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(Article begins on next page)

Spatial conflict simulator using game engine technology and Bayesian networks for workspace management

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Abstract

Workspace demand changes across space and time, stressing the need to consider space as a limited and renewable resource. Traditional scheduling techniques have not fully handled this issue. This study proposes a workspace management framework using a game engine to address that. The simulator detects spatial interferences by combining geometric computations and physics simulations. The detected conflicts are filtered through Bayesian inference to detect non-critical scenarios and avoid overestimation. The proposed spatial conflict simulator was tested using a real use case and compared to commercial tools. Results showed that the Navisworks approach detected 58 spatial conflicts (of which only 25% were relevant), the Synchro approach detected 1 spatial conflict, and the proposed approach detected 1 “direct” and 4 “indirect” spatial conflicts. Results show its capability to detect more relevant spatial issues than state-of-the-art tools and avoid overestimations. Construction management teams can adjust or confirm the schedule with that information.

Keywords

Construction Management; Workspace Scheduling; Spatial Conflicts; BIM; Game Engine; 4D Tool.

1. Introduction

In the Architecture, Engineering and Construction (AEC) industry, construction sites usually involve large numbers of workers, equipment, adjacent buildings, and facilities. They are also affected by different weather conditions and are very dynamic operating environments. Consequently, safety and constructability issues are usually contextual, as they depend on building and resource displacement, spatial-temporal dependencies, and ever-changing site conditions.

In such a dynamic environment, any activity requires a specific workspace to be executed [1], defined as the suitable space crews and/or equipment occupy during execution [2]. As the construction progresses, the space occupied by completed activities will be released and reused by other operations [3]. Consequently, the space required for construction operation continuously changes over time [4], leading to a sequence of workspaces associated with the project’s activities [5]. When the same workspace is occupied simultaneously by two or more activities, a spatial interference occurs, which might lead to significant problems such as construction delay, loss in productivity and labor safety hazards. As suggested by [6], this evidence demonstrates that space in the construction site must be considered as a limited but renewable resource, similar to workers, equipment, and materials [3]. Impacts due to spatial interferences have been measured qualitatively and quantitatively. To cite a few statistics, a study related to masonry works has reported that congested workspaces and restricted access cause efficiency losses of up to 65% [7]. In addition to the productivity impacts, another study conducted in the US private industry sector associated the death of 323 workers over 12 years with poor workspace planning [8].

43 However, automating the identification of workspaces is challenging for several reasons. The first one is that
44 operational workspaces are seldom limited to the volume surrounding the building components interested
45 in ongoing tasks (i.e., the so-called main workspace). Rather, they include additional volumes used for
46 ancillary tasks such as materials storage, passageways, etc. The second reason is that there might occur
47 indirect clashes even between non-overlapping workspaces, hence not detectable using mere geometric
48 intersection checks, because some actions occurring in one space could interfere indirectly with the activity
49 carried out in another detached space (e.g., struck-by hazard from falling objects, electrical hazard). Another
50 reason is that contextual variables often determine the actual occurrence of a risk and its severity. In these
51 cases, expert knowledge can contribute to refining and enhancing the assessment of detected spatial
52 interferences. In other words, two identical clashes detected at different points in time or occurring due to
53 different concurrent activities can result in remarkably different severity levels.

54 Furthermore, the dynamic nature of construction activities makes the management of workspaces
55 challenging using conventional planning methods. The authors in [9] assert that conventional planning
56 methods do not adequately represent and communicate interferences between construction activities and
57 do not consider space constraints in the planning process. They typically focus on the time and cost aspects
58 [9–12]. In fact, traditional construction scheduling techniques, such as Gantt charts and network diagrams,
59 are inadequate for managing site workspaces, mainly due to the lack of spatial representation [3]. Similarly,
60 traditional safety planning relies on manual observation, which is labor-intensive, time-consuming, and
61 potentially highly inefficient [8]. The resulting safety plans are often error-prone due to subjective judgments
62 of the available decision-makers. As of now, workspace planning has often been performed through
63 judgment or with the aid of 2D sketches [2]. Commercial 4D visual planning software tools (e.g., Autodesk
64 Navisworks [13], Synchro 4D [14], etc.) have improved display functionalities that can aid construction
65 managers and field engineers in their tasks but still lack automated assessment capabilities in favor of
66 workspace management [5].

67 This study investigates spatial simulation tools with advanced visualization functionalities to detect clashes
68 among workspaces, including looking beyond the case of geometric clashes between overlapping main
69 workspaces. An analysis of the advantages these tools can provide to those in charge of work planning will
70 be performed, and an enhanced workflow will be suggested. In addition, a methodology to develop an expert
71 knowledge system to assess the severity of detected conflicts will be reported and preliminarily tested and
72 compared with current state-of-the-art technologies.

73 Section 2 provides the scientific background about the latest research progress in workspace management,
74 the application of serious gaming technology in the AEC industry, and the Bayesian inference basics. Section
75 3 describes the methodology proposed by this study, whereas Section 4 presents the adopted use case. The
76 running of the proposed tool and benchmarks adopted in this study is described in Section 5. Finally, Sections
77 6 and 7 are devoted to the results of the experiments, the discussion, and the conclusions, respectively.

78 2. Scientific background

79 Nowadays, the need to consider the spatial dimension to ensure the schedule's feasibility and avoid critical
80 issues, such as safety, productivity, and constructability, is unanimously accepted by field experts. Stemming
81 from this assumption, researchers have spent many efforts on workspace definition, conflict detection, and
82 severity assessment. As emerged from the literature review, several approaches and technologies, mainly
83 based on geometric intersection tests between workspaces, have been proposed.

84 The workspace management process refers to three main phases [3,5]. The first one is the generation and
85 allocation of workspaces. The second one is the detection of congestion and spatial-temporal conflicts.
86 Finally, the third phase is the resolution of identified conflicts. Since this study focused on detecting spatial
87 conflicts and severity assessment, these topics will be the subject of sub-Sections 2.1 and 2.2. Afterward,
88 sub-Section 2.3 focuses on simulation environments adopted by past studies. Sub-Section 2.4 provides a

89 literature review of Bayesian inference applications in the AEC industry. Finally, sub-Section 2.5 formalizes
 90 the research questions answered by this study.

91

Table 1. Overview of workspaces' classification, conflicts taxonomies, and metrics from literature.

Akinci et al., 2002 [17]	Getuli et al., 2020 [16]	Thabet et al., 1994 [15]
Building component space (BCS) Labor crew space (LCS) Equipment space (ES) Temporary structure space (TSS) Protected space (PS) Hazard space (HS)	Workers space Equipment space Safety space (outward hazard) Hazard space (inward hazard)	<i>Object-based (Physical surrounding space)</i> Manpower Equipment Material <i>Space-based</i> Work blocks (Zone + Layer)
Design conflict (BCS-BCS) Safety hazard (HS-LCS) Damage conflict (PS-LCS/ES/HS) Congestion (LCS/ES-LCS/ES/TSS)		Conflicts Can share workspace (Class B) Cannot share workspace (Class A, C)
Conflict Ratio $C_R = V_C / V_R$ where V_C = conflicting volume, V_R = required volume		Metrics Space Capacity Factor $S_{CF} = V_A / V_R$ where V_A = available volume, V_R = required volume

Ma et al., 2020 [3]	Kassem et al., 2015 [5]	Zhang et al., 2015 [8]	Dawood et al., 2006 [12]
Entity space (ES) Efficient working space (EWS) Safety working space (SWS)	Object space Main space Support space Safety space	Building component space (BCS) Worker space Equipment/temporary structure space Space for material handling path Protective space	Product space Workspace Equipment space Equipment path Path space Storage space Process space Support space Protected space
ES-ES (h=100) ES-SWS (h=50) SWS-SWS (h=20) ES-SWS (h=10) SWS-EWS (h=5) EWS-EWS (h=1)	Temporal/Schedule conflict Spatial/Physical/Workspace conflict Workspace congestion	Design clashes Congestion Safety hazard	Design conflict Safety hazard Congestion Access blockage Damage Space obstruction Work interruption
Severity of the Spatio-Temporal Conflict $I_{12}=h(k_1 * S_{v1} * S_{t1} + k_2 * S_{v2} * S_{t2})$ where h =severity grade (1÷100), k_1, k_2 =urgency/danger grades (1÷10), S_{v1}, S_{v2} =ratio of spatial conflict relative to v_1, v_2 , S_{t1}, S_{t2} =ratio of coincident period relative to t_1, t_2	Severity of Conflict $S_C = T_C / T_A$ where T_C =conflict duration, T_A =activity duration Severity of Workspace Conflict $S_{WC} = V_C / V_A$ where V_C =conflicting volume, V_A =available volume Congestion of Severity $C_{gs} = V_R / V_A$ where V_R =required volume, V_A =available volume Workspace Criticality Level $W_{CL} = S_{WC} + C_{gs}$	Conflict Ratio $C_R = V_C / V_R$ where V_C =conflicting volume, V_R =required volume Space Criticality $S_C = V_R / V_A$ where V_R =required volume, V_A =available volume	Space Criticality $S_C = V_R / V_A$ where V_R =required volume, V_A =available volume

<p>Mirzaei et al., 2018 [1]</p>	<p>Product space</p> <p>Labor crew space</p> <p>Equipment space</p> <p>Temporary structure space</p> <p>Material storage space</p> <p>Hazard space</p>	<p>Labor congestion (RSD<50%)</p> <p>Constructability issue (RSD>50%)</p>	<p>Required Space Decrease per person $RSD=1-(A_{AP}/A_{RP})$ where A_{AP}=available workspace per person for activity, A_{RP}=required workspace per person for activity</p>
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92 **2.1. Workspace definition and conflicts detection**

93 The hierarchical classification of workspaces, known as Location Breakdown Structure (LBS), can help develop
94 work plans and manage the project’s physical size and complexity [18,19]. 2D working areas have been
95 defined irrespective of the activities to be performed. According to [18], an LBS should include the five levels
96 of detail, namely: (1) project, (2) buildings or sections, (3) floors, (4) stage of implementation, and (5) zones.
97 Another application divides the floor into same-size areas (zone-LBS) or considers the position of seismic
98 joints (area-LBS) [19]. However, the limitation of this approach is that it cannot classify non-structured
99 buildings, such as large open spaces lacking demarcating zones or renovation works.

100 Due to the wide variability of scenarios, other works have suggested several classifications, which adopt
101 different approaches, including object-, activity-, space- and process-based classifications.

102 The object-based classification uses a 3D visualization of workspaces and requires allocating volumes
103 adjacent to the building element under construction for specific functions [5,12,17]. An example can be
104 provided by the micro-level discretization defined in [17], which includes the following workspaces: building
105 component space, labor crew space, equipment space, hazard space, protected space, and, finally,
106 temporary structure space (Table 1). Complementarily, the concepts of macro-level (e.g., storage areas) and
107 paths (e.g., equipment’s and crews’ paths) discretization have been introduced [12].

108 An activity-based classification focused on Health and Safety (H&S) management has been defined in [16,17],
109 where safety and hazard spaces correspond respectively to outward and inward hazards (Table 1). Another
110 unique classification for the three discretization categories was proposed (Table 1) [12]. Also, a macro- and
111 micro-level discretization can help differentiate labor crew workspaces into static and dynamic ones [1].
112 In the first case, the entire workspace is required throughout the activity duration; in the second case, the labor
113 crew occupies a specific portion of the space during each time interval. Four execution patterns have been
114 defined to simulate labor movement through the subspaces. In [8], a micro-level discretization and the
115 material handling path space have been introduced. In the research presented in [3], the workspaces defined
116 by the studies mentioned above have been grouped into two main categories: entity and working spaces.
117 The first includes the space occupied by laborers, mechanical equipment, and building components, whereas
118 the second corresponds to the spaces required to ensure smooth operation and tasks.

119 In [15], the authors compare an object-based and a space-based workspace definition to quantify workspace
120 demand and availability. The authors include some of the space categories seen in previous works in the
121 object-based workspace definition, such as manpower, equipment, and material spaces. In the space-based
122 workspace definition, a work block is the combination of a zone (i.e., the portion of the architectural layout
123 of the floor) and a layer (i.e., the status of construction work progress in a zone within a specific time). In
124 order to include the effects of dynamicity, a novel method for look-ahead equipment workspace during
125 earthworks was developed in [20]. For this purpose, Dynamic Equipment Workspaces (DEWs) and Look-

126 Ahead Equipment Workspaces (LAEWs) have been defined. The two types of workspaces differ in that while
127 DEWs are generated based on the equipment pose, state, geometry, and speed in real-time (to form a safety
128 buffer around the equipment that can help to prevent collisions), LAEWs are built based on the predicted
129 future motion of equipment and operator visibility in near-real-time (to help finding a collision-free path for
130 equipment). This method enables different pieces of equipment to ensure that their initially planned paths
131 are collision-free, or it adjusts their path planning to avoid potential collisions.

132 Inspired by the manufacturing industry, a shift from object-based to process-based workspace definition has
133 been proposed in [5]. In addition to the workspaces occupied by building elements and reserved as safety
134 distance, the working area is discretized considering the value added by the activities (Table 1). For example,
135 building a wall requires a “main workspace” since it adds tangible value to the project; on the contrary,
136 transferring materials requires a “support workspace”, a preparatory activity supporting the first one.

137 Another challenge relies on the estimation of the shape and size of workspaces. A first approach is to
138 represent workspaces as user-input rectangular prisms [17], whereas in other applications, they are
139 represented as user-inputted bounding boxes [2,3,5,16]. In the studies mentioned above, workspace
140 occupation is either estimated based on the authors' background or experience or estimated by the user as
141 input values during simulation. On the contrary, the authors in [8] implement an occupancy model to define
142 distance offsets from the building components under construction; in this way, they infer the workspace
143 allocation based on historical workforce location data densities.

144 For the sake of a realistic estimation of clashes and temporal dependences, once workspaces have been
145 defined, they must be associated with specific time slots in which each correspondent activity is scheduled.
146 In other words, the 3D model is extended towards the fourth dimension, i.e., time [1–3,5,8,12,17].

147 Running 4D simulations can lead to the identification of potential interferences within the project schedule
148 and their visualization. This approach assumes that time-space conflicts may occur only between concurrent
149 activities [17]. In addition to the temporal detection, some authors report other approaches available in the
150 literature to identify spatial issues. For example, the approximation detection compares the length of the line
151 connecting center points for every pair of adjacent workspaces against the combined lengths of workspaces'
152 radii [21]. In the topographical detection, each workspace is assigned a spatial matrix, and the entry-wise
153 product of matrices would mark the collisions [22]. Finally, geometrical intersection tests check each
154 workspace against all other ones (pairwise comparison) for detecting eventual overlaps, called
155 Spatial/Physical/Workspace conflicts [2,5], as reported in Table 1. The last approach, based on pure
156 geometric intersection tests, is the most widely adopted method in literature for detecting spatial conflicts
157 [1,3,5,16,17].

158 Lately, several studies have attempted to classify spatial interferences between tasks that share the same
159 workspace. One of the first time-space conflict taxonomy in construction differentiates design conflicts,
160 safety hazards, damage conflicts, and congestions [17] (Table 1). The first category occurs when there is a
161 conflict between two building components. Since existing commercially available applications (e.g., clash
162 detection and coordination) already solve this issue [8], design clashes are outside the scope of this research.
163 According to [17], a safety hazard occurs when the space required by a hazardous activity (e.g., hazard space)
164 conflicts with the space allocated to a labor crew. Indeed, sharing a space, which should be left free to protect
165 a building component, with a labor crew, a piece of equipment, or a hazardous space may cause damage
166 conflicts. The mutual sharing of space between labor crews, equipment and temporary structures identifies
167 a more or less severe congestion [5,17]. On the contrary, the authors in [15] differentiate the activities that
168 can share the workspace and those that cannot share it to define a work schedule. The taxonomy presented
169 in [17] has been adopted by the authors in [8,12] and extended in [12], with path-related conflicts (e.g.,
170 access blockage and space obstruction). Other authors consider two types of spatial interferences, namely
171 labor congestion and constructability issue [1], corresponding respectively to Acceptable (ASI) and

172 Unacceptable Spatial Interferences (USI) [23]. Finally, a time-space conflict taxonomy, including the three
173 available combinations between the Entity Spaces (ES) and Working Spaces (WS), is presented in [3]. As long
174 as two different entity spaces (ES-ES) overlap, a breakage in the building element is caused [17]. In case an
175 entity crashes into a working space (ES-WS), delays of construction and, in some cases, accidents occur.
176 Finally, an interference between working spaces (WS-WS) occurring between parallel activities, corresponds
177 to a particular scenario of congestion [2,17].

