of the fitting lines in Figure 6 ($\log N_{f,E} =$
 257 $a \log N_{f,\delta} + b$) were determined using the total least square (TLS) method, and the correlation
 258 between $N_{f,E}$ and $N_{f,\delta}$ was assessed through the Pearson coefficient ρ . The values of the parameters a
 259 and b summarized in Table 2 indicate that the slope of the fitting function is somewhat similar for
 260 CRM1 and AC, whereas it is considerably different for CRM2 with higher cement content. Moreover,
 261 the Pearson coefficients denote a good correlation between $N_{f,E}$ and $N_{f,\delta}$ for CRM2 and AC ($\rho > 0.70$)
 262 and a moderate correlation for CRM1 ($\rho = 0.61$).

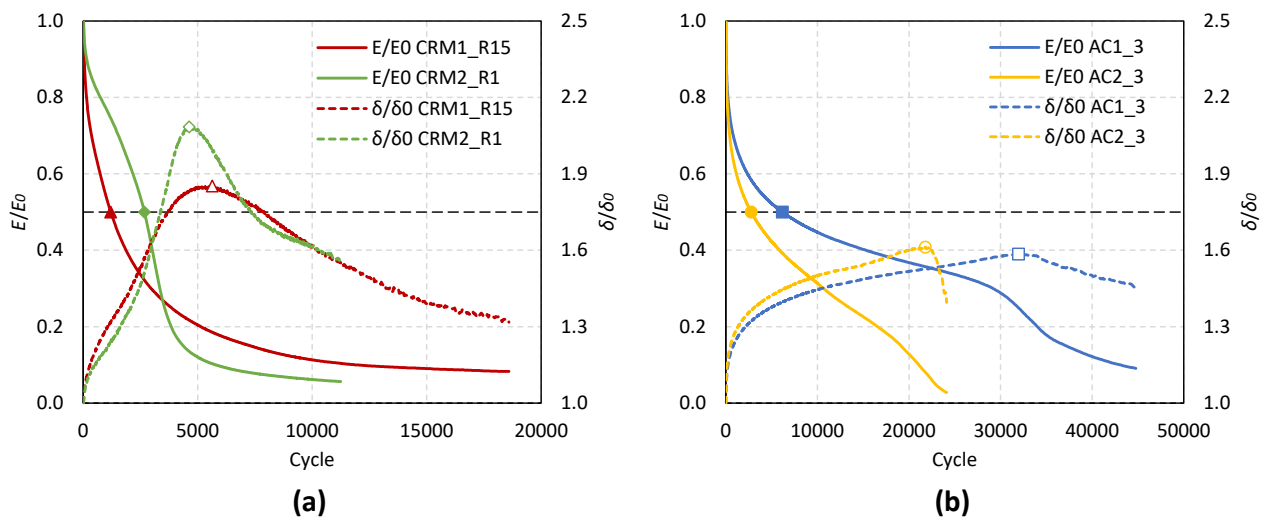


Figure 5. Evolution of stiffness modulus and phase angle for (a) CRM1 and CRM2, (b) AC1 and AC2

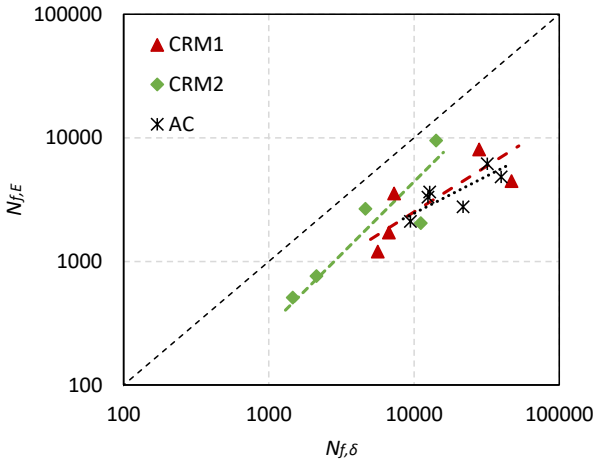
265

266

Table 1. Number of cycles to failure determined according to the empirical failure criteria

Mixture	Specimen	$\varepsilon_{0,initial}$ (microstrain)	$N_{f,E}$	$N_{f,\delta}$	$N_{f,\delta} / N_{f,E}$	$E/E_0 @ N_{f,\delta}$
CRM1	R5	80	3550	7280	2.1	0.34
	R14	70	4460	46900	10.5	0.12
	R15	75	1200	5630	4.7	0.19
	R17	75	1710	6720	3.9	0.24
	R18	70	8040	28040	3.5	0.27
	Average				3.7	0.23
CRM2	R1	80	2670	4630	1.7	0.14
	R5	80	760	2130	2.8	0.18
	R9	75	510	1460	2.9	0.14
	R10	75	2040	11140	5.5	0.18
	R11	75	9500	14170	1.5	0.17
	Average				2.3	0.16
AC1	1	400	3640	12790	3.5	0.23
	2	430	2110	9420	4.5	0.08
	3	380	6170	31950	5.2	0.25
	Average				4.3	0.19
AC2	1	400	4830	39710	8.2	0.27
	2	430	3310	12470	3.8	0.17
	3	450	2760	21770	7.9	0.08
	Average				5.8	0.17

267



268

269

Figure 6. $N_{f,E}$ vs $N_{f,\delta}$

270

Table 2. Fitting line parameters and Pearson coefficient for the data sets in Figure 6

Mixture	Slope (a)	Intercept (b)	Correlation (ρ)
CRM1	0.74	0.43	0.61
CRM2	1.17	-1.05	0.82
AC	0.60	0.98	0.77

3.4 Energy-based fatigue failure criteria

Figure 7 shows the evolution of the stress degradation ratio parameter ($\sigma \cdot N$) for the same four representative specimens shown above. The fatigue failure points corresponding to the maximum $\sigma \cdot N$ value ($N_{f,\sigma \cdot N}$) and to the maximum phase angle ($N_{f,\delta}$) are also highlighted in the figure. Note that, in the two subfigures, the scale on the y-axis is different (the AC specimens showed significantly higher values).

