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Risk Assessment of Reinforced Concrete Buildings with Rubber Isolation Systems Designed by the Italian Seismic Code

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note finali coverage

(Article begins on next page)

1 **Risk assessment of Reinforced Concrete buildings with Rubber**
2 **Isolation Systems designed by the Italian Seismic Code**

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1 **Risk assessment of Reinforced Concrete buildings with rubber isolation systems designed**
2 **by the Italian Seismic Code**

3 ABSTRACT

4 This paper presents an insight on the seismic response and seismic risk of base-isolated struc-
5 tures performed within the RINTC project, considering different configurations of rubber-based
6 isolation systems. This represents an in-depth revision of past works [*Ragni et al. 2018a, Car-*
7 *done et al. 2019b*] due to the adoption of more robust and accurate isolator model. Four arche-
8 type 6-storeys RC frame buildings are examined, representing both new designed isolated build-
9 ings and existing buildings retrofitted with seismic isolation, differing in age of construction and
10 location (the cities of L'Aquila (central Italy) and Naples (southern Italy)). All the isolation sys-
11 tems are designed in accordance with the current Italian Seismic Code. Seismic performance as-
12 sessment is performed by multi-stripe nonlinear time history analysis. The annual failure rates
13 for two different performance levels, namely Global Collapse and Usability Preventing Dam-
14 age, are computed. The results point out that all isolation systems work effectively in limiting
15 damage while they show a quite low margin with respect to collapse, regardless of the dominant
16 failure mode, which is governed by the more fragile component among isolation system and su-
17 perstructure. The annual failure rates derived for base-isolated buildings are critically reviewed
18 and then compared with those obtained for similar new designed fixed-base RC buildings.

19
20 KEYWORDS

21 Base isolation, high damping rubber bearings, seismic performance, multi-stripe analyses, risk
22 assessment, annual failure rate

23

1

2 **Introduction**

3 In the last decades, the base isolation technique [*Naeim and Kelly, 1999*] has emerged
4 as an attractive strategy for both the seismic design of new buildings and the seismic retrofit of
5 existing buildings. Several numerical studies and the experience derived from recent seismic
6 events have definitely demonstrated the applicability of base isolation for the seismic protection
7 of buildings.

8 So far, only a few studies have focused on the collapse performance of seismically iso-
9 lated structures and, as a consequence, on the assessment of the safety margins against collapse
10 [*Cardone et al. 2019a, Kitayama and Constantinou 2018, Kitayama and Constantinou 2019,*
11 *Shao et al. 2019*]. Among those, the authors of this paper already investigated the seismic per-
12 formances of RC frame buildings equipped with rubber-based isolation systems [*Ragni et al.,*
13 *2018a, Cardone et al., 2019b*], towards two different performance levels (i.e. Global Collapse
14 (GC) and Usability-Preventing Damage (UPD) performance levels), via Multi-Stripe nonlinear
15 dynamic Analyses (MSAs) [*Jalayer, 2003, Scozzese et al., 2020*]. In the mentioned studies, car-
16 ried out within the RINTC (Implicit Risk of code-conforming Italian buildings) research project
17 [*ReLUIIS-RINTC, 2018, Iervolino and Dolce, 2018*], reference to two sites, characterized by dif-
18 ferent seismic hazard (i.e. L'Aquila and Naples), both on soil type C (medium soft soil), has
19 been made. The outcomes have been then used as input for the subsequent evaluation of the rel-
20 evant implicit risk of failure within a probabilistic framework [*Iervolino et al., 2018*].

21 The results presented in [*Ragni et al., 2018a, Cardone et al., 2019b*] outlined that, re-
22 gardless of the characteristics of the superstructure (new or existing, namely retrofitted), the
23 rubber-based isolation systems work effectively in limiting damage in non-structural compo-
24 nents up to seismic intensities much higher than the relevant design earthquake intensity level.
25 As a consequence, the annual failure rates associated with the UPD performance level, observed
26 for base-isolated buildings, are lower than those obtained for fixed-base structures [*Iervolino et*
27 *al., 2018*]. On the other hand, a little margin to collapse (beyond the design earthquake intensity

1 level) has been observed for base-isolated buildings, thus leading to collapse failure rates very
2 similar to (or even greater than) those for fixed-base structures.

3 In the mentioned past studies, the nonlinear 3D models of base-isolated buildings have
4 been implemented in the OpenSees framework [McKenna, 2011] using the *HDR Bearing Ele-*
5 *ment* [Kumar et al., 2014] to describe the cyclic behaviour of rubber isolators. The *HDR Bear-*
6 *ing Element* is characterized by a very advanced horizontal behaviour (in shear) able to capture
7 the first cycle stiffness and the softening behaviour due to repeated cycles; however, it does not
8 account for the post-buckling response characterized by the reduction of the horizontal stiffness
9 due to vertical loads. On the other hand, the *ElastomericX* element (already implemented in
10 Opensees by the same Authors of *HDR Bearing Element*) is based on a simpler shear behaviour
11 and on a simplified method to predict the reduction of the horizontal stiffness due to vertical
12 loads. However, the *ElastomericX* element is specific for low damping rubber bearings and is
13 not able to properly describe the cyclic behaviour of high damping rubber bearings.

14 Recently, a new model for *HDRB* isolators, referred to as *Kikuchi Bearing Element*
15 [Ishii and Kikuchi, 2019], has been proposed and implemented in Opensees. It represents an up-
16 grade of the very preliminary version proposed in [Yamamoto et al., 2009]. The *Kikuchi Bear-*
17 *ing Element* is a two-nodes link element with multi-spring mechanical model which includes
18 two sets of multiple axial springs and a set of mid-height multiple (radial) shear springs. Each
19 radial spring is characterized by the *KikuchiAikenHDR* uniaxial material [Kikuchi and Aiken,
20 1997]. The springs are bound together by rigid links, according to the older *two spring model*
21 formulation [Koh and Kelly, 1988, Koh and Kelly 1986]. The main advantage of the *Kikuchi*
22 *Bearing Element* is represented by the possibility of capturing the axial-shear load interaction
23 for small and large displacements and, as a consequence, the associated pre- and post-buckling
24 behaviour. As a result, the *Kikuchi Bearing Element* model is able to capture the effective hori-
25 zontal stiffness of the isolators as well as its variability due to rocking effects of the superstruc-
26 ture during an earthquake. A synthetic comparison of the two bearing elements is reported in
27 Table 1.

28 *Table 1. Features comparison of the HDR Bearing Element and the Kikuchi Bearing Element*

<i>Features</i>	<i>HDR Bearing Element</i> [Kumar et al. 2014]	<i>Kikuchi Bearing Element</i> [Ishii and Kikuchi, 2019]
Coupled bidirectional horizontal model	✓	✓* (multi-shear spring)
Shear degradation due to Mullins effect	✓	✗
Coupled horizontal-vertical behaviour: Vertical stiffness reduction due to horizontal displacement	✓	✓
Coupled horizontal-vertical motion: horizontal stiffness reduction due to vertical load and horizontal displacement	✗	✓
Cavitation and post-cavitation effects	✓	✓
Cyclic and degrading hysteresis behaviour in cavitation and post-cavitation	✓	✗
Post-buckling behaviour	✗	✓

1

2

A further difference that should be remarked is that the *Kikuchi Bearing Element* has a reduced number of calibration parameters for the horizontal behaviour with respect to *HDR Bearing Element*, thus simplifying the calibration procedure (even if there are some limitation for hardening behaviour calibration).

6

The main novelties of the present study are: (i) the calibration of the *Kikuchi Bearing Element*, based on fitting of experimental data, specifically