178 As mentioned earlier in this text, spatial conflicts are detected in existing studies by simply carrying out
179 geometric intersection tests between defined workspaces. Although being able to provide early valuable
180 results and enabled process automation, this approach overestimates the results and fails to detect clashes
181 that are not purely geometric.

182 In addition, most existing studies consider object-based workspace taxonomies that allocate static
183 workspaces around building elements under construction for very specific purposes. Due to this strong
184 assumption, these studies look for spatial conflicts between static object-based workspaces. The possibility
185 of crews and equipment moving and eventually getting into conflicts within the construction site has been
186 sporadically considered [1,4,8,20]. This gap must be addressed by considering more realistic simulations.

187 Finally, a workflow that integrates currently available construction planning methods and the most advanced
188 simulation systems (e.g., based on physics simulations, expert knowledge, etc.) for detecting spatial conflicts
189 must be defined. This would improve existing construction planning approaches by covering their gaps and
190 ease the assessment of the added values provided by novel spatial conflict simulators.

191 2.2. Conflict's severity assessment

192 In order to rank lists of conflicts generated as a result of an automated conflict detection, the activities'
193 conflicting status must be evaluated by adopting metrics that concisely describe the severity of conflicts and
194 their overall trend. For this purpose, several metrics for evaluating the magnitude of the collisions are
195 available in the literature. Some can assess the conflicting status between workspaces by computing ratios
196 between volumes and/or setting arbitrary thresholds for different congestion severity levels [5,8,12,15,17]
197 (Table 1). More sophisticated metrics also consider temporal, severity, urgency and danger parameters [3]
198 (Table 1). Other metrics assess the conflict severity based on decreased workspace per person for a given
199 activity [1] (Table 1). The main limitation of this assumption is that some spatial conflicts may occur even if
200 workspaces are not reduced or do not intersect each other (e.g., struck-by risk from falling objects, electrical
201 risk, etc.).

202 2.3. Simulation environments of spatial conflicts

203 Past studies address spatial conflict challenges by adopting different technological approaches. Low-tech
204 workspace management applies LBS and spreadsheet applications (e.g., Microsoft Excel) [18,19]. The familiar
205 and easy-to-use interface of such applications represents the strength of this approach. In contrast, the
206 approximate 2D-modelling of space and the too rigid and arbitrary workspace discretization provided by LBS
207 affect the results.

208 These issues are overcome by high-tech workspace management approaches that apply BIM for a continuous
209 3D modeling of space and the definition of the 4D model by linking tasks and building elements. In this
210 context, serious game engines are promising tools to integrate semantically rich models (e.g., BIM models)
211 and simulation engines. The first application of gaming technology can be found in the aircraft industry, using
212 Microsoft Flight Simulator for educational purposes [24].

213 Later, serious game engines became widespread in the AEC industry, demonstrating that mere
214 entertainment is not the only feasible or promising application. The success of this approach is due to the
215 difficulty in carrying out real field experiments in some research areas, such as construction management,

216 which usually requires quite a huge budget and time to set up an experimental study. Using game engines
217 facilitates the deployment of virtual testbeds and test execution.

218 In the construction industry, game engine usage was first limited to construction safety training purposes. In
219 2009, Torque 3D game engine was applied to develop a tool to enhance electrical safety awareness within
220 the construction industry [25]. Virtual safety learning platforms have been developed using Unity3D™ [26]
221 and head-mounted display (HMD) technologies [27]. A similar technological stack can be applied to develop
222 a virtual learning environment for multiplayer lean training [28], with the possibility of collecting run-time
223 feedback [29].

224 Several studies applied serious game engines to improve collaboration and communication in construction.
225 A tool based on the Java-based jMonkeyEngine 3.0 game enabled clients to navigate in first-person design-
226 in-progress environments [30]. Another example is the Database-supported VR/BIM-based Communication
227 and Simulation (DVBCS), a middleware and communication system between the design team and
228 stakeholders, developed in [31] using the Unreal game engine and tested in healthcare design. Similar-
229 purpose systems have been developed using Unity3D™ too [32,33] and adopting openBIM principles (i.e.,
230 IFC format rather than a vendor-specific one) [34]. The integration in Unity3D™ of BIM models and as-built
231 images, processed via various computer vision techniques, enables the definition of a 3D virtual environment
232 of the construction site that can be updated automatically according to work progress [35]. Another tool,
233 developed in Unity3D™ and tested for modular-based construction projects, integrates four main project
234 teams (i.e., design, production, transportation, and construction teams) and supports them by providing a
235 virtual environment to visualize their process to make better-informed decisions [36].

236 The application of serious game engines recently embraces simulations of physical building dynamics and
237 behaviors of virtual building users, such as in the framework called Design-Play and based on the Microsoft
238 XNA game engine, for design validation [37]. Blender, an open-source gaming engine, has been applied to
239 develop parallel and loosely coupled simulation-driven visualizations of industrial construction operations
240 [38]. An Industry Foundation Class (IFC) compliant 4D tool has been developed using the Microsoft XNA game
241 engine as a holistic solution for workspace management, including workspace allocation, conflicts detection
242 and real-time resolution [5]. A holonic emergency management system, based on Unity3D™, can compute
243 the most effective way out by pathfinding algorithms (i.e., A*) and enhance the contribution given by
244 standard emergency plans [35]. Unity3D™ has been applied to simulate activities and analyze the
245 productivity difference between conventional and robotics-based modular construction [39]. Other
246 Unity3D™ game engine applications have resulted in a digital twin mock-up that implements a BN for the
247 real-time assessment of runover hazards by drilling machines [40] and fall hazards [41]. Unity3D™ spatial
248 simulators aim to detect conflicts among main and support workspaces to address COVID-19 threats [42] and
249 struck-by hazards [43,44].

250 Previous studies prove the possibility of importing Building Information Models by an open file format (i.e.,
251 IFC) into a serious gaming environment [31,33,34]. The 4D BIM model has been recreated within the gaming
252 environment [28], specifically for workspace management [5]. A proof-of-concept of a reasoner,
253 implemented using a BN within a serious game engine, has been presented [40]. Some authors have
254 demonstrated the possibility of integrating simulation functionalities with game engines [45]. This can carry
255 out dynamics and physics simulations directly within a BIM-based construction site environment recreated
256 in Unity3D™ [41]. Unity3D™ game engine, being widely adopted by past studies and supporting C# scripting
257 for endless functionalities implementation, represents the candidate tool for this study.

258 2.4. Bayesian inference and its applications in AEC

259 A system that assesses the severity of spatial-temporal conflicts must reproduce how humans perform
260 cognitive tasks. This implies developing applications that can perform both steps of inference reasoning
261 conditioned upon contextual evidence and knowledge elicitation from experts. The core claim of Bayesian

262 reasoning, called conditionalization, is that it can adjust prior beliefs given new evidence [54]. This is suitable
263 for scenarios where a model describing a set of events can be defined in advance. However, the severity of
264 the outcomes is conditioned upon a set of pieces of evidence that change over time. In this context, the
265 advantages of Bayesian networks (BNs) are largely in simplifying conditionalization, planning decisions under
266 uncertainty, and explaining the outcome of stochastic processes [55]. Basically, BNs are graphical models for
267 reasoning under uncertainty, where the nodes represent variables and arcs represent the quantitative
268 strength of those direct connections, allowing probabilistic beliefs to be updated automatically as new
269 information becomes available [54].

270 Several studies applying BNs to manage construction-related issues have been published in the last 20 years.
271 A literature review mapped articles selected within the last two decades against the 12 construction
272 management functional areas defined by [46] to identify the major areas of Bayesian application [47].
273 Bayesian approaches are most frequently applied in safety management, followed by risk management,
274 contract management and process control, demonstrating the merits of Bayesian approaches to deal with
275 uncertainties and the interdependencies of multiple factors. Most of the selected studies apply BN for
276 predictive reasoning, whereas the Bayesian diagnostic function is relatively underutilized compared to
277 prediction.

278 2.4.1. Application to safety management

279 As reported in [47], the application of Bayesian approaches to safety management is mainly related to safety
280 performance [48–51], the selection of effective safety management strategies [51–53], and safety
281 supervision [54–58].

282 The full potential of Bayesian approaches to analyze the interdependencies of a wide range of physical and
283 psychosocial hazards is yet to be exploited [47]. Existing Bayesian research on safety performance has mainly
284 adopted a static approach, whereas the potential to use dynamic BNs to capture the changes in safety
285 performance over time (e.g., before and after implementation of safety interventions or in different project
286 phases) is underutilized.

287 2.4.2. Application to risk management

288 Risk assessment is the most popular application field of Bayesian approaches in risk management [47]. BNs
289 have the advantages of showing the propagation influence of risks in a network and updating the
290 interdependency among risks when new information is available, overcoming the limitation of structural
291 equation modeling, artificial neural networks and other simulation techniques in analyzing risks [59].

292 As reported in [60], risk assessment includes two main processes: estimating the occurrence probability [61–
293 65] and impacts [65–67] of certain events to calculate risk. Although Bayesian approaches are widely applied
294 to manage risks in construction-related research, the interaction and propagation of risks throughout the
295 whole lifecycle of construction projects are relatively understudied [68]. To solve this, [68] proposes a
296 modified BN to consider risk propagation in different stages.

297 Bayesian approaches for risk management are applied to various types of projects, such as excavation
298 projects [62,65,69], deep foundation pit construction [70], buried infrastructure [71] and high-speed rail
299 projects [72]. For these projects, the historical data are limited and difficult to obtain. Bayesian approaches
300 are able to combine both objective data from field observation and subjective data from expert knowledge,
301 which can improve the quality of input data and achieve a relatively high assessment precision even with a
302 small number of samples [61,70].

303 Generally, applying Bayesian approaches to risk management still has room for improvement in dynamic risk
304 management (i.e., covering all stages of the project), whole process risk management (i.e., covering all steps
305 of risk management) and comprehensive consideration of the risk occurrence probability and impact degree.

306 2.4.3. Application to contract management

307 Bayesian approaches are used in the contract management field to analyze construction contractual risks
308 [73,74], deal with disputes [75–82], improve the effectiveness of bidding decisions [83–86] and the efficiency
309 of required contractual text extraction [87].

310 Further studies are needed to explore the application of Bayesian approaches in contract management, such
311 as expanding the influence of a single contractual risk to a set of contractual risks in a construction project
312 and applying the established model to more scenarios (e.g., different types of construction projects and
313 market conditions) [47].

314 2.4.4. Application to process control

315 Process control includes various activities, such as management of project schedule [64,88,89], productivity
316 and resource allocation [90–95] for achieving project success.

317 Although Bayesian approaches have been adopted in the above areas of process control, the application in
318 each area still needs to be further investigated in different contexts [47]. There is limited application of
319 Bayesian approaches for efficient allocation of resources and the workforce in specific construction projects,
320 which concerns process control.

321 2.5. The research questions answered by this study

322 This study shows that by combining physics simulations with geometric computations, even those spatial-
323 temporal conflicts that are not caused by direct overlapping of main workspaces can be detected. For this
324 purpose, the process-based workspace taxonomy, inherited from the manufacturing industry and presented
325 in [5], has been adopted. In this first implementation of the proposed spatial conflict simulator, main
326 workspaces have been considered. This tool, including an interface between the simulation environment and
327 the BIM model of the building under construction, has been developed in a serious gaming environment. In
328 addition, a methodology and a demonstrator concerning the integration of a Bayesian reasoner in the form
329 of a BN are developed. The combined simulator embedding the BN is showcased to automatically update the
330 severity assessment of detected spatial-temporal conflicts due to workspace displacement and the scheduled
331 work plan. This is applied in the specific case of crews that may be struck by falling objects. Finally, a
332 comparison between the performance of this novel system and the state-of-the-art commercial software
333 tools is provided.

334 The robustness of the proposed approach, although only main workspaces are considered at this level of
335 development, resides in the following multi-steps process for detecting and assessing spatial conflicts:

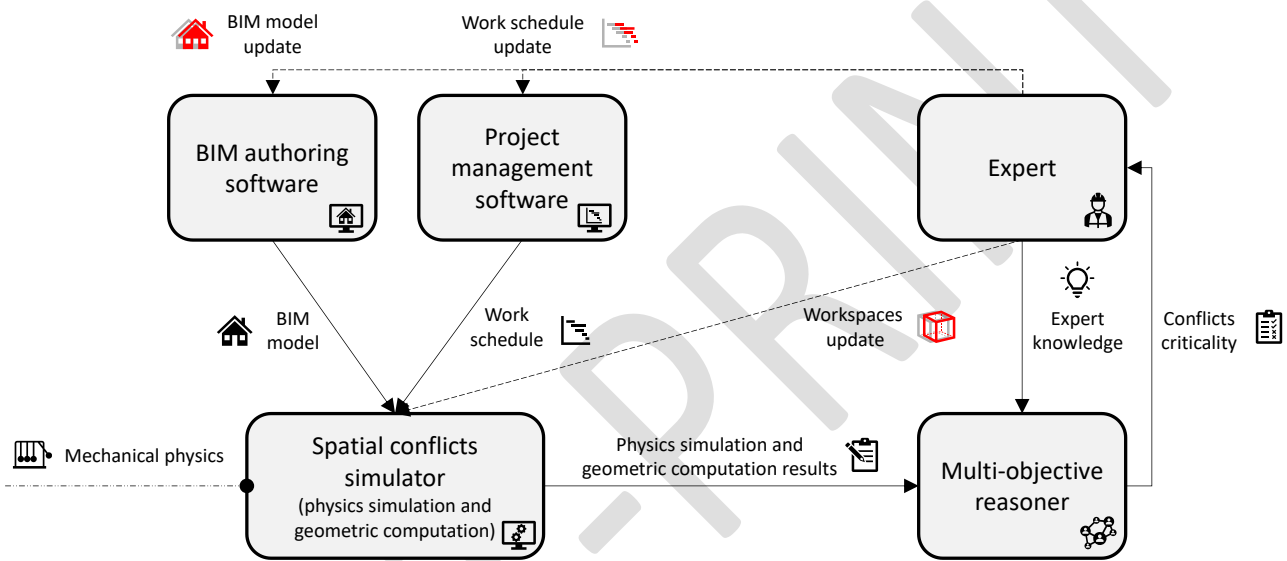
- 336 1. “Direct conflicts” between workspaces at their static positions are searched by carrying out
337 geometric computations.
- 338 2. “Indirect conflicts” between workspaces affected by construction site dynamics are searched by
339 conducting physics simulations and geometric computations.
- 340 3. The criticality of eventual “indirect conflicts”, detected in the previous step, is computed by Bayesian
341 inference that supports the project manager in filtering out the ones that can be considered non-
342 critical or false positives.

343 A limit of the proposed approach is the fact that spatial conflicts among incompatible workspaces (e.g.,
344 electrical hazards) have not been addressed yet. Another limitation resides in the refinement process of the
345 work schedule. In fact, given the definitive list of detected spatial conflicts, the project manager would rely
346 only on his/her experience to detect the set of activities that must be scheduled earlier or later.

347 **3. Methodology**

348 **3.1. System architecture**

349 In order to cover these research gaps, this study presents a novel methodology that integrates the work
350 planning phase with a spatial conflict simulator and a Bayesian reasoner. The resulting system architecture
351 is depicted in Figure 1. The BIM authoring and the project management software provide the BIM model and
352 the work schedule to the spatial conflicts simulator. The latter embeds mechanical physics and carries out
353 physics simulations and geometric computations. Simulation results are transferred as a list of spatial
354 conflicts to the Bayesian reasoner fed by expert knowledge and sent back to the expert for further
355 consideration. At this point, the expert can resolve detected spatial conflicts by carrying out the required
356 action, such as updating the BIM model, the work schedule, or the workspace size. In Figure 1, solid arcs
357 represent the interfaces implemented in this study.



358

359

Figure 1. System architecture.

360 **3.2. Workspace management framework**

361 Implementing the proposed system architecture leads to the definition of a novel workspace management
362 framework described by the Business Process Model (BPM) (Figure 2). The top lane of the BPM includes the
363 tasks executed by the project management team during the construction planning phase, the middle lane
364 represents a simulation hub, and the bottom lanes depict the functioning of the proposed spatial conflict
365 simulator and the Bayesian reasoner.