The AC specimens showed the expected behaviour, i.e., the parameter $\sigma \cdot N$ increased during the test until reaching its maximum value and then dropped rapidly before the specimen collapse. It is also worth noting that $N_{f,\sigma \cdot N}$ slightly precedes $N_{f,\delta}$, in agreement with the literature [57]. Conversely, for the CRM specimens, the parameter $\sigma \cdot N$ steadily increased until the specimen collapse, confirming the different fatigue damage mechanisms with respect to AC mixtures. More in detail, the parameter $\sigma \cdot N$ increased at a higher rate in the first part of the test, and at a slower rate in the second part of the test, suggesting that the physical mechanism leading to energy dissipation changed as damage increased during the test. The absence of a peak value in the $\sigma \cdot N$ curve was expected because the test is almost in pure stress control mode for the CRM mixtures, as shown in Figure 4b ($\sigma \cdot N = f(N)$ is a line with slope equal to σ for a purely stress-controlled test). $N_{f,\delta}$ broadly corresponded to the beginning of the second phase, characterized by a slower increase of the parameter $\sigma \cdot N$.

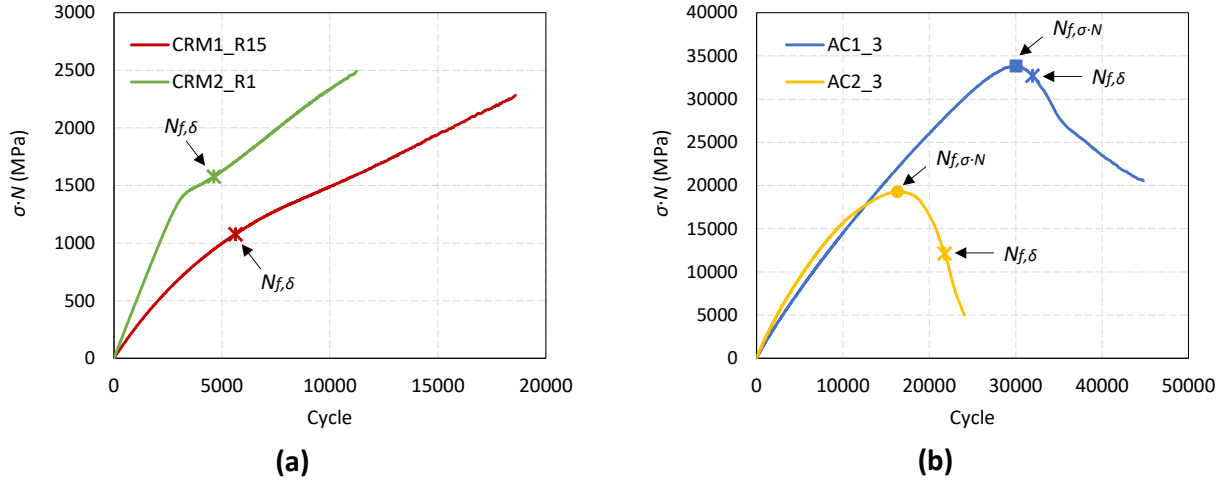


Figure 7. Evolution of the parameter $\sigma \cdot N$ for (a) CRM1 and CRM2, (b) AC1 and AC2

Since the point of maximum for $\sigma \cdot N$ cannot be used to define fatigue failure, it is necessary to take a step back and examine first the evolution of the dissipated energy per unit volume per cycle (Equation 1) during the test.

Figure 8 shows the evolution of W for the same four representative specimens shown above. It should be noted that W was one order of magnitude higher for the AC mixtures, which was expected, given the higher applied strain level and phase angle with respect to CRM mixtures (Figure 5, Table 1). The fatigue failure point corresponding to the maximum phase angle ($N_{f,\delta}$) is also highlighted in the figure.

For AC specimens, the dissipated energy increased rapidly in the very first loading cycles, then remained almost constant in the central part of the test, before dropping very quickly in the final part (Figure 8b). The three typical phases that characterize the evolution of modulus and phase angle (Figure 5b) can be easily recognised. Moreover, Figure 8b shows that $N_{f,\delta}$ corresponds to the end of the constant phase for specimen AC1_3, whereas it is located in the descending part of the curve for specimen AC2_3.

Conversely, for CRM specimens, the dissipated energy increased in the first part of the test until reaching a maximum, and then decreased at a slower rate compared to the first part until the end of the test (Figure 8a). This behaviour is more evident for CRM2 with respect to CRM1. As highlighted

above, the quasi-stationary phase that characterizes damage evolution in AC mixtures is completely missing. On the other hand, such an evolution (increasing in the first part, decreasing in the second part) confirms that the energy dissipation mechanism changed during the test. It should be also noted that, for both CRM1 and CRM2 specimens, the maximum phase angle almost corresponded to the maximum value of W . In addition, the CRM2 curve is characterized by two evident inflection points, one before and one after the peak W value. In the case of CRM1, only the inflection point after the peak W value is immediately apparent.