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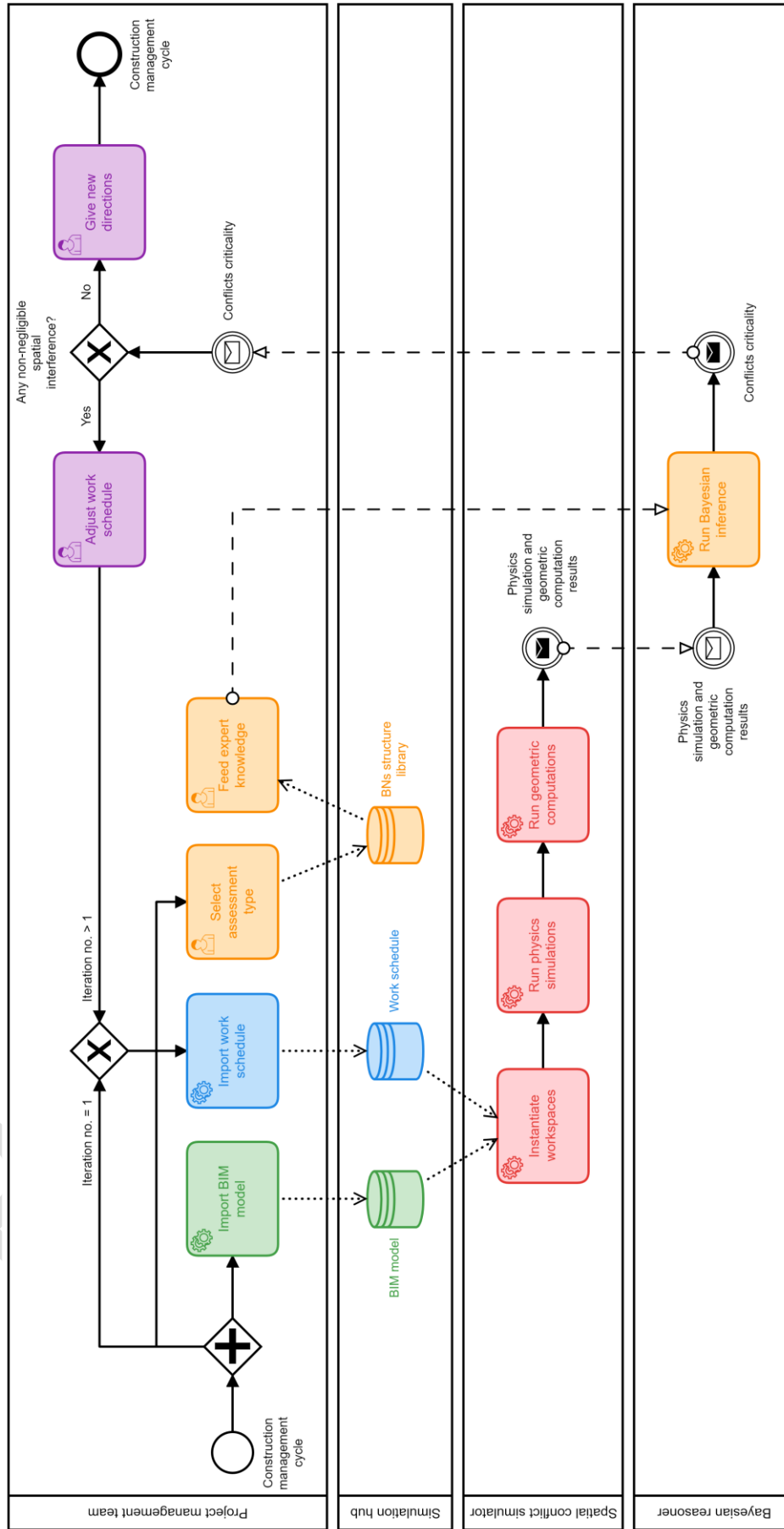


Figure 2. Overview of the proposed workspace management framework with the implementation of the proposed system architecture (please use color in print).

369 As indicated by the parallel gateway reported at the beginning of the BPM, the construction manager
370 executes three main tasks in parallel. Green and blue nodes describe, respectively, the process of loading the
371 BIM model and the work schedule within the simulation hub implemented in the serious gaming environment
372 (i.e., “Load BIM model” and “Import work schedule” tasks). Orange nodes describe the process of selecting
373 the type of assessment to carry out by one of the Bayesian networks (BNs) structures pre-loaded in the
374 library. Whereas expert knowledge applied to define the BNs’ structure (i.e., the cause-effect relationships
375 between node variables, referred to as “Causal knowledge”) can be considered generally true, the one
376 affecting conditional probability (i.e., “Conditional probability knowledge”) is contextual and must be
377 provided by the construction management team who knows in detail the construction process under
378 assessment. Hence, the construction management team is asked to provide this kind of knowledge by filling
379 the conditional probability tables (CPTs) (i.e., “Feed expert knowledge” task).

380 At this point, the simulation hub can be considered as initialized, and both the spatial conflict simulator and
381 the Bayesian reasoner are ready to start the simulation process. Red nodes are related to the workspaces’
382 generation and related physics simulations and geometric computation. First, the workspaces are generated
383 within the serious gaming environment (i.e., “Instantiate workspaces” task), given as inputs both the BIM
384 model and the work schedule. The instantiated workspaces are the input of the physics simulations (i.e., “Run
385 physics simulation” task) and geometric computations (i.e., “Run geometric computation” task). Geometric
386 intersection tests between main workspaces are carried out, considering them in their static position and
387 then falling down under the law of gravity. As a result, spatial conflicts are detected and labeled as either
388 “direct” in the first case or “indirect” in the second one. Their criticality level is computed by the Bayesian
389 reasoner (i.e., “Run Bayesian inference” task) to support the project management team in refining the work
390 schedule. The decision-making process is represented by purple nodes and the exclusive gateway. The
391 project management team adjusts the work schedule if any non-negligible spatial interference is detected;
392 otherwise, they can give instructions on the field.

393 3.3. Integration with existing technologies

394 One of the key features of the proposed methodology is the integration with existing technologies (Figure 2).
395 In fact, a BIM model can be generated using any of the BIM authoring software tools available in the market
396 (e.g., Autodesk Revit in our implementation) and then exported as an IFC file. Similarly, the work schedule
397 can be done using a commercial project management software tool (e.g., Microsoft Project in our
398 implementation). A resource-constrained schedule is generated by defining first the baseline and allocating
399 available resources. Then, the resulting work schedule can be exported into the CSV or XML format. The
400 information in machine-readable file formats, like IFC, CSV and XML, is used to define the 4D model required
401 to generate workspaces within the proposed spatial conflicts simulator. In Section 4, this integration is done
402 in a real use case. A BIM model and a work schedule related to the execution of construction works will be
403 presented.

404 3.4. Development of the spatial conflicts simulator

405 The first added value of the proposed approach is the integration of 4D BIM data, provided by commercial
406 tools, into an environment carrying out physics simulations and geometric computation. The literature
407 review reported in Section 2.3 indicates serious game engines as a proper technical solution. In fact, game
408 engines embed mechanical physics, enable the execution of physics simulations, and can enhance the range
409 of spatial conflicts detected by existing commercial tools. Contrary to the rule-based approach usually
410 adopted by currently available 4D software, serious game engines enable the adoption of an agent-based
411 approach to effectively simulate the interaction among involved agents.

412 In this study, the Unity3D™ game engine was chosen to develop the proposed spatial conflicts simulator.
413 Unity3D™ has been widely adopted by past studies (Section 2.3) and industries beyond video gaming, such
414 as film, automotive, architecture, engineering, construction, and the United States Armed Forces [96]. This

415 game engine, supporting C# scripting, ensures the implementation of endless functionalities. The integration
416 of multiple spatial conflict simulator's C# scripts with the overall workspace management framework is
417 depicted in Figure 3. Every task of the Business Process Model, labeled by a squared brackets' caption,
418 represents a component of the serious gaming tool. In addition, for each task, input and output are
419 represented, respectively, by an ingoing and an outgoing arrow.

420 The "File Chooser" C# script (Figure 3), developed in-house by the authors based on the IFC Engine DLL library
421 [97], enables importing the Building Information Model in IFC format into the gaming environment. The
422 advantage of importing the IFC model is that topological information, material properties, and semantic
423 information are directly applied to the building model in the serious gaming environment. This IFC Loader
424 models the environment using one of the most powerful techniques in solid modeling: boundary
425 representation (B-REP). B-REP represents a solid as a collection of connected surface elements, which are the
426 boundary between solid and non-solid.

427 The "Model Input" C# script imports the works schedule in CSV format to define, along with the building
428 model, the 4D BIM model. The latter is received as an input by the "Instantiate main workspace from IFC" C#
429 script to generate main workspaces linked to the work schedule tasks. At this point, the "Intersection test"
430 C# script uses workspaces-related information to run physics simulations and geometric computations. This
431 script includes several methods. The "FindSpatialConflict()" (Figure 4 (a)) method carries out a geometric
432 intersection test between main workspaces in their initial static position and provides a list of so-called
433 "direct" spatial conflicts. The "FindAllOverlaps()" (Figure 4 (b)) method, instead, carries out a geometric
434 intersection test during physics simulations in a gravitational environment. The "OnTriggerEnter(Collider
435 other)" (Figure 4 (c)) method, attached to each main workspace, detects spatial conflicts between the main
436 workspaces while the physics simulation is running.

437 An application example of the presented spatial conflicts simulator is provided in Section 5.1.

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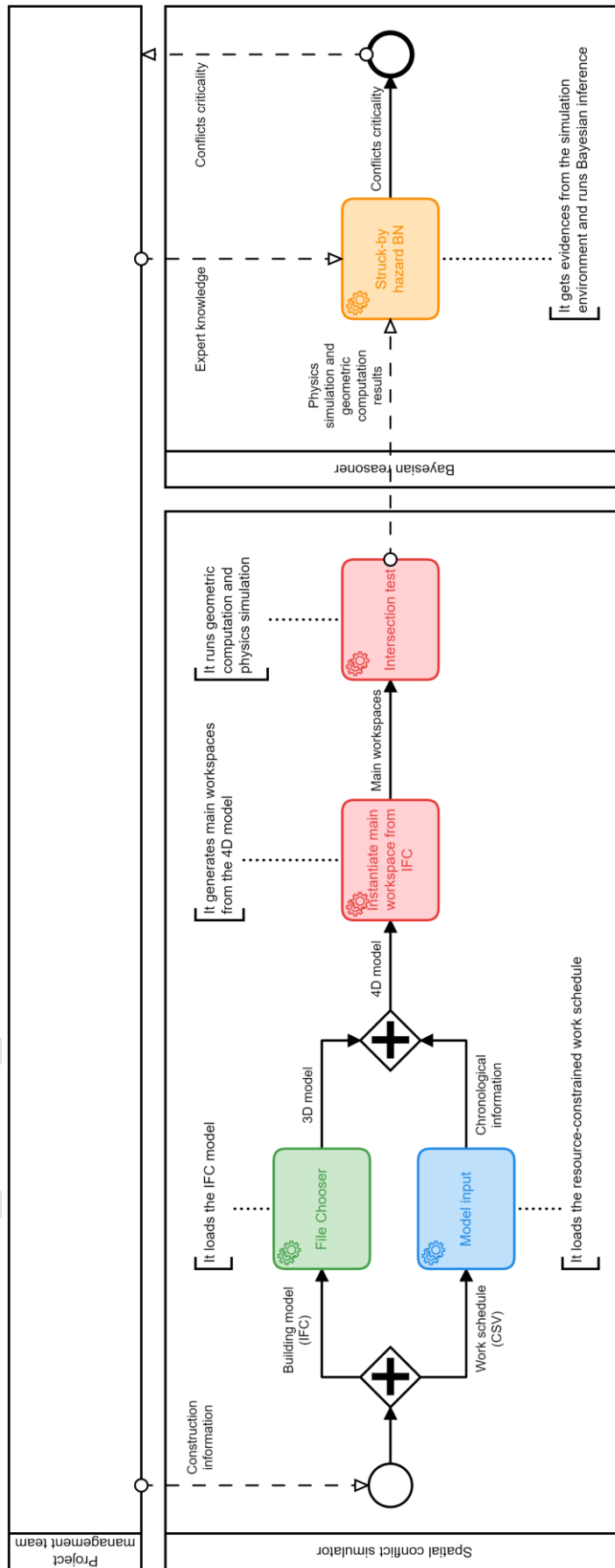


Figure 3. Simulation workflow describing the integration of the spatial conflict simulator's C# scripts for Unity3D™ with the overall workspace management framework.

```

FindSpatialConflict()
CREATE empty workspaces array(gameobject)
GET gameobjects having tag equal to "Workspace"
ADD gameobjects having tag equal to "Workspace" to workspaces array
CREATE conflicts dictionary(integer, gameobject array)
GET display conflicts material
FOREACH i-th gameobject in workspaces array
    FOREACH J-th gameobject in workspaces array
        COMPUTE hash sum of i-th gameobject and j-th
        gameobject
            GET i-th crew string
            GET j-th crew string
            IF i-th gameobject is different from j-th
            gameobject AND conflicts dictionary does
            not contain hash sum AND i-th crew string
            is different from j-th crew string AND i-th
            gameobject intersect j-th gameobject
                ADD conflict(hash sum, (i,j)) to conflicts
                dictionary
                SET i-th gameobject material equal to display
                conflicts material
                SET j-th gameobject material equal to display
                conflicts material
            END IF
        END FOREACH
    END FOREACH
END

```

(a)

```

FindAllOverlaps()
CREATE empty workspaces array(gameobject)
GET gameobjects having tag equal to "Workspace"
ADD gameobjects having tag equal to "Workspace" to workspaces array
CREATE overlaps dictionary(integer, gameobject array)
GET display conflicts material
GET simulation duration
START COROUTINE PhysicsSimulation()
    FOREACH i-th gameobject in workspaces array
        GET i-th gameobject initial position
        SET Rigidbody useGravity as true
        WAIT for seconds (simulation duration)
        SET Rigidbody useGravity as false
        SET Rigidbody constraints as freezeAll
        SET i-th position equals to initial
        position
    END FOREACH
END COROUTINE

```

(b)

```

OnTriggerEnter(Collider other)
IF other has tag equals to "Workspace" AND game object crew string
is different from other crew string THEN
    COMPUTE hash sum overlaps of gameobject and other
    CREATE overlaps array(collider) containing gameobjects and
    other colliders
    IF overlaps dictionary does not contain hash sum overlaps
    THEN
        ADD (hash sum overlaps, overlaps array (collider))
    END IF
END IF
END

```

(c)

441

Figure 4. Pseudo-codes of the methods defining the "Intersection test" C# script for Unity3D™.

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3.5. Development of the Bayesian reasoner

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Bayesian networks (BNs) represent a powerful knowledge representation and reasoning tool to visually model conditional probabilistic relationships among a set of variables [98]. As mentioned in sub-Section 2.4, they are made of connected nodes and can perform diagnostics and predictive reasoning. In this study, the second type of reasoning has been applied. It flows along the path pointing from new information about causes, that is, evidence included in the network through the instantiation of the set of query nodes associated with the variables representing causes, towards new beliefs about query nodes, i.e., the severity of a detected conflict. In fact, as soon as variables are instantiated with new evidence, the corresponding variables are set at a particular value. For BNs' basics and examples of computing posterior probability, given conditional probability tables (CPTs), the authors refer to [61,62,98].

452 BNs have many advantages, such as suitability for small and incomplete data sets, the combination of
453 different sources of knowledge, the ability to model causal relationships among variables, and the explicit
454 handling of uncertainty for decision analysis [98].

455 In this study, a BN for assessing struck-by hazards of objects that may fall and constitute a threat for laborers
456 at a lower level is developed. The results of the simulations represent the input of the Bayesian inference
457 (i.e., the “Run Bayesian inference” node). Its role is to estimate the severity of each detected spatial conflict.
458 Each spatial conflict will be assessed by running Bayesian inference and estimating its criticality level as “low”,
459 “medium”, or “high”. This approach has the potential to label any detected spatial conflicts in the simulator
460 that are not critical.

461 The approach adopted for developing the BN comes from the basic concept presented in [98]. An accident
462 due to struck-by hazards can be described as originated from a combination of triggering conditions and acts.
463 An act can be defined as the possibility that whatever element falls to a lower level. The triggering condition
464 can be defined as the vulnerability of laborers to be hit by elements that may potentially fall down. This
465 general model is based on a risk factors classification into four levels: external (e.g., factors related to political
466 or external issues), policy (e.g., factors related to contracting strategy, ownership and control, and
467 construction company culture), organizational (e.g., factors related to site organization and local
468 management), and direct ones (e.g., factors related to site technicians).

469 The BN depicted in Figure 5 originates from the basic cause-effect relationship between the event and
470 triggering acts/conditions and the general BN model introduced by [98]. For simplicity, three out of four risk
471 factor levels defined in [98] have been considered in this first implementation.

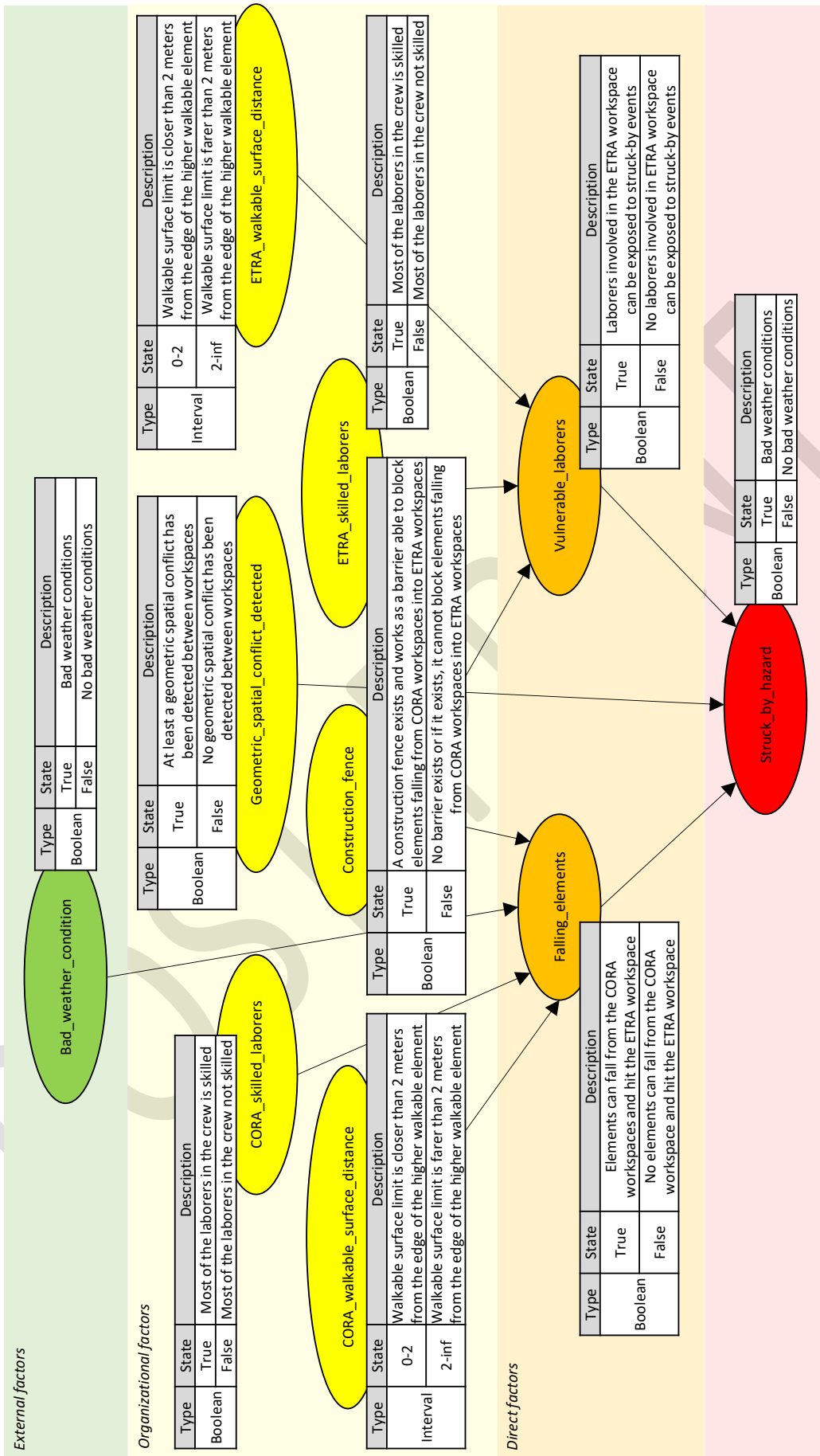


Figure 5. BN, proposed by this study, for assessing the probability that struck-by hazards may occur.

474 Listing the variables of the proposed BN (Figure 5) from the bottom to the top, the first variable is
 475 “Struck_by_hazard”. It models the possibility that laborers in the Exposed-to-Risk-Activities (ETRA)
 476 workspace (i.e., the lower one) may be struck-by falling objects from the Cause-of-Risk-Activities (CORA)
 477 workspaces (i.e., the higher one). The “Direct factors” level’s variables are “Falling_elements” and
 478 “Vulnerable_laborers”. According to [98], the first one is the possible occurrence, whereas the second one is
 479 the triggering condition. The “Organizational factors” level’s variables of the proposed Bayesian network are
 480 “Construction_fence”, “Geometric_spatial_conflict_detected”, “CORA_skilled_laborers”,
 481 “ETRA_skilled_laborers”, “CORA_walkable_surface_distance”, and “ETRA_walkable_surface_distance”. The
 482 “External factor” level’s variable of the proposed Bayesian network is “Bad_weather_condition”.

483 Once the Bayesian network is defined, it must be trained with data from experts [99]. This process is
 484 commonly defined elicitation of expert opinion. The authors have carried out this process by filling every CPT
 485 according to their experience. In order to make the Bayesian inference fully operational, the overall CPTs,
 486 reported in Table 2, are obtained by averaging the probability density functions provided by each author
 487 during the survey. These values, representing the authors’ knowledge, are assumed only for validation
 488 purposes and do not have to be considered as the unique possible configuration. For a reading example of
 489 CPTs, reported in Table 2, the reader is referred to [43].

490 Once the Bayesian network is trained, it is implemented in the serious game engine Unity3D™ by developing
 491 the “Struck by hazard BN” C# script (Figure 3). The script automatically gets the results of geometric
 492 computations and physics simulations from the spatial conflict simulator and updates the criticality levels of
 493 spatial conflicts. This study applies the commercial Discrete Bayesian Network library [26] for Unity3D™ to
 494 implement the struck-by hazard BN in the serious gaming environment. The “Struck By Hazard BN” C# script
 495 (Figure 3) implements the developed Bayesian network and the methods for carrying out physical simulations
 496 and getting the Bayesian network variables’ evidence.

497 An example of the presented Bayesian reasoner is provided in Section 5.2.

498 *Table 2. CPTs, obtained as the average of the authors’ ones, corresponding to each child node: (a) “Falling_elements”, (b)*
 499 *“Vulnerable_laborers”, and (c) “Struck_by_hazards”.*

Falling_elements																	
CORA_skilled_laborers	False									True							
Bad_weather_condition	False				True				False				True				
CORA_walkable_surface_distance	0-2	2-inf	0-2	2-inf	0-2	2-inf	0-2	2-inf	0-2	2-inf	0-2	2-inf	0-2	2-inf	0-2	2-inf	
Construction_fence	False	True	False	True	False	True	False	True	False	True	False	True	False	True	False	True	
False	0.1	0.8	0.8	0.9	0	0.7	0.7	0.8	0.2	0.9	0.9	1	0.2	0.8	0.8	0.9	
True	0.9	0.2	0.2	0.1	1	0.3	0.3	0.2	0.8	0.1	0.1	0	0.8	0.2	0.2	0.1	
(a)																	
Vulnerable_laborers																	
Construction_fence	False									True							
ETRA_walkable_surface_distance	0-2				2-inf				0-2				2-inf				

ETRA_ skilled_ laborers	False	True	False	True	False	True	False	True
False	0.05	0.15	0.75	0.85	0.75	0.85	0.85	0.95
True	0.95	0.85	0.25	0.15	0.25	0.15	0.15	0.05

(b)

Struck_by_hazard								
Geometric_ spatial_ conflict_ detected	False				True			
	Vulnerable_ laborers		True		False		True	
Falling_ elements	False	True	False	True	False	True	False	True
High	0	0	0	0.1	0.1	0.33	0.33	1
Medium	0	0.1	0.1	0.2	0.2	0.33	0.33	0
Low	1	0.9	0.9	0.7	0.7	0.33	0.33	0

(c)

500 4. Use case

501 The workspace management framework, presented in Section 3.2, has been tested on the management of
502 the construction of a public building (known as Eustachio), which hosts the Faculty of Medicine in the campus
503 of the Polytechnic University of Marche (Figure 6 (a)). This building is located in the town of Ancona (Italy).
504 The building is arranged on six floors above ground, has an area of 16,900 m², and is devoted to classrooms,
505 offices, laboratories, a library, and other faculty-related activities. It dates back to the nineties and comprises
506 two longitudinal blocks, whose longer sides are the main facades, facing north and south.

507 The technical and project documents necessary to develop the BIM model and a resource-constrained work
508 schedule were made available for this study. A 3D view of the resulting BIM model is depicted in Figure 6 (b).
509 The overall work schedule includes works related to the installation of precast elements, like pillars and
510 facades, and the execution of industrial flooring. For simplicity, three crews, one for each work category,
511 have been assumed. Crews composition and productivities have been derived from one of the most complete
512 Italian price lists for public tenders (i.e., the Florence price list), rectified according to data provided by RS
513 Means [100]. Quantities for each work have been computed according to the BIM model. At this point, the
514 duration of each activity is computed by multiplying productivity and quantity. Afterward, the automatic
515 leveling function and a final manual adjustment were executed in Microsoft Project.

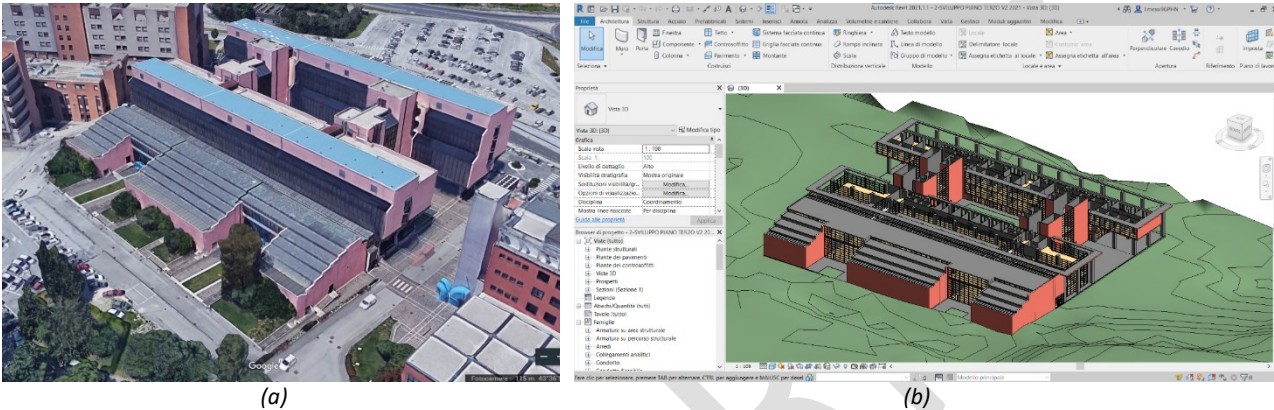
516 This study considered a time span as long as two days (i.e., from May 27th at midnight to May 29th at
517 midnight), highlighted in yellow in Figure 7. During those days, four activities were planned: the installation
518 of pillars and facades on the north wing and the execution of two portions of industrial flooring. Contrarily,
519 a higher number of activities would have implied much more effort to report all the detected conflicts
520 without providing tangible added values. The reason for considering a short simulation interval is twofold.
521 First, detecting spatial conflicts within a longer time frame would require more processing time to identify
522 the issue and related causes. Second, detecting and resolving spatial conflicts scheduled too far into the
523 future could be useless. Since the project schedule is updated frequently, far-away conflicts could be resolved
524 without requiring any intervention.

525 In the simulation scenario presented above, one “direct” and four “indirect” spatial conflicts are expected to
526 be detected. The “direct” spatial conflict is expected to occur between the following activities:

- 527 - “Install 3rd-level north-wing E-alignment pillars” and “Install 3rd-level north-wing north facades”.

528 The “indirect” spatial conflicts are expected to occur between the following activities:

- 529 - “Install 3rd-level north-wing E-alignment pillars” and “Place ground-level north-wing part 3-4
- 530 industrial flooring”.
- 531 - “Install 3rd-level north-wing E-alignment pillars” and “Place ground-level north-wing part 3-4
- 532 industrial flooring”.
- 533 - “Install 3rd-level north-wing north facades” and “Place ground-level north-wing part 4-5 industrial
- 534 flooring”.
- 535 - “Install 3rd-level north-wing north facades” and “Place ground-level north-wing part 4-5 industrial
- 536 flooring”.



537 *Figure 6. Real (a) and BIM (b) view of the Eustachio building, located in Ancona (Italy).*

ID	Task Name	Duration	Start	Finish	24 May '21							
					M	T	W	T	F	S	S	M
6	Install 3rd-level north-wing E-alignment pillars	2 days	Thu 27/05/21	Fri 28/05/21				■	■			
18	Install 3rd-level north-wing north facades	4 days	Tue 25/05/21	Fri 28/05/21	■	■	■	■				
36	Place ground-level north-wing part 3-4 industrial flooring	1 day	Thu 27/05/21	Thu 27/05/21				■				
40	Place ground-level north-wing part 4-5 industrial flooring	1 day	Fri 28/05/21	Fri 28/05/21				■				

538
539 *Figure 7. Excerpt of the overall work schedule reporting the activities scheduled on the selected working days (please use color in*
540 *print).*

541 5. Running the serious gaming tool

542 The developed serious gaming tool (Section 3.4) was regulated by the information model reported in Figure
543 8. The Entity Relationship Diagram (ERD) notation adopted for the model representation makes it possible to
544 express the cardinality of relationships between each pair of entities by the symbols at the ends of the links
545 (e.g., one or many to one or many). The different colors in Figure 8 are referred to different entity domains,
546 such as the BIM model (green), work schedule (blue), main workspaces and spatial conflicts (red), and
547 Bayesian inference (orange).

548

549

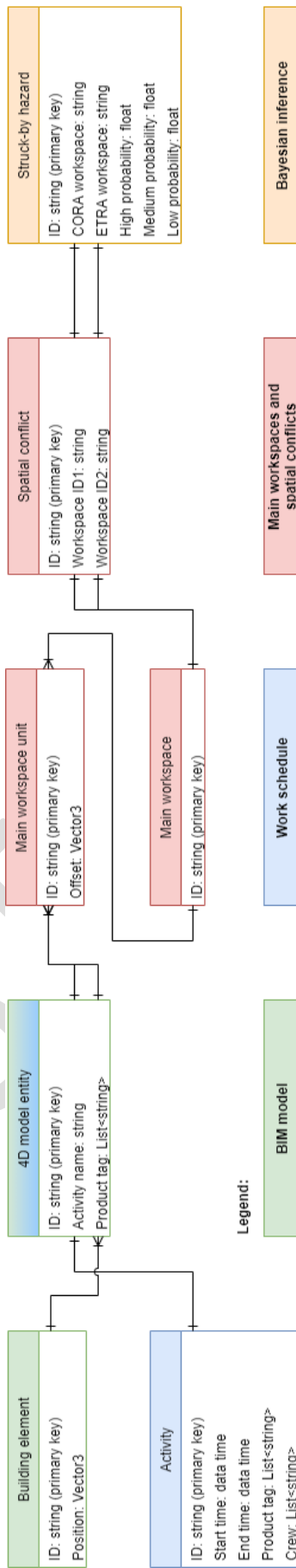
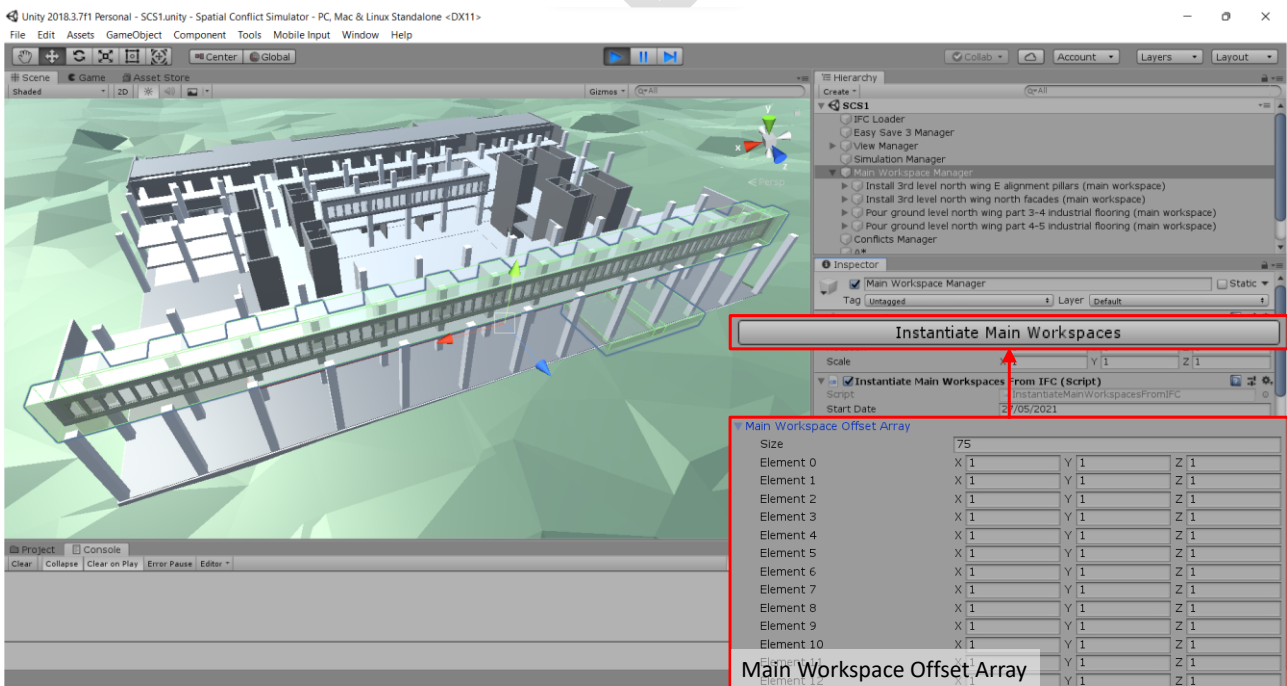


Figure 8. ERD describing the information model that regulates the developed serious gaming tool.