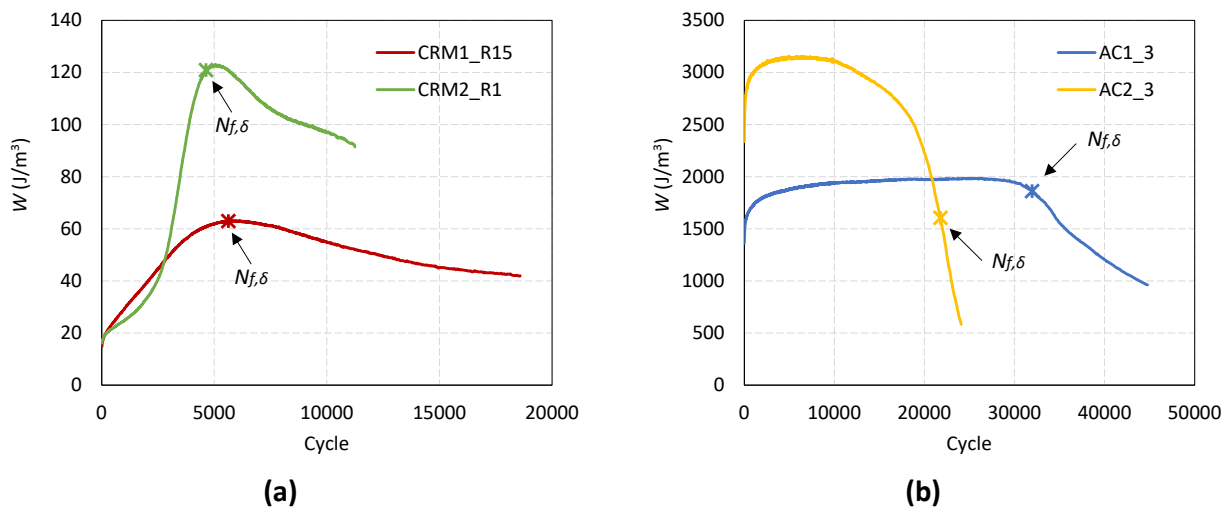


Figure 8. Evolution of the dissipated energy per unit volume per cycle for (a) CRM1 and CRM2, (b) AC1 and AC2

The differences in the dissipated energy per cycle led to a different evolution of the DER (Figure 9). For the CRM specimens, a zoom of the initial part of the test is presented in Figure 9a, as these are the data of greatest interest.

Figure 9b shows the typical DER evolution that characterizes AC mixtures in a strain-controlled test (MF indicates that the test is in mixed mode of loading, see Figure 4). As long as the specimen is undamaged, the DER curve is superimposed to the line of equality, then the curve progressively deviates, approaching an oblique asymptote (irrecoverable fatigue asymptote). One way to define the

number of cycles to failure based on the DER curve is to consider the intersection between the no damage line and the irrecoverable fatigue asymptote, as shown in Figure 9b.

Figure 9a shows that the behaviour of CRM mixtures was totally different. First, the DER values are located below the line of equality from the very early testing cycles. This behaviour typically characterizes damage in stress-controlled tests (the MF is indeed close to -1 , see Figure 4). Second, the DER evolution of CRM2 specimens showed a local maximum, an inflection point (highlighted in Figure 9a), and a local minimum within a relatively short interval of cycles. After the local minimum, the DER value increased again at a rather constant rate until the specimen failure (not shown in the plot). For CRM1, such a behaviour was less pronounced, but an inflection point is present also in this case (as highlighted in Figure 9a). A possible interpretation of the fatigue failure mechanism of CRM mixtures is proposed in the next section.

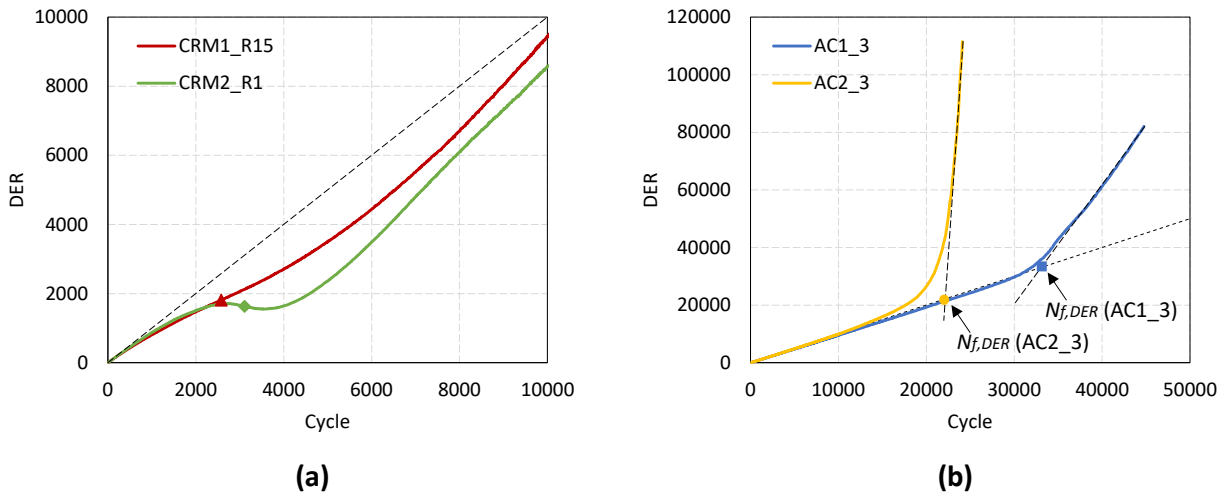


Figure 9. Evolution of DER for (a) CRM1 and CRM2, (b) AC1 and AC2

4. Discussion

4.1 Interpretation of the composite fatigue failure of CRM specimens

The experimental results clearly showed that the fatigue damage evolution of CRM and AC specimens was different. It is readily apparent that such a difference was due to the presence of

345 cementitious bonds, and the different behaviour between CRM1 and CRM2 mixtures also confirms
346 that the cement dosage played a critical role. Consequently, a different fatigue failure criterion,
347 specifically devoted to identifying the composite effect of cementitious and bituminous bonds is
348 necessary.