550 **5.1. The spatial conflicts simulator**

551 In the developed simulator, the execution of spatial-temporal analysis starts with the definition of the 4D
 552 BIM model by loading the IFC model of the building assumed as the use case onto Unity3D™ (Section 4) along
 553 with the CSV-formatted work schedule. These simulation steps are enabled by the “File Chooser” and “Model
 554 Input” C# scripts, respectively (Figure 3). In the 4D BIM model, 3D geometric data from the BIM model are
 555 linked to temporal data provided by the work schedule. This is shown by the information model (Figure 8),
 556 where each “4D model entity” corresponds to one activity (i.e., “Activity name”) and includes one or more
 557 produced building elements (i.e., “Product tag”). Each building element, defined by the loaded IFC model, is
 558 represented by the “building element” entity, whereas each activity, defined in the work schedule, is
 559 represented by the “activity” entity (Figure 8).

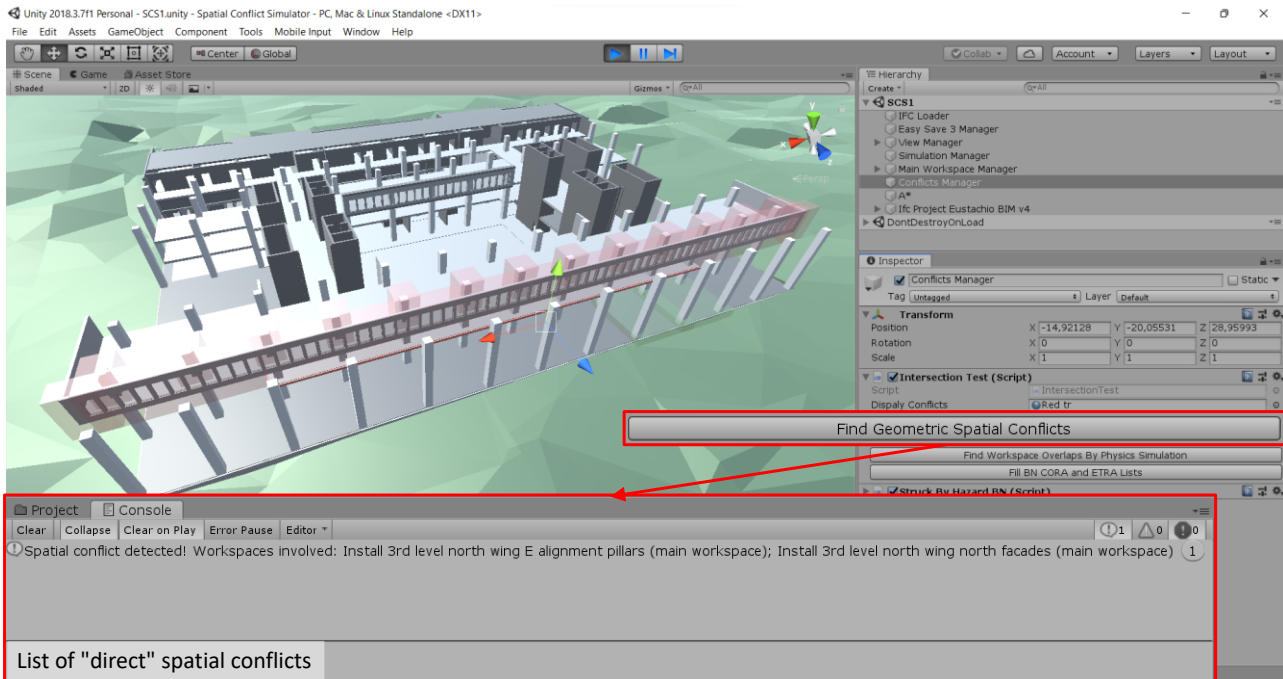
560 At this point, the main workspaces can be generated within Unity3D™. Generating the main workspace for
 561 a given activity (e.g., installing an alignment of pillars) consists of two steps. The first one consists in
 562 generating main workspace units for each one of the building elements (e.g., pillars) associated with the
 563 considered activity. Each main workspace unit is instantiated in the geometric center of the corresponding
 564 building element and obtained by expanding the volume of the considered building element of a given
 565 quantity, defined as “Main Workspace Offset Array”, and set by default as 1 meter (Figure 9). These
 566 parameters can be customized by the user if a bigger or smaller main workspace is required for operational
 567 or safety purposes. According to this, the information model (Figure 8) reports the “Main workspace unit”
 568 entity, including the “Offset” parameter. The second step consists in merging the main workspace units into
 569 a unique main workspace. This is shown by the information model (Figure 8), where the “Main workspace”
 570 entity is defined by merging one or more “Main workspace unit” produced by the considered activity. This
 571 simulation step is executed by clicking on the “Instantiate Main Workspaces” button (Figure 9) implemented
 572 by the “Instantiate main workspace from IFC” C# script (Figure 3).



573
 574 *Figure 9. Main workspaces generated assuming the “Main Workspace Offset Array” values filled by default with the 1-meter offset*
 575 *in all three directions (please use color in print).*

576 Once main workspaces are instantiated, “direct” spatial conflicts can be detected by carrying out geometric
 577 intersection tests among workspaces in their initial static position, inherited from the corresponding building
 578 elements. This simulation step is executed by clicking on the “Find Geometric Spatial Conflict” button (Figure
 579 10) implemented by the “Intersection test” C# script (Figure 3). A spatial conflict is detected between two

580 given workspaces only if their boundaries intersect each other and are assigned to different crews. The
581 developed tool displays a detected spatial conflict by changing the color of the relevant main workspaces
582 from green (Figure 9) to red (Figure 10). In addition, a message reporting the pairs of the conflicting main
583 workspaces is printed in the Unity3D™ console. The proposed tool, as described so far in this section, aims
584 to replicate the last advances in workspace management.



585

586 *Figure 10. "Direct" spatial conflicts detected by geometric intersection tests, triggered by the "Find Geometric Spatial Conflicts"*
587 *button showing conflicts in red and associated message (please use color in print).*

588 As already mentioned, due to the construction site dynamics, "direct" spatial conflicts do not include the
589 totality of spatial issues affecting a construction site. To make an example, main workspaces superimposed
590 at different heights, also if not intersecting each other, can be affected by spatial conflicts. In fact, objects
591 involved in the construction process may fall from the main workspace at higher levels and hit laborers
592 working at lower levels. In order to consider this set of conflict scenarios, the proposed tool can carry out
593 physical simulations of main workspaces and detect related spatial conflicts. These spatial conflicts are
594 labeled as "indirect", meaning that they cannot be directly detected simply by conducting a geometric
595 intersection test among workspaces in their initial static position. On the contrary, virtual physics simulations
596 must be executed to consider "possible" future workspace configurations. In practice, each game object
597 representing a main workspace is let fall down, according to the gravity law, to check if it hits, during the fall,
598 any other main workspace(s) below assigned to another crew. The probability of "indirect" spatial conflicts
599 that virtually occur must be assessed (Section 5.2) since we cannot determine if they occur in reality. The
600 developed tool displays the detected spatial conflicts by changing the color of the main workspaces involved
601 from green to red (Figure 11). In addition, a message reporting the pairs of the conflicting main workspaces
602 is printed in the Unity3D™ console (Figure 11). This simulation step is executed by clicking on the "Find
603 Workspace Overlaps By Physics Simulation" button (Figure 11) implemented by the "Intersection Test" C#
604 script (Figure 3).

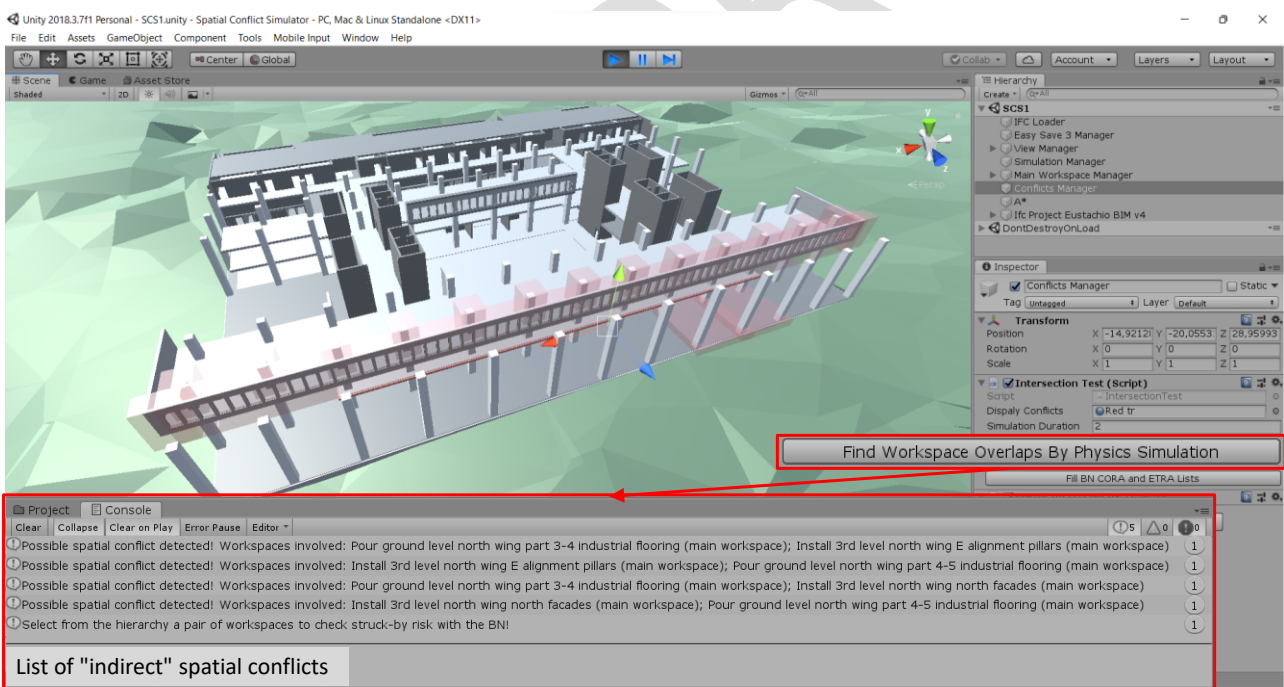
605 In the information model, both "direct" and "indirect" spatial conflicts are represented by the "Spatial
606 conflict" entity, which includes the "Workspace ID1" and "Workspace ID2" parameters, inherited from the
607 conflicting "Main workspace" entities' "ID" (Figure 8).

608 To conclude, the spatial conflict simulator described in this section enables the semi-automatic generation
 609 of main workspaces and the detection of spatial conflicts. In order to quantify how much manual effort is
 610 required from the user, main tasks have been classified into semi-automatic and automatic ones, the latter
 611 requiring, in particular cases, a manual contribution. Semi-automatic tasks are:

- 612 - “Load BIM model”: it loads the BIM model to be made available to the spatial conflicts simulator
 613 within the simulation hub. This is a semi-automatic task because it requires the user to locate the IFC
 614 file to be loaded.
- 615 - “Load work schedule”: it loads the work schedule to be made available to the spatial conflicts
 616 simulator within the simulation hub. This is a semi-automatic task because it requires the user to
 617 locate the CSV file to be loaded.

618 Automatic tasks are:

- 619 - “Instantiate Main Workspace”: it generates main workspaces with standard dimensions according to
 620 the pre-defined value assigned to the “Main Workspace Offset Array” parameter. If the user requires
 621 a different dimension, he/she is asked to manually update the parameter value. Only in this case,
 622 this task becomes a semi-automatic one.
- 623 - “Find Geometric Spatial Conflict”: it detects “direct” spatial conflicts by running automatically
 624 geometric computations.
 625 “Find Workspace Overlaps By Physics Simulation”: it detects “indirect” spatial conflicts by
 626 automatically running physics simulations and geometric computations.



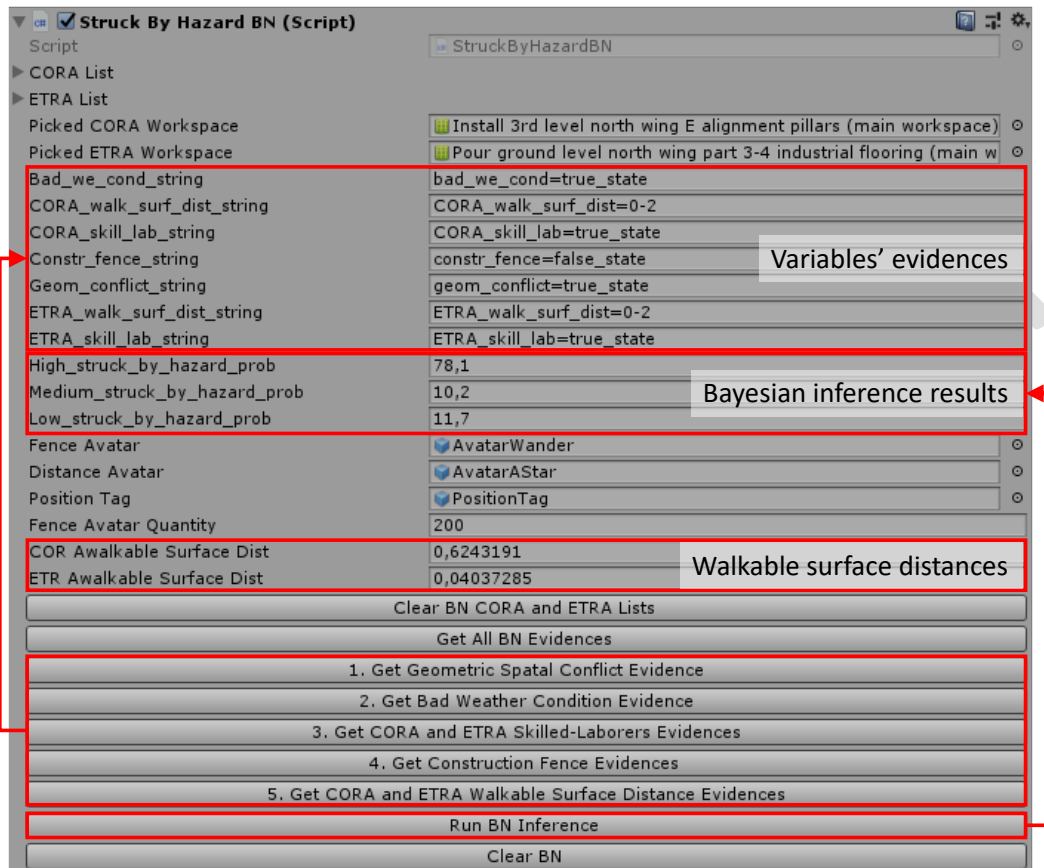
627
 628 *Figure 11. “Indirect” spatial conflicts detected by geometric intersection tests during physics simulations.*

629 5.2. The integrated Bayesian network

630 The criticality of detected “indirect” spatial conflicts, introduced in the previous sub-Section 5.1, is assessed
 631 using the developed struck-by hazard Bayesian network (BN) (Section 3.5). In each “indirect” spatial conflict,
 632 a pair of main workspaces is involved. The one having the highest initial position is the main workspace from
 633 which falling objects may cause struck-by hazards. This workspace, being the source of struck-by hazards,
 634 can be defined as the “Cause-of-Risk Activities” (CORA) workspace. The other one in the pair, placed at the
 635 lowest initial position, is the main workspace where falling objects can hit laborers. This workspace is defined
 636 as the “Exposed-to-Risk Activities” (ETRA) workspace. The information model (Figure 8) maps this

637 classification, including, within the “Struck-by hazard” entity, both the “CORA workspace” and “ETRA
638 workspace” parameters.

639 The developed struck-by hazard BN (Section 3.5) is implemented within Unity3D™ by the “Struck-by hazard
640 BN” C# script (Figure 3). In this way, the results of physical simulations and geometric computations, executed
641 in the serious gaming environment, can automatically feed the states of the BN’s variables. These simulation
642 steps are triggered by clicking on the buttons numbered from “1.” to “5.” in Figure 12.



643

644 Figure 12. Front end of the “Struck By Hazard BN” component after including the BN evidence.

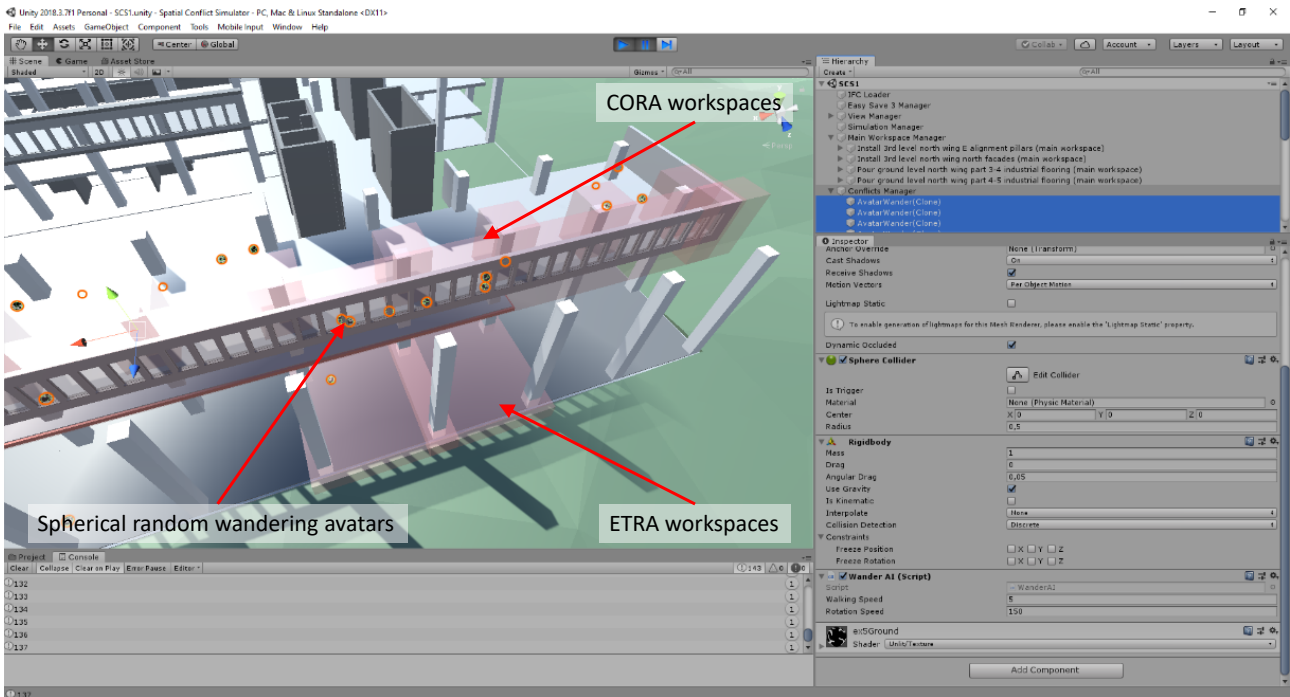
645 If at least one possible spatial conflict has been detected by physical simulations, the “Geom_confl_string”
646 variable state will be set to “true”; otherwise, “false” (Figure 12).

647 The “Bad_we_cond_string” variable state will be filled as “true” if bad weather conditions are expected
648 according to the weather forecast; otherwise “false” (Figure 12). This functionality was implemented using
649 the commercial Real-time Weather tool for Unity3D™ [101].

650 The “CORA_skil_lab_string” and “ETRA_skil_lab_string” variables states will be filled with a “true” or “false”
651 state if the majority of the laborers constituting the crew are skilled or not (Figure 12). This information is
652 obtained from the crews’ information from the resource-constrained work schedule.

653 The “Constr_fence_string” variable state will be filled with a “true” state if any barrier that can protect the
654 laborers at the lower workspace (i.e., ETRA workspace) from falling objects exists (Figure 12). For this
655 purpose, avatars are instantiated in random positions within the higher workspace (i.e., CORA workspace).
656 They are able to wander and check if they can fall down or not (Figure 13). These avatars are defined in
657 Unity3D™ as spheres having the same physical properties (e.g., mass, drag, etc.) as objects involved in the
658 construction process. If they hit a thin plastic sheeting placed as a barrier against dust, they will break through
659 it; otherwise, they will be blocked if they hit a barrier made of bricks or concrete. So, if none of the
660 instantiated avatars hit the lower workspace (e.g., ETRA workspace), the serious gaming tool deduces the

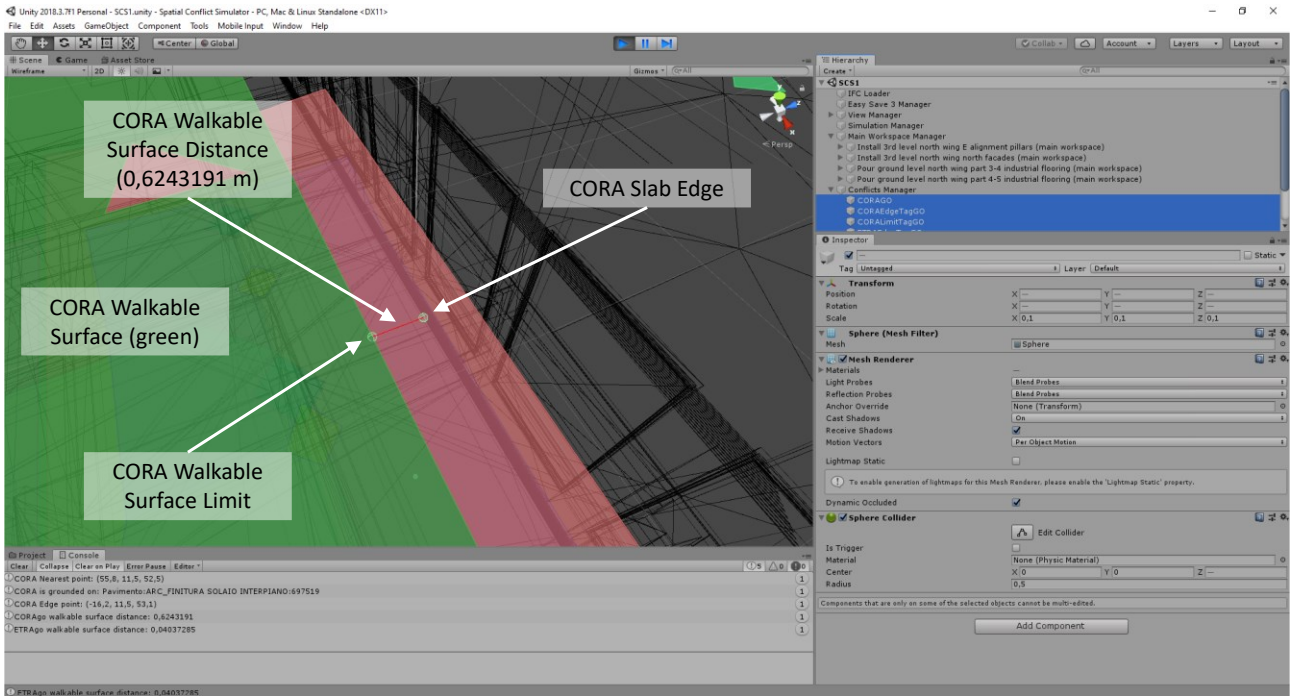
661 presence of a barrier that protects the ETRA workspace and the “Constr_fence_string” variable state is set
662 as “true”, otherwise “false” (Figure 12).



663

664 *Figure 13. Instantiation of spherical random wandering avatars for checking the presence of any barrier protecting ETRA*
665 *workspaces.*

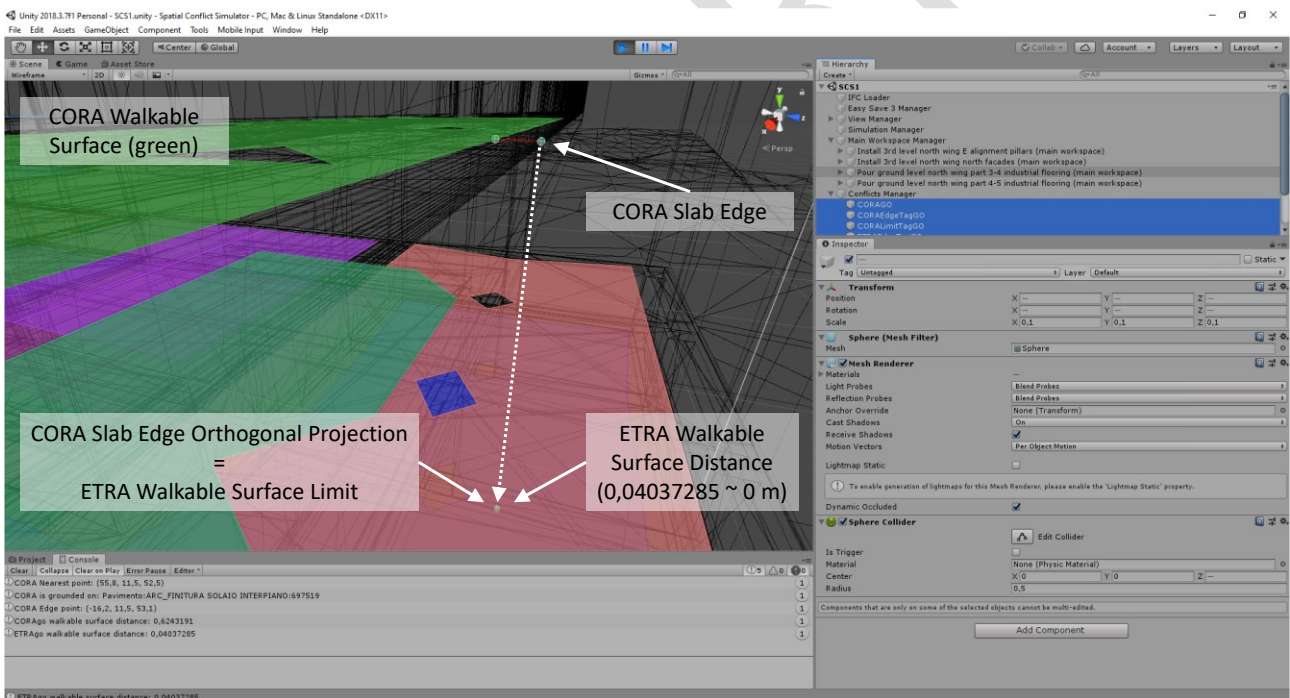
666 Finally, the “CORAwalk_surf_dist_string” and “ETRAwalk_surf_dist_string” variables states will be filled
667 with “0-2” or “2-inf”. The first state means that the walkable surface limit is closer than 2 meters from the
668 edge of the higher walkable element, whereas the second is farther than 2 meters (Figure 12). The distance
669 between the walkable surface’s limit and the slab edge was determined using geometric computations using
670 the Recast graph provided by the A* Pathfinding tool for Unity3D™ [102]. Generating a Recast graph means
671 voxelizing the world, that is, constructing an approximation of the world out of many boxes. The walkable
672 surfaces are automatically peeled off from the regions by tracing the boundaries and then simplifying them.
673 In Figure 14, the green area is the walkable surface on the slab where the CORA workspace is placed. In the
674 same Figure 14, the automatic computation of the “CORAwalkable Surface Distance” is depicted. This
675 distance is computed as the distance between the walkable limit on the CORA slab (i.e., “CORAwalkable
676 Surface Limit”) and the edge of the CORA slab (i.e., “CORASlab Edge”). In Figure 15, the pink area represents
677 the walkable surface on the slab where the ETRA workspace is placed. In the same Figure 15, the automatic
678 computation of the “ETRAwalkable Surface Distance” is depicted. This distance is computed as the distance
679 between the walkable limit on the ETRA slab (i.e., “ETRAwalkable Surface Limit”) and the orthogonal
680 projection of the “CORASlab Edge” on it (i.e., “CORASlab Edge Orthogonal Projection”). The distances
681 computed within Unity3D™ are reported in Figure 14 and Figure 15.



682

683

Figure 14. Automatic geometric computation of the “CORA Walkable Surface Distance” made by the serious gaming tool.



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Figure 15. Automatic geometric computation of the “ETRA Walkable Surface Distance” made by the serious gaming tool.

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Once evidence for all variables is obtained, the Bayesian inference is triggered by clicking on the “Run BN Inference” button. As a result, the probability values for all the three states of the “Struck-by hazard” variable, namely “High_struck_by_hazard_prob”, “Medium_struck_by_hazard_prob”, and “Low_struck_by_hazard_prob” are provided (Figure 12). In Figure 12, the higher value is computed for the “High_struck_by_hazard_prob” (i.e., 78%), indicating that, given the states of the variable, the corresponding scenario can be effectively considered critical. Therefore, the construction management team can benefit from the contribution given by this decision support system (DSS) during the refinement process of the work schedule.

694 **5.3. Implementation and comparison of the proposed tool**

695 In order to prove its added value, the developed spatial conflict simulator (Sections 3 and 5) must be
 696 compared with existing approaches. For this purpose, an overview of prototype tools proposed by existing
 697 studies and commercial applications is shown in Table 3. Table 3 classifies spatial analysis tools into two
 698 macro-categories of detection methods, namely component-level and workspace-level. Whereas in the first
 699 category spatial conflicts are detected with reference to building components, the second one relies on the
 700 workspace concept. The workspace-level category includes five sub-categories adapted from [2] with the
 701 exception of the last one: topographical, approximate, static-geometrical, dynamic-geometrical, and
 702 combined physics-geometric simulation-based. The workspace-level topographical detection method
 703 defines GIS-based spatial analysis. Whereas the approximate one detects spatial conflicts among workspaces
 704 by applying simplified methods, the static- and dynamic-geometrical ones are based on pure geometrical
 705 intersection tests. The latter sub-category takes into account workspaces' dynamics too. Finally, in the
 706 combined physics-geometric simulation-based approach, geometrical intersection tests are combined with
 707 physics simulations. In Table 3, tools marked with the 4D paradigm combine the spatial analysis functionality
 708 with the temporal one.

709 *Table 3. Overview of the detection methods adopted by past studies and commercial software tools.*

Detection method	Tool	Description
Component-level	Autodesk Navisworks [13]	A 4D BIM commercial construction management tool by Autodesk. Clash detection among building elements is natively implemented.
	Solibri Model Checker [103]	A BIM commercial model checking tool by Nemetschek. Clash detection among building elements is natively implemented.
	Trimble Connect [104]	A BIM commercial model checking tool by Trimble. Clash detection among building elements is natively implemented.
Workspace-level	Topographical Cai et al., [22]	A 4D GIS-based construction planning tool is proposed. Physical workspace conflicts are checked by the entry-wise product of matrices, each associated with a workspace.
	Approximate Moon et al., 2014 [21]	A 4D BIM workspace conflict visualization system is proposed. Physical workspace conflicts are checked for parallel activities using spatial 3D distance calculation.
	Static-geometrical Kassem et al., 2015 [5]	A 4D BIM IFC-compliant tool for workspace management is proposed. Physical workspace conflicts are checked for parallel activities using the axis-aligned bounding box (AABB) intersection test algorithm.