349 A possible interpretation of the fatigue failure of CRM specimens is outlined in Figure 10. At the
350 beginning of the fatigue test, the cementitious bonds carried most of the applied tensile load due to
351 their higher stiffness with respect to the bituminous bonds. However, they are also more brittle than
352 the bituminous bonds and thus started failing as the tensile strain amplitude increased in the first stage
353 of the test (Figure 4 and Figure 8). We suggest that the local maximum, the inflection point, and the
354 local minimum that characterize the initial DER evolution for CRM2 specimens (Figure 9a) were due
355 to the failure of the cementitious bonds.

356 The local failure of the cementitious bonds can be interpreted as microcracks that reduce the effective
357 area of the specimen. Those microcracks could originate from the breaking of the cement hydrates or
358 from a detachment at the interface between the hydrates and the aggregate particles, mostly composed
359 of RA particles. Failure of the cementitious bonds started at a relatively low number of loading cycles
360 and extended through a narrow interval of cycles. The process led to the dramatic reduction of
361 stiffness and increase in phase angle shown in Figure 5a, as the stress was progressively transferred
362 to the bituminous binder. This explains the observed dramatic increase of dissipated energy per cycle
363 (Equation 1, Figure 8a), which in turn causes the decrease of DER (Equation 2, Figure 9a). It is
364 important to note that, at this stage, the formation of macrocracks can be reasonably excluded because
365 they would lead to the specimen collapse within a few cycles. As the number of loading cycles further
366 increased, the bituminous bonds progressively carried a higher share of the load, and therefore they
367 were also affected by an increasing damage. We observe a decreasing trend of the dissipated energy
368 per cycle and the DER curve starts increasing again (slope greater than 1). Such a behaviour is similar

369 to that of conventional AC mixtures in strain-controlled tests and ultimately leads to the development
 370 of macrocracks, followed by the specimen collapse.

371 The damage evolution for CRM1 specimens was characterised by smoother transitions in the
 372 evolution of energy dissipation (Figures 8a and 9a), highlighting the lower impact of the cementitious
 373 bonds, which is clearly due to the lower cement dosage.

374 Overall, the evolutions of both W and DER suggest that for CRM mixtures there was a transition from
 375 a cement-dominated to a bitumen-dominated dissipation behaviour and that the fatigue failure was a
 376 composite phenomenon affected by both cementitious and bituminous bonds.

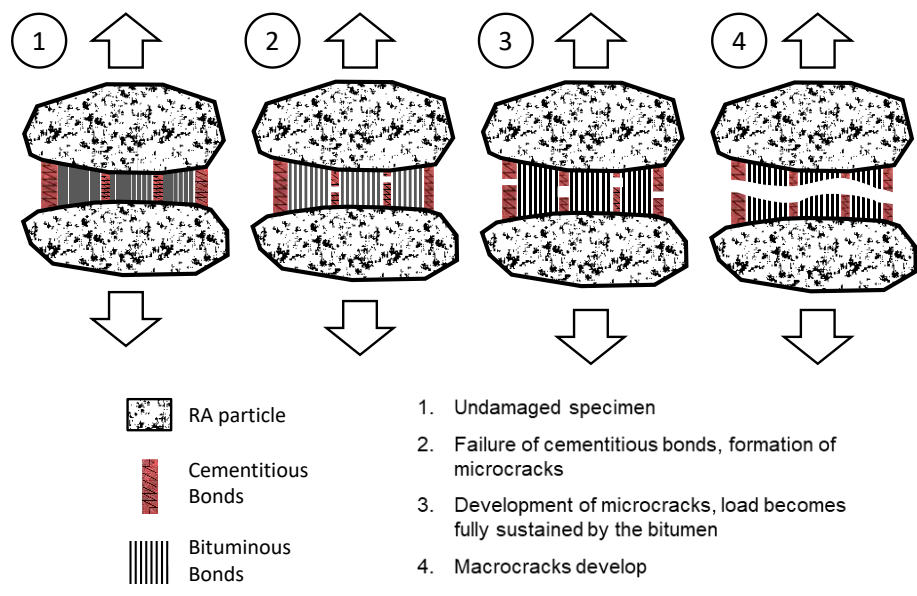


Figure 10. Interpretation of fatigue failure of CRM specimens

4.2 Fatigue failure criterion for CRM specimens

381 We suggest that, for CRM mixtures, the inflection point of the DER evolution curve (highlighted in
 382 Figure 9a) can be used to identify the number of cycles corresponding to the failure of the
 383 cementitious bonds. The inflection point can be calculated using several numerical procedures. In this
 384 research we applied the algorithm developed by Virgili et al. [58] to identify the failure point of
 385 reinforced double-layered asphalt specimens in cyclic four-point bending tests.

386 Table 3 reports the number of cycles to failure $N_{f,DER}$ corresponding to the inflection point of the DER
387 evolution curve for all CRM specimens. For AC specimens, failure was identified with the tangent
388 intersection method (Figure 9b). Figure 11 compares the $N_{f,DER}$ values with the number of cycles to
389 failure determined according to the 50 % modulus reduction criterion ($N_{f,E}$) and the maximum phase
390 angle criterion ($N_{f,\delta}$).

391 For all specimens, the $N_{f,DER} / N_{f,E}$ ratio was higher than one, and higher values were obtained for the
392 AC mixtures with respect to the CRM mixtures (Figure 11a). Once again, it is highlighted that the 50
393 % modulus reduction is an arbitrary failure definition without any direct physical interpretation.

394 For AC specimens, the $N_{f,DER} / N_{f,\delta}$ ratio is comprised between 1.0 and 1.56 (average value of 1.18,
395 standard deviation of 0.24). It has been reported by several Authors that for AC mixtures the DER
396 criterion and the maximum phase angle criterion are almost equivalent [47][59]. For CRM specimens,
397 the $N_{f,DER} / N_{f,\delta}$ ratio is comprised between 0.33 and 1.05 (average value of 0.67, standard deviation
398 of 0.23). These values suggest that the two criteria describe different failure mechanisms. Specifically,
399 $N_{f,DER}$ could identify the failure of the cementitious bonds, whereas $N_{f,\delta}$ could identify the failure of
400 the bituminous bonds, analogously to AC mixtures. The parameters of the fitting lines in Figure 11b
401 ($N_{f,DER}$ vs $N_{f,\delta}$) are shown in Table 4 and indicate that also in this case the fitting functions are
402 somewhat similar for CRM1 and AC (in particular, they are parallel with slope approximately equal
403 to 1), whereas the slope of the fitting line for CRM2 is considerably different. The Pearson
404 coefficients indicate a good correlation between $N_{f,DER}$ and $N_{f,\delta}$ for all mixtures ($\rho > 0.70$).

405 Finally, we remark that both the DER-based criterion (failure of cementitious bonds) and the
406 maximum phase angle criterion (failure of bituminous bonds) highlighted a longer fatigue life for
407 CRM1 with respect to CRM2. However, as long as field behaviour is concerned, typically CRM
408 mixtures produced with 1% Portland cement (or less) are not prone to fatigue because permanent
409 deformation accumulation is more severe. On the other hand, if Portland cement dosage is equal to
410 or greater than 2%, permanent deformation is normally not an issue [20]. It should also be noted that,

411 beyond the point of maximum phase angle, all CRM specimens were characterized by a relatively
 412 long life before collapse (Figure 5a). During this phase, stiffness is quite low (less than 20 % of the
 413 initial value), but phase angle is rather high and, overall, this led to values of dissipated energy per
 414 cycle that were higher than those measured in the undamaged specimens (Figure 8a). This aspect,
 415 that must be further investigated, may affect the field behaviour of CRM mixtures.

416

417 Table 3. Number of cycles to failure determined according to the proposed energy-based failure criterion and
 418 comparison with the empirical failure criteria

Mixture	Specimen	$N_{f,DER}$	$N_{f,DER} / N_{f,E}$	$N_{f,DER} / N_{f,\delta}$
CRM1	R5	5178	1.46	0.71
	R14	17466	3.92	0.37
	R15	2578	2.15	0.46
	R17	4290	2.51	0.64
	R18	29562	3.68	1.05
	<i>Average</i>		2.74	0.65
CRM2	R1	3108	1.16	0.67
	R5	1573	2.07	0.74
	R9	1246	2.44	0.85
	R10	3712	1.82	0.33
	R11	11776	1.24	0.83
	<i>Average</i>		1.75	0.68
AC1	1	20000	5.49	1.56
	2	9400	4.45	1.00
	3	32000	5.19	1.00
	<i>Average</i>		5.05	1.19
AC2	1	56000	11.59	1.41
	2	14000	4.23	1.12
	3	22000	7.97	1.01
	<i>Average</i>		7.93	1.18

419

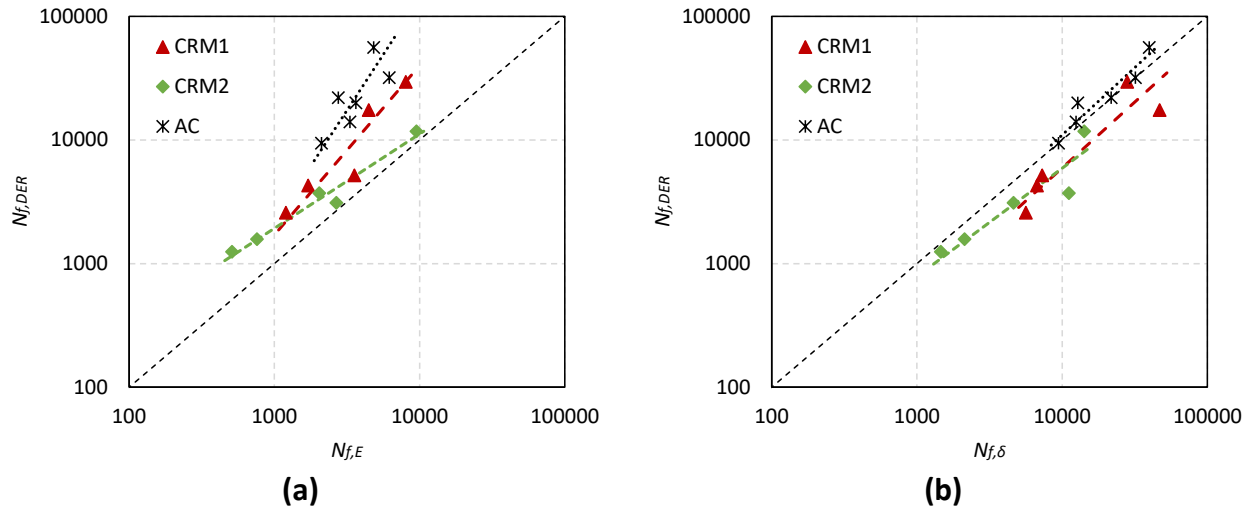


Figure 11. $N_{f,DER}$ vs (a) $N_{f,E}$, (b) $N_{f,\delta}$

Table 4. Fitting line parameters and Pearson coefficient for the data sets in Figure 11b