	Ma et al., 2020 [3]	A 4D BIM workspace management tool is proposed. Physical workspace conflicts are checked by a hybrid AABB and orientational bounding box (OBB) algorithm.
Dynamic-geometrical	Akinci et al., 2002 [17]	A 4D CAD workspace management tool (4D TSConAn) is proposed. Physical workspace conflicts are checked by combining basic 3D geometric clash detection algorithms with discrete event-simulation mechanisms.
	Dawood et al., 2006 [12]	A 4D CAD workspace management tool (PECASO) is proposed. Physical workspace conflicts are checked by Critical Space-time Analysis (CSA) and dynamic Execution Patterns (EP).
	Mirzaei et al., 2018 [1]	A 4D BIM dynamic conflict detection and quantification system is proposed. Physical workspace conflicts are checked for parallel activities using the AABB intersection test algorithm. The dynamic detection of conflicts is performed considering the labor movements in the workspace.
	Synchro 4D [14]	A 4D BIM commercial construction management tool by Bentley Systems. Workspace entities are natively implemented for the detection of spatial conflicts. An animation editor that simulates the construction site dynamics based on the user's inputs is natively implemented.
Combined physics-geometric-simulation-based	Proposed tool (reported in this paper)	A 4D BIM workspace management tool is proposed in this study. Physical workspace conflicts are checked by combining geometric computations and agent-based physics simulations. An integrated Bayesian reasoner enables to filter non-critical scenarios.

710

711 A tool from each one of the two detection methods macro-categories reported in Table 3, namely
712 component-level and workspace-level, has been selected as a benchmark to be compared with the
713 developed spatial conflicts simulator (referred to as the "Enhanced" approach). In particular, the "Navisworks
714 Benchmark" identifies the one based on the commercial 4D BIM software Autodesk Navisworks, whereas the
715 "Synchro Benchmark" approach identifies the one based on the application of the commercial 4D BIM
716 software Synchro 4D. Four experiments have been carried out considering the use case described in Section
717 4 and a time window as long as two working days (i.e., May 27th and 28th), highlighted in yellow in Figure 7
718 (Table 4). The "Navisworks Benchmark" and "Synchro Benchmark" approaches have been tested on the
719 Standard BIM model (i.e., experiments no. 1 and 2 in Table 4). The "Enhanced" approach was tested both on
720 the "Standard" and "Modified" BIM model (i.e., experiments no. 3 and 4 in Table 4). Further details are
721 provided in sub-Sections 5.4, 5.5, and 5.6.

722 Table 4 shows the functionalities implemented by the considered tools. In the "Navisworks Benchmark"
723 approach, Autodesk Navisworks enables loading the BIM model and construction schedule and carrying out
724 geometric intersection tests. In the "Synchro Benchmark" approach, Synchro 4D allows the manual definition

725 of main workspaces. Finally, in the “Enhanced” approach, the proposed tool enables the execution of physics
 726 simulations and Bayesian inference.

727 *Table 4. Overview of the main differences between the four experiments.*

Experiment No.	Approach	Construction schedule	BIM model	Tool functionalities				
				Loading BIM model and construction schedule	Generating main workspaces	Carrying out geometric intersection tests	Carrying out physics simulations	Running Bayesian network
1	Navisworks Benchmark	May 27 th and 28 th	Standard					
2	Synchro Benchmark							
3	Enhanced (proposed tool)							
4	Enhanced (proposed tool)		Modified					

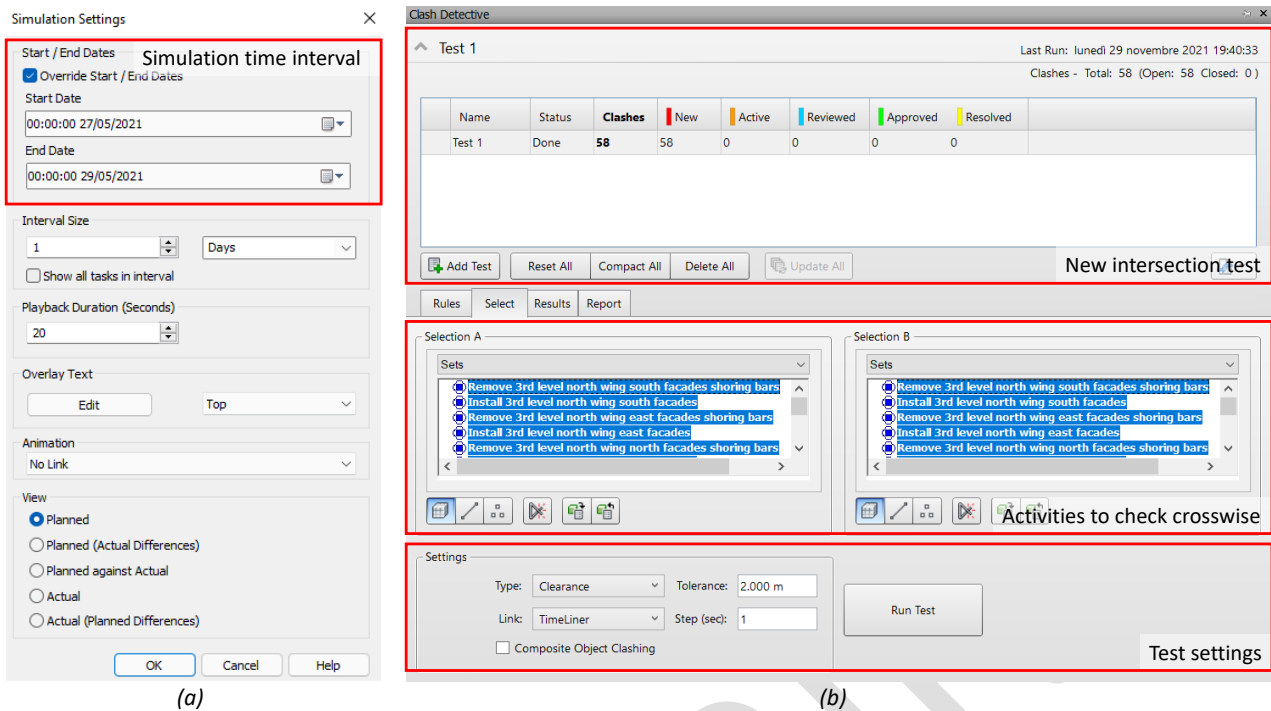
728 **5.4. The “Navisworks Benchmark” approach**

729 Experiment no. 1 was carried out by applying the “Navisworks Benchmark” approach, corresponding to the
 730 one applied by professionals to detect spatial conflicts using Autodesk Navisworks.

731 First, the IFC model of the use case presented in Section 4 was loaded within Autodesk Navisworks. Then, the
 732 work schedule was imported in CSV format by clicking on the “Add” button under the “Data Sources” tab of
 733 the TimeLiner.

734 In order to simulate the same working days chosen for the use case (Section 4), the following time interval
 735 has been selected in the “Simulate” tab of the TimeLiner: from May 27th at midnight until May 29th at
 736 midnight (Figure 16 (a)).

737 In the Clash Detective window, a new test was added by selecting all the available sets (each set corresponds
 738 to an activity in the schedule) both in “Selection A” and “Selection B”. This enabled to check for conflicts by
 739 considering all the possible pairs of sets (i.e., activities) (Figure 16 (b)). Then, a “Clearance” type with 2 meters
 740 “Tolerance” was set to apply the equivalent offset value of 1 meter used as the default value in the serious
 741 gaming tool (Section 5.1). A “Clearance” clash, in Navisworks, was defined as the one in which “the geometry
 742 of Selection A may or may not intersect that of Selection B, but comes within a distance of less than the set
 743 tolerance” [105]. On the contrary, in the developed serious gaming tool, the offset was applied to the border
 744 of each element. Finally, the TimeLiner “Link” was selected to carry out a spatial-temporal analysis within the
 745 TimeLiner interval set above (Figure 16 (b)). Finally, the test was launched by clicking on the “Run Test”
 746 button. The outcome is shown in Figure 16 (b).



747 *Figure 16. Setting the “Simulation Settings” (a) and the “Clash Detective” (b) parameters within Autodesk Navisworks.*

748 **5.5. The “Synchro Benchmark” approach**

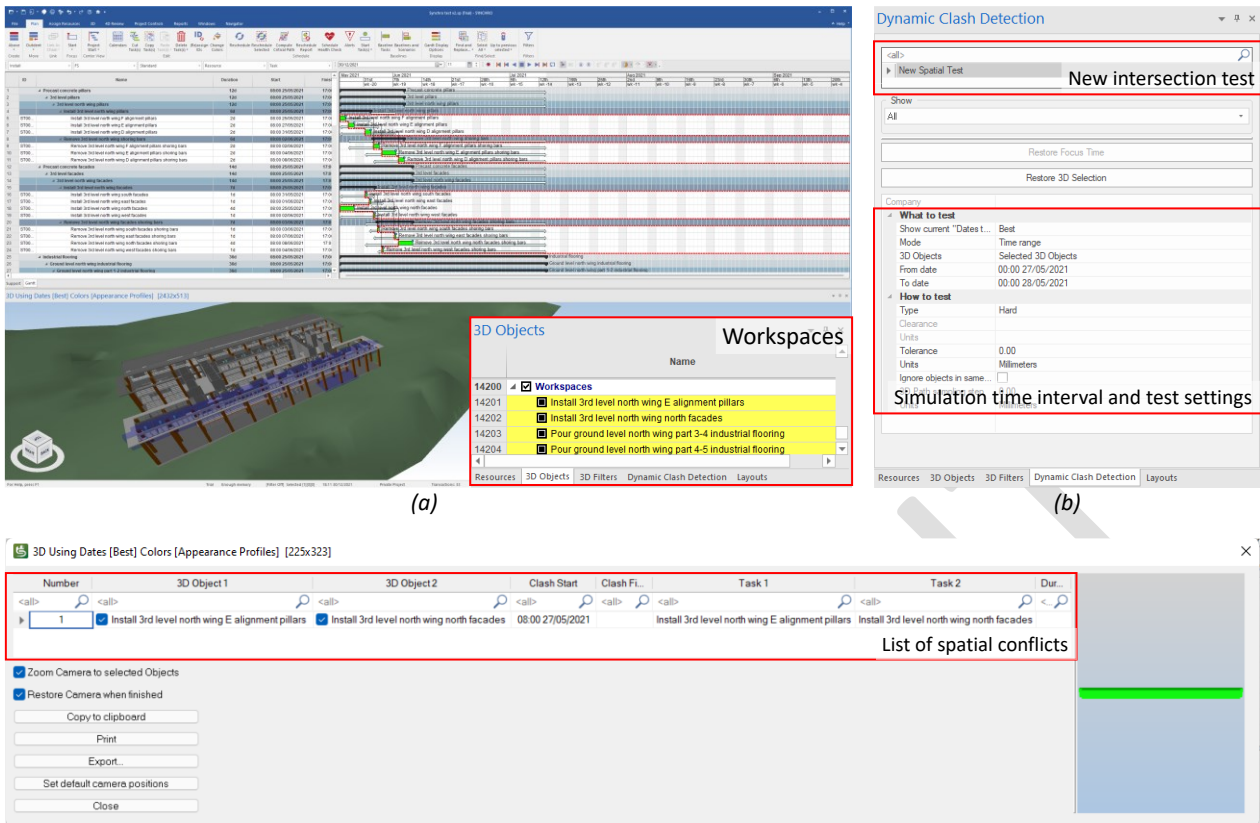
749 Experiment no. 2 has been carried out by applying the “Synchro Benchmark” approach, corresponding to the
 750 one applied by professionals to detect spatial conflicts using Synchro 4D.

751 First, the IFC model of the use case, presented in Section 4, was loaded within Synchro 4D. Then, the work
 752 schedule was imported in XML format by clicking on the “Import” button under the “File” section in the main
 753 window.

754 Then workspaces were generated (Figure 17 (a)), for each scheduled activity (Figure 7), by setting an offset
 755 equal to 1 m, as described in Section 5.1. This task has been fulfilled by selecting the building elements
 756 produced by each activity and clicking on the “Bounding Box” button of the “Create Workspace” function,
 757 located under the “3D” tab.

758 In the “Dynamic Clash Detection” window, a new “New Spatial Test” was added (Figure 17 (b)). In the same
 759 window, in order to simulate the same working days chosen for the use case (Section 4), the “Time range”
 760 option was selected, and the following time interval was set: from May 27th at midnight until May 29th
 761 at midnight (Figure 17 (b)). Then, an “Hard” clash type test that looks for elements overlapping by more than a
 762 specified “Tolerance” distance equal to 0 mm was selected.

763 Finally, the generated workspaces were selected in the “3D Objects” window (Figure 17 (a)), and the spatial-
 764 temporal analysis was run by clicking on the “Run Test” function related to the set “New Spatial Test”. The
 765 obtained results are shown in Figure 17 (c).

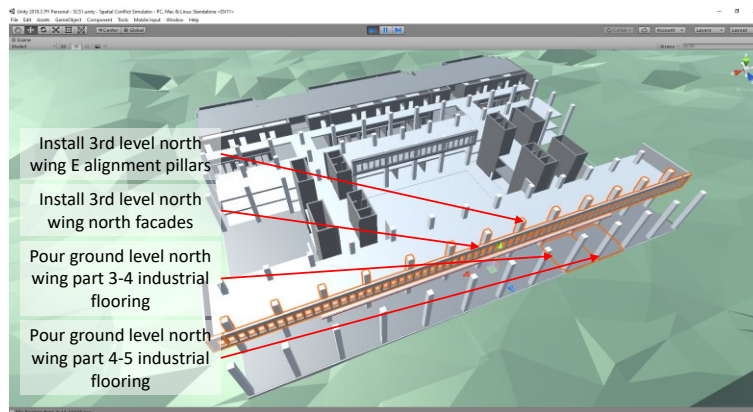


766 Figure 17. Generating workspaces (a) and setting “Dynamic Clash Detection” parameters (b) to detect spatial conflicts within
 767 Synchro 4D (c).

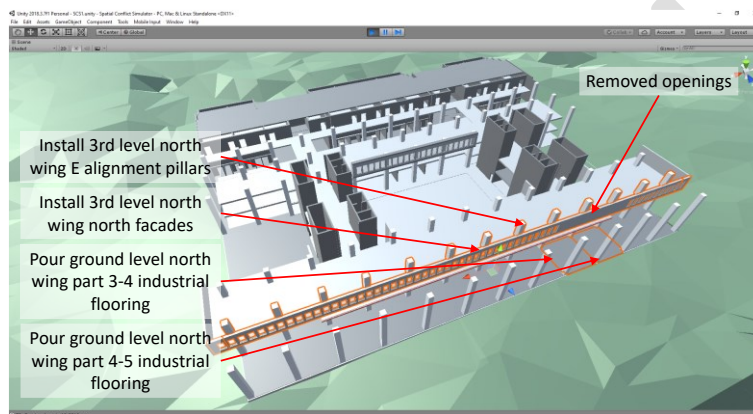
768 5.6. The “Enhanced” approach

769 Experiments no. 3 and 4 were carried out with reference to the use case and working days presented in
 770 Section 4 by executing the simulation steps described in Section 5.1. As a result, “direct” and “indirect” spatial
 771 conflicts were identified. Then, the criticality levels of the latter category were computed by running the
 772 struck-by hazards Bayesian network (BN) (Section 5.2).

773 In order to stress the contribution given by the Bayesian inference, the spatial conflict simulator was first
 774 tested on the “Standard” BIM model of the use case (Figure 18 (a)) and then on the “Modified” BIM model
 775 (Figure 18 (b)). The latter was obtained by removing some of the openings on the 3rd level north façade to
 776 give it the function of a construction fence that can protect laborers below from likely falling objects. The aim
 777 of this scenario was to demonstrate that the struck-by hazard BN can automatically catch this information
 778 from the serious gaming environment and fire the “Construction_fence” variable’s evidence accordingly.
 779 Therefore, a different criticality level than in the Enhanced scenario has been provided.



(a)



(b)

780

Figure 18. Views of the “Standard” (a) and “Modified” (b) BIM models.

781

6. Results and discussion

782

This section summarizes the results from the implementation and comparison of the proposed tool (i.e., the “Enhanced” approach) with two benchmarks, namely “Navisworks Benchmark” and “Synchro Benchmark” (Table 7). Before going into details of these data, an overview of the main differences among each approach is provided as follows:

786

- The main differences between the “Enhanced” and the “Navisworks Benchmark” approaches are:
 - The “Enhanced” approach provides not only the “direct” spatial conflicts, like the “Navisworks Benchmark” one does, but also the “indirect” ones.
 - The “Enhanced” approach also computes the criticality levels of the “indirect” conflicts.
 - The “Navisworks Benchmark” approach, contrarily to the “Enhanced” one, cannot generate workspaces.
 - The “Navisworks Benchmark” approach, contrarily to the “Enhanced” one, looking for building elements closer than a given threshold instead of intersecting workspaces, detects a high percentage of “false positives”.
- The main differences between the “Enhanced” and the “Synchro Benchmark” approaches are:
 - The “Enhanced” approach provides not only the “direct” spatial conflicts, like the “Synchro Benchmark” one does, but also the “indirect” ones.
 - The “Enhanced” approach also computes the criticality levels of the “indirect” conflicts.
- The main differences between the “Navisworks Benchmark” and the “Synchro Benchmark” approaches are:

800

- 801 ○ The “Navisworks Benchmark” approach, contrary to the “Synchro” one, cannot generate
802 workspaces.
- 803 ○ The “Navisworks Benchmark” approach, contrarily to the “Synchro” one, looking for building
804 elements closer than a given threshold instead of intersecting workspaces, detects a high
805 percentage of “false positives”.