Mixture	Slope (a)	Intercept (b)	Correlation (ρ)
CRM1	1.07	-0.49	0.73
CRM2	0.88	0.27	0.86
AC	1.09	-0.32	0.95

5. Conclusions

The objective of this research was to provide new insights into the fatigue failure of CRM mixtures. To this aim, two CRM mixtures characterized by different dosages of Portland cement (1% and 2%), were subjected to uniaxial cyclic tension fatigue tests in control crosshead mode. Empirical and energy-based failure criteria typically adopted for AC mixtures were applied to analyse the results, and the main findings can be summarized as follows:

- The stress/strain evolution during the fatigue test highlighted that the test was almost in pure stress control mode for the CRM mixtures whereas it was in mixed mode for the AC mixtures. Hence the test was more severe for CRM mixtures.

- 434 • The stiffness modulus and phase angle evolution of CRM mixtures were characterized by: a) the
435 absence of the quasi-stationary phase; b) a sharper maximum value of the phase angle curve; c) a
436 relatively long and almost flat final part of the stiffness modulus curves.
- 437 • The energy dissipation evolution of CRM mixtures was characterised by: a) the absence of a peak
438 in the evolution of the parameter $\sigma \cdot N$; b) the rapid increase of the dissipated energy per cycle until
439 reaching a maximum, followed by a slower decrease until the end of the test; c) the DER curve
440 was below the equality line from the very early testing cycles and showed an inflection point.
- 441 Based on the experimental results, a new interpretation of fatigue failure of CRM mixtures is
442 proposed:
- 443 • At the beginning of the fatigue test, the CRM specimens showed a cement-dominated damage
444 behaviour, followed by the breaking of the cementitious bonds, which led to the transition towards
445 a bitumen-dominated damage behaviour. Afterwards, further damage of the bituminous bonds led
446 to the specimen collapse.
- 447 • The inflection point of the DER curve was proposed to identify the failure of the cementitious
448 bonds whereas, analogously to typical AC mixtures, the subsequent failure of the bituminous
449 bonds was identified through the maximum phase angle value. Based on both criteria, a longer
450 fatigue service life was observed for CRM specimen with lower cement content.

451 The findings of this research suggest that the fatigue failure of CRM mixtures during uniaxial
452 laboratory tests is a composite phenomenon affected by both cementitious and bituminous bonds.
453 However, it is still not clear how these mechanisms affect the field behaviour. Future work will also
454 explore the possibility of applying the viscoelastic continuum damage (VECD) theory to CRM
455 mixtures.

456

457 Funding

458 No funding was received for conducting this study.

459

460 Competing interests

461 The authors have no competing interests to declare that are relevant to the content of this article.

462

463 References

- 464 1. Wiesmeth, H., 2020. Implementing the circular economy for sustainable development. Elsevier.
465 ISBN 9780128217986, <https://doi.org/10.1016/C2019-0-04150-7>.
- 466 2. Cross, S., Chesner, W., Justus, H., Kearney, E., 2011. Life-cycle environmental analysis for
467 evaluation of pavement rehabilitation options. Transportation Research Record, 2227, pp. 43-52.
- 468 3. Giani, M.I., Dotelli, G., Brandini, N., Zampori, L., 2015. Comparative life cycle assessment of
469 asphalt pavements using reclaimed asphalt, warm mix technology and cold in-place recycling.
470 Resources, Conservation and Recycling, 104, pp. 224-238.
- 471 4. Thenoux, G., González, A., Dowling, R., 2007. Energy consumption comparison for different
472 asphalt pavements rehabilitation techniques used in Chile. Resources, Conservation and
473 Recycling, 49(4), pp. 325-339.
- 474 5. Thives, L.P., Ghisi, E., 2017. Asphalt mixtures emission and energy consumption: A review.
475 Renewable and Sustainable Energy Reviews, 72, pp. 473-484.
- 476 6. Dołżycki, B., Jaskuła, P., 2019. Review and evaluation of cold recycling with bitumen emulsion
477 and cement for rehabilitation of old pavements. Journal of Traffic and Transportation
478 Engineering (English Edition), 6(4), pp. 311-323.

- 479 7. Dolzycki, B., Jaczewski, M., Szydłowski, C., 2017. The long-term properties of mineral-
480 cement-emulsion mixtures. *Construction and Building Materials*, 156, pp. 799-808.
- 481 8. Godenzoni, C., Graziani, A., Bocci, E., Bocci, M., 2018. The evolution of the mechanical
482 behaviour of cold recycled mixtures stabilised with cement and bitumen: field and laboratory
483 study. *Road Materials and Pavement Design*, 19(4), pp. 856-877.
- 484 9. Guatimosim, F.V., Vasconcelos, K.L., Bernucci, L.L.B., Jenkins, K.J., 2018. Laboratory and
485 field evaluation of cold recycling mixture with foamed asphalt. *Road Materials and Pavement*
486 *Design*, 19(2), pp. 385-399.
- 487 10. Kuchiishi, A.K., Santos Antão, C.C.D., Vasconcelos, K., Bernucci, L.L.B., 2019. Influence of
488 viscoelastic properties of cold recycled asphalt mixtures on pavement response by means of
489 temperature instrumentation. *Road Materials and Pavement Design*, 20(sup2), pp. S710-S724.
- 490 11. Fedrigo, W., Núñez, W.P., Visser, A.T., 2020. A review of full-depth reclamation of pavements
491 with Portland cement: Brazil and abroad. *Construction and Building Materials*, 262, 120540.
- 492 12. Fedrigo, W., Núñez, W.P., Schreinert, G.G., Kleinert, T.R., Matuella, M.F., Castañeda López,
493 M.A., Ceratti, J.A.P., 2021. Flexural strength, stiffness and fatigue of cement-treated mixtures of
494 reclaimed asphalt pavement and lateritic soil. *Road Materials and Pavement Design*, 22(5), pp.
495 1004-1022.
- 496 13. SABITA, 2020. Technical guideline: Bitumen stabilised materials. A Guideline for the Design
497 and Construction of Bitumen Emulsion and Foamed Bitumen Stabilised Materials.
- 498 14. Orosa, P., Pérez, I., Pasandín, A.R., 2022. Evaluation of the shear and permanent deformation
499 properties of cold in-place recycled mixtures with bitumen emulsion using triaxial tests.
500 *Construction and Building Materials*, 328, 127054.
- 501 15. Bocci, M., Grilli, A., Cardone, F., Graziani, A., 2011. A study on the mechanical behaviour of
502 cement-bitumen treated materials. *Construction and Building Materials*, 25(2), pp. 773–778.
- 503 16. Buczyński, P., Iwański, M., 2017. Fatigue Life Comparison of Recycled Cold Mixes with
504 Foamed Bitumen and with Bitumen Emulsion. *Procedia Engineering*, 172, pp. 135-142.

- 505 17. Dolzycki, B., Szydlowski, C., Jaczewski, M., 2020. The influence of combination of binding
506 agents on fatigue properties of deep cold in-place recycled mixtures in Indirect Tensile Fatigue
507 Test (ITFT). *Construction and Building Materials*, 239, 117825.
- 508 18. Kavussi, A., Modarres, A., 2010. Laboratory fatigue models for recycled mixes with bitumen
509 emulsion and cement. *Construction and Building Materials*, 24(10), pp. 1920–1927.
- 510 19. Leandri, P., Losa, M., Di Natale, A., 2015. Field validation of recycled cold mixes viscoelastic
511 properties. *Construction and Building Materials*, 75, pp. 275–282.
- 512 20. Stimilli, A., Ferrotti, G., Graziani, A., Canestrari, F., 2013. Performance evaluation of a cold-
513 recycled mixture containing high percentage of reclaimed asphalt. *Road Materials and*
514 *Pavement Design*, 14(SUPPL.1), pp. 149–161.
- 515 21. Chehelgo, K., Gariy, Z.C.A., Shitote, S.M., 2019. Modeling of fatigue-strength development in
516 cold-emulsion asphalt mixtures using maturity method. *Applied Sciences*, 9(13), 2694.
- 517 22. Ebels, L.-J., 2008. Characterisation of Material Properties and Behaviour of Cold Bituminous
518 Mixtures for Road Pavements. PhD Dissertation, Stellenbosch University, South Africa.
- 519 23. Huang, W., Cao, M., Xiao, L., Li, J., Zhu, M., 2023. Experimental study on the fatigue
520 performance of emulsified asphalt cold recycled mixtures. *Construction and Building Materials*,
521 369, 130607.
- 522 24. Di Benedetto, H., Perraton, D., Lamothe, S., Boussabnia, M.M., 2023. Rational relationship
523 between the fatigue curves of asphalt mixes obtained from tension/compression and 4-point
524 bending tests. *Road Materials and Pavement Design*, 24(sup1), pp. 192-208.
- 525 25. Di Benedetto, H., Partl, M.N., Francken, L., De La Roche Saint André, C., 2001. Stiffness
526 testing for bituminous mixtures. *Materials and Structures*, 34(2), pp. 66-70.
- 527 26. Nemati, R., Dave, E.V., Sias, J.E., Thibodeau, E.S., Worsman, R.K., 2019. Evaluation of
528 Laboratory Performance and Structural Contribution of Cold Recycled Versus Hot Mixed
529 Intermediate and Base Course Asphalt Layers in New Hampshire. *Transportation Research*
530 *Record*, 2673(6), pp. 467-476.

- 531 27. Tavassoti, P., Solaimanian, M., Chen, X., 2022. Characterization of fatigue performance of cold
532 mix recycled asphalt mixtures through uniaxial tension-compression testing. *Construction and*
533 *Building Materials*, 329, 127155.
- 534 28. EN 13043, 2002. Aggregates for bituminous mixtures and surface treatments for roads, airfields
535 and other trafficked areas.
- 536 29. EN 13808, 2013. Bitumen and bituminous binders – Framework for specifying cationic
537 bituminous emulsions.
- 538 30. EN 197-1, 2011. Cements – Part 1: Composition, specifications and conformity criteria for
539 common cements.
- 540 31. Winter, M., Mollenhauer, K., Graziani, A., Mignini, C., Giancontieri, G., Lo Presti, D.,
541 Bjurström, H., Kalman, B., Hornyk, P., Gaudefroy, V., 2020. Design of flexible pavements with
542 cold recycled asphalt bases: Comparison of five national approaches. In: *Proceedings of the 8th*
543 *Transport Research Arena TRA 2020*.
- 544 32. Mignini, C., Cardone, F., Graziani, A., 2022. Complex modulus of cement-bitumen treated
545 materials produced with different reclaimed asphalt gradations. *Materials and Structures*, 55(7),
546 169.
- 547 33. Spadoni, S., Ingrassia, L.P., Jaskuła, P., Canestrari, F., 2023. Advanced fatigue and rutting
548 characterisation of Polish asphalt mixtures based on the VECD model and viscoplastic shift
549 model. *Road Materials and Pavement Design*, 24(S1), pp. 145-159.
- 550 34. Graziani, A., Raschia, S., Mignini, C., Carter, A., Perraton, D., 2020. Use of fine aggregate
551 matrix to analyze the rheological behavior of cold recycled materials. *Materials and Structures*,
552 53(4), 72.
- 553 35. EN 12697-31, 2019. Bituminous mixtures – Test methods – Part 31: Specimen preparation by
554 gyratory compactor.