806 The spatial-temporal analysis carried out according to the “Navisworks Benchmark” approach (i.e.,
807 experiment no. 1 described in Section 5.4) detected 58 spatial conflicts (Figure 16 (b), Table 7), whereas the
808 “Synchro Benchmark” approach (i.e., experiment no. 2 described in Section 5.5) detected 1 spatial conflict
809 (Figure 17 (c), Table 7).

810 The spatial-temporal analysis carried out according to the “Enhanced” approach detected 1 “direct” and 4
811 “indirect” spatial conflicts for both the “Standard” and “Modified” BIM models (i.e., experiments no. 3 and 4
812 in Section 5.6). In Table 7, the last column reports the criticality levels of the struck-by hazard BN for each
813 “indirect” spatial conflict. As far as the “Standard” model is considered (i.e., experiment no. 3), the Bayesian
814 inference provides a “high” criticality level. Table 5 summarizes the results of the Bayesian inference for the
815 “Enhanced” approach, considering the “Standard” and the “Modified” BIM models. As reported in Table 5,
816 the “high” state of the “Struck_by_hazard” variable has the highest probability value for each “indirect”
817 spatial conflict (e.g., 78%). When the “Modified” BIM model is considered, the Bayesian inference provides
818 a “low” criticality level. As reported in Table 5, the “low” state of the “Struck_by_hazard” variable has the
819 highest probability value for each “indirect” spatial conflict (e.g., 57%). The results of the “Enhanced”
820 approach resulted from considering a time span of as long as two days, in which four activities were planned
821 (Section 4). Average simulation times for automatic tasks that process the four activities in one step are
822 reported in Table 6. These data are obtained using a laptop equipped with an Intel® Core™ i7-8750H CPU
823 2.20 GHz processor, 16 GB of RAM, and an NVIDIA GeForce GTX 1050. Unity 2018.3.7f1 [106] is the release
824 adopted for developing the proposed tool. Scaling up the longer average simulation time (i.e., 10 seconds)
825 to one hundred activities, even if a linear progression has not been demonstrated, would result in 250
826 seconds. In the “Navisworks Benchmark” approach (i.e., experiment no. 1), only 15 out of 58 spatial conflicts
827 (i.e., with ID from N.44 to N.58 in Table 7) are actual spatial conflicts and correspond to the “direct” spatial
828 conflicts detected by “Enhanced” approach (i.e., with E.1 in Table 7). Hence, only about 25% of the detected
829 spatial conflicts are “true positive”. More spatial conflicts in the “Navisworks Benchmark” approach
830 correspond to anyone in the “Enhanced” approach. This occurs because workspaces are not considered in
831 the first case, and a spatial conflict is detected when two building elements are closer than a given minimum
832 threshold, called “tolerance value”. The rest of the spatial conflicts (i.e., with ID from N.1 to N.43 in Table 7),
833 corresponding to about 75% of the total, are “false positive”. This shows that the “Navisworks Benchmark”
834 approach overestimates the results. In the “Navisworks Benchmark” approach, any building element closer
835 than the given threshold to any other building element is detected as a conflict. Hence, although Autodesk
836 Navisworks can effectively check clashes between building elements, it cannot properly be applied for
837 checking spatial interferences between activities’ workspaces.

838 In the “Synchro Benchmark” approach (i.e., experiment no. 2), only a spatial conflict (i.e., with IDs S.1 in Table
839 7) corresponding to the “direct” spatial conflict “Enhanced” approach (i.e., with E.1 in Table 7) was detected.
840 The “Enhanced” approach (i.e., experiments no. 3 and 4) detected 4 additional “indirect” spatial conflicts by
841 integrating physics simulations and geometric computations. The “Enhanced” approach can apply Bayesian
842 inference to consider the related criticality level for those conflicts. In the case of the “Standard” BIM model
843 (i.e., experiment no. 3), the “high” state of the “Struck_by_hazard” variable has the highest probability value
844 for each “indirect” spatial conflict (e.g., 78%). Therefore, according to the proposed workspace management
845 framework (Section 3.2), the construction management team must adjust the work schedule to resolve the
846 5 detected spatial conflicts having IDs from E.1 to E.5 (Table 7). On the contrary, in the case in which the
847 “Modified” BIM model is considered, the “low” state of the “Struck_by_hazard” variable has the highest

848 probability value for each “indirect” spatial conflict (e.g., 57%). This means that the construction
 849 management team must adjust the work schedule to resolve only the “direct” spatial conflict having E.1 as
 850 ID (Table 7). Finally, even if the tools proposed by existing studies have not been replicated in the current
 851 research, some considerations can be moved forward. Testing tools from previous studies on the use case
 852 presented in Section 4 would have provided very similar results to the ones provided by the “Synchro
 853 Benchmark” approach. This can be stated for the following reasons:

- 854 - Tools from existing studies, like in the “Synchro Benchmark” approach but differently from the
 855 “Navisworks Benchmark” one, implement the workspace concept. In fact, several workspaces and
 856 conflicts taxonomies exist in the literature (Sections 2.1 and 2.2).
- 857 - Tools from existing studies, like in the “Synchro Benchmark” approach but differently from the
 858 “Enhanced” one, detect spatial conflicts by carrying out only geometric intersection tests (Section
 859 2.1). To the authors’ knowledge, no other tool exists in the literature that carries out physics
 860 simulations to detect spatial conflicts.

861 Hence, tools from existing studies would have detected, for the use case presented in Section 4, the same
 862 “direct” spatial conflict detected by the “Synchro Benchmark” approach (Table 7).

863 *Table 5. Bayesian inference results for the “Enhanced” approach, considering the “Standard” and the “Modified” BIM models.*

Variable	Variables states for each "indirect" spatial conflict				Variables states for each "indirect" spatial conflict			
	Experiment no. 3				Experiment no. 4			
	E.2	E.3	E.4	E.5	E.6	E.7	E.8	E.9
Bad_weather_condition	True	True	True	True	True	True	True	True
CORA_walkable_surface_distance	0-2	0-2	0-2	0-2	0-2	0-2	0-2	0-2
CORA_skilled_laborers	True	True	True	True	True	True	True	True
Construction_fence	False	False	False	False	True	True	True	True
Geometric_spatial_conflict_detected	True	True	True	True	True	True	True	True
ETRA_walkable_surface_distance	0-2	0-2	0-2	0-2	0-2	0-2	0-2	0-2
ETRA_skilled_laborers	True	True	True	True	True	True	True	True
Struck_by_hazard	High	78%	78%	78%	78%	19%	19%	19%
	Medium	10%	10%	10%	10%	23%	23%	23%
	Low	11%	11%	11%	11%	57%	57%	57%

864
 865 *Table 6. Average simulation time for the main automatic tasks.*

Automatic task name	Average simulation time [s]
“Instantiate Main Workspace”	1
“Find Geometric Spatial Conflict”	< 1
“Find Workspace Overlaps By Physics Simulation”	10

866 7. Conclusions and outlook

867 Much effort has been spent to date by researchers in workspace management. As reported in Section 2, the
 868 main gaps existing in the literature point out the need to consider the construction site dynamics and filter
 869 non-critical scenarios among pure geometric spatial conflicts.

870 In order to cover these gaps, this study proposes a workspace management framework that integrates the
 871 work scheduling phase with a spatial conflict simulator and a Bayesian reasoner. The simulator and the

872 reasoner have been developed using serious game engine technology (in this case, Unity3D™). Thanks to this
873 technological solution, potential spatial interferences can be detected based on given geometric and
874 semantic information stored in the BIM model and construction process data included in the work schedule.
875 Using game engine technology, geometric and physics simulations can be carried out to anticipate likely
876 future scenarios. Contrarily to the rule-based approach adopted by currently available 4D tools, the proposed
877 spatial conflict simulator, embodying an agent-based approach, can effectively simulate the interaction
878 among involved agents. Hence, in addition to interferences between static workspaces, other “indirect”
879 spatial conflicts (e.g., struck-by hazards) can be detected by simulating the physical behavior of objects
880 moving (or dropping down) within corresponding workspaces, eventually retrieving intersections that could
881 fall outside their volumes. In addition, to avoid overestimations, the criticality levels of “indirect” spatial
882 conflicts are considered by running a BN, whose variables’ states are automatically fed by the simulation data
883 provided by the serious gaming tool (Section 5.2).

884 The proposed approach (i.e., “Enhanced” approach) has been tested on a real use case and compared with
885 two benchmarks referring to the most popular 4D BIM tools, namely Autodesk Navisworks (i.e., “Navisworks
886 Benchmark” approach) and Synchro 4D (i.e., “Synchro Benchmark” approach). The experiments showed that
887 the “Enhanced” approach can accurately detect more spatial conflicts by combining geometric computations
888 and physics simulations and filtering those with low criticality levels. In fact, the “Enhanced” approach
889 detected 1 “direct” and 4 “indirect” spatial conflicts. In the same scenario, the “Navisworks Benchmark”
890 approach detected 58 spatial conflicts, of which only 25% were relevant and corresponded to the “direct”
891 conflict detected by the “Enhanced” approach. The “Synchro Benchmark” approach, instead, detected only
892 1 spatial conflict corresponding to the “direct” one detected by the “Enhanced” approach. This makes the
893 proposed approach relevant for the construction management team in making informed decisions during
894 the refinement process of the work schedule.

895 A limitation of the proposed approach is the fact that spatial conflicts among incompatible workspaces (e.g.,
896 electrical hazards) have not been addressed yet. In addition, further development of the proposed workspace
897 management framework will focus on the refinement process of the work schedule, given the list of detected
898 spatial conflicts. In this regard, future studies will investigate a system able to support managers in minimizing
899 spatial conflicts, providing them with implications for schedule and cost variations.

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905 **Appendix A**

906 Table 7 summarizes the results provided by implementation and comparison of the proposed tool (i.e.,
 907 “Enhanced” approach) with two benchmarks, namely “Navisworks Benchmark” (Section 5.4) and “Synchro
 908 Benchmark” (Section 5.5).

909 *Table 7. Overview of the results from the experiments.*

Experiment no.	Approach	Pairs of element IDs involved in the spatial conflicts detected by only geometric computation		Pairs of element IDs involved in the spatial conflicts detected by physics simulations and geometric computation			Criticality level	
		ID		ID				
1	Navisworks Benchmark	N.1	195809	1226040	n/a	n/a	n/a	n/a
		N.2	195809	1226040	n/a	n/a	n/a	n/a
		N.3	759850	760059	n/a	n/a	n/a	n/a
		N.4	760059	1226040	n/a	n/a	n/a	n/a
		N.5	195927	760059	n/a	n/a	n/a	n/a
		N.6	195927	639149	n/a	n/a	n/a	n/a
		N.7	195821	1224989	n/a	n/a	n/a	n/a
		N.8	195821	1224989	n/a	n/a	n/a	n/a
		N.9	195821	1224989	n/a	n/a	n/a	n/a
		N.10	195821	1224989	n/a	n/a	n/a	n/a
		N.11	760059	1225516	n/a	n/a	n/a	n/a
		N.12	1225516	1225516	n/a	n/a	n/a	n/a
		N.13	195809	760059	n/a	n/a	n/a	n/a
		N.14	1226040	1226040	n/a	n/a	n/a	n/a
		N.15	1227080	1225516	n/a	n/a	n/a	n/a
		N.16	639149	1226040	n/a	n/a	n/a	n/a
		N.17	639149	1227080	n/a	n/a	n/a	n/a
		N.18	639149	760059	n/a	n/a	n/a	n/a
		N.19	1224989	760059	n/a	n/a	n/a	n/a
		N.20	1225516	639149	n/a	n/a	n/a	n/a
		N.21	1225516	1224989	n/a	n/a	n/a	n/a
		N.22	1225516	1226040	n/a	n/a	n/a	n/a
		N.23	759850	1226040	n/a	n/a	n/a	n/a
		N.24	759850	1226040	n/a	n/a	n/a	n/a
		N.25	1225516	760059	n/a	n/a	n/a	n/a
		N.26	195809	760059	n/a	n/a	n/a	n/a
		N.27	195797	1225516	n/a	n/a	n/a	n/a
		N.28	195797	1225516	n/a	n/a	n/a	n/a
		N.29	1225516	1226040	n/a	n/a	n/a	n/a
		N.30	1225516	1226040	n/a	n/a	n/a	n/a
		N.31	1225516	1224989	n/a	n/a	n/a	n/a
		N.32	1225516	1224989	n/a	n/a	n/a	n/a
		N.33	760059	1224989	n/a	n/a	n/a	n/a
		N.34	759850	1224989	n/a	n/a	n/a	n/a
		N.35	759850	639149	n/a	n/a	n/a	n/a

N.36	195797	760059	n/a	n/a	n/a	n/a	
N.37	195797	759850	n/a	n/a	n/a	n/a	
N.38	1227080	1227080	n/a	n/a	n/a	n/a	
N.39	1227080	1227080	n/a	n/a	n/a	n/a	
N.40	1227080	1226040	n/a	n/a	n/a	n/a	
N.41	1227080	1226040	n/a	n/a	n/a	n/a	
N.42	195785	1226040	n/a	n/a	n/a	n/a	
N.43	195785	1226040	n/a	n/a	n/a	n/a	
N.44	213613	1227080	n/a	n/a	n/a	n/a	
N.45	213681	1227080	n/a	n/a	n/a	n/a	
N.46	213565	760059	n/a	n/a	n/a	n/a	
N.47	213649	760059	n/a	n/a	n/a	n/a	
N.48	213589	760059	n/a	n/a	n/a	n/a	
N.49	213601	760059	n/a	n/a	n/a	n/a	
N.50	213553	760059	n/a	n/a	n/a	n/a	
N.51	213541	760059	n/a	n/a	n/a	n/a	
N.52	213541	760059	n/a	n/a	n/a	n/a	
N.53	213661	760059	n/a	n/a	n/a	n/a	
N.54	213577	639149	n/a	n/a	n/a	n/a	
N.55	213683	760059	n/a	n/a	n/a	n/a	
N.56	213625	760059	n/a	n/a	n/a	n/a	
N.57	213637	760059	n/a	n/a	n/a	n/a	
N.58	213661	759850	n/a	n/a	n/a	n/a	
Experiment no.	Approach	Pairs of workspace names involved in the spatial conflicts detected by only geometric computation	ID	Pairs of workspace names involved in the spatial conflicts detected by physics simulations and geometric computation	ID	Criticality level	
2	Synchro Benchmark	Install 3rd-level north-wing E-alignment pillars	Install 3rd-level north-wing north facades	n/a	n/a	n/a	
Experiment no.	Approach	Pairs of workspace names involved in the spatial conflicts detected by only geometric computation	ID	Pairs of workspace names involved in the spatial conflicts detected by physics simulations and geometric computation	ID	Criticality level	
3	Enhanced (proposed tool)	Install 3rd-level north-wing E-alignment pillars	Install 3rd-level north-wing north facades	E.2	Place ground-level north-wing part 3-4 industrial flooring	Install 3rd-level north-wing E-alignment pillars	High (78%)
				E.3	Place ground-level north-wing part 4-5 industrial flooring	Install 3rd-level north-wing E-alignment pillars	High (78%)
				E.4	Place ground-level north-wing part 3-4 industrial flooring	Install 3rd-level north-wing north facades	High (78%)
				E.5	Place ground-level north-wing part 4-5 industrial flooring	Install 3rd-level north-wing north facades	High (78%)

Experiment no.	Approach	Pairs of workspace names involved in the spatial conflicts detected by only geometric computation	ID	Pairs of workspace names involved in the spatial conflicts detected by physics simulations and geometric computation	Criticality level		
4	Enhanced (proposed tool)	Install 3rd-level north-wing E-alignment pillars	Install 3rd-level north-wing north facades	E.6	Place ground-level north-wing part 3-4 industrial flooring	Install 3rd-level north-wing E-alignment pillars	Low (57%)
				E.7	Place ground-level north-wing part 4-5 industrial flooring	Install 3rd-level north-wing E-alignment pillars	Low (57%)
				E.8	Place ground-level north-wing part 3-4 industrial flooring	Install 3rd-level north-wing north facades	Low (57%)
				E.9	Place ground-level north-wing part 4-5 industrial flooring	Install 3rd-level north-wing north facades	Low (57%)

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