- 555 36. Grilli, A., Graziani, A., Bocci, E., Bocci, M., 2016. Volumetric properties and influence of water
556 content on the compactability of cold recycled mixtures. *Materials and Structures*, 49, pp. 4349-
557 4362.
- 558 37. Cardone, F., Grilli, A., Bocci, M., Graziani, A., 2014. Curing and temperature sensitivity of
559 cement-bitumen treated materials, *International Journal of Pavement Engineering*, 16(10), pp.
560 868-880.
- 561 38. EN 12697-6, 2020. Bituminous mixtures – Test methods – Part 6: Determination of bulk density
562 of bituminous specimens.
- 563 39. EN 12697-8, 2018. Bituminous mixtures – Test methods – Part 8: Determination of void
564 characteristics of bituminous specimens.
- 565 40. AASHTO PP 99, 2019. Standard Practice for Preparation of Small Cylindrical Performance Test
566 Specimens Using the Superpave Gyratory Compactor (SGC) or Field Cores.
- 567 41. AASHTO T 400, 2023. Standard method of test for determining the damage characteristic
568 curve and failure criterion using the Asphalt Mixture Performance Tester (AMPT) cyclic fatigue
569 test.
- 570 42. Underwood, B.S., Kim, Y.R., Guddati, M.N., 2010. Improved calculation method of damage
571 parameter in viscoelastic continuum damage model. *International Journal of Pavement*
572 *Engineering*, 11(6), pp. 459–476.
- 573 43. Jaczewski, M., Szydlowski, C., Dolzycki, B., 2022. Preliminary study of linear viscoelasticity
574 limits of cold recycled mixtures determined in Simple Performance Tester (SPT). *Construction*
575 *and Building Materials*, 357, 129432.
- 576 44. Jaczewski, M., Szydlowski, C., Dolzycki, B., 2023. Stiffness of cold-recycled mixtures under
577 variable deformation conditions in the IT-CY test. *Case Studies in Construction Materials*, 18,
578 e02066.

- 579 45. Bhasin, A., Castelo Branco, V.F., Masad, E., Little, D.N., 2009. Quantitative comparison of
580 energy methods to characterize fatigue in asphalt materials. *Journal of Materials in Civil*
581 *Engineering*, 21(2), pp. 83–92.
- 582 46. Gajewski, M., Bańkowski, W., Pronk, A.C., 2020. Evaluation of fatigue life of high modulus
583 asphalt concrete with use of three different definitions. *International Journal of Pavement*
584 *Engineering*, 21(14), pp. 1717-1728.
- 585 47. Shen, S., Lu, X., 2011. Energy based laboratory fatigue failure criteria asphalt materials. *Journal*
586 *of Testing and Evaluation*, 39(3), 103088.
- 587 48. Sudarsanan, N., Kim, Y.R., 2022. A critical review of the fatigue life prediction of asphalt
588 mixtures and pavements. *Journal of Traffic and Transportation Engineering (English Edition)*,
589 9(5), pp. 808-835.
- 590 49. AASHTO T 321, 2017. Standard method of test for determining the fatigue life of compacted
591 asphalt mixtures subjected to repeated flexural bending.
- 592 50. EN 12697-24, 2018. Bituminous mixtures – Test methods – Part 24: Resistance to fatigue.
- 593 51. Reese, R., 1997. Properties of aged asphalt binder related to asphalt concrete fatigue life.
594 *Journal of the Association of Asphalt Paving Technologists*, 66, pp. 604-632.
- 595 52. Pronk, A.C. and Hopman, P.C., 1991. Energy dissipation: the leading factor of fatigue. In:
596 *Highway Research: Sharing the Benefits*. Thomas Telford Publishing, London, pp. 255-267.
- 597 53. Van Dijk, W., 1975. Practical Fatigue Characterization of Bituminous Mixes. *Proceedings of the*
598 *Association of Asphalt Paving Technologists (AAPT)*, 44, pp. 38–74.
- 599 54. Van Dijk, W., Visser, W., 1977. The Energy Approach to Fatigue for Pavement Design.
600 *Proceedings of the Association of Asphalt Paving Technologists (AAPT)*, 46, pp. 1–40.
- 601 55. Monismith, C.L., Deacon, J.A., 1969. Fatigue of asphalt paving mixtures. *Transportation*
602 *Engineering Journal of ASCE*, 95(2), pp. 317-346.
- 603 56. Di Benedetto, H., De La Roche, C., Baaj, H., Pronk, A., Lundström, R., 2004. Fatigue of
604 bituminous mixtures. *Materials and Structures*, 37(267), pp. 202-216.

- 605 57. Lee, K.C., 2020. Improvement in dynamic modulus and cyclic fatigue testing of asphalt
606 mixture. PhD Thesis, North Carolina State University.
- 607 58. Virgili, A., Canestrari, F., Grilli, A., Santagata, F.A., 2009. Repeated load test on bituminous
608 systems reinforced by geosynthetics. *Geotextiles and Geomembranes*, 27(3), pp. 187-195.
- 609 59. Tapsoba, N., Sauzéat, C., Di Benedetto, H., 2013. Analysis of fatigue test for bituminous
610 mixtures. *Journal of Materials in Civil Engineering*, 25(6), pp. 701-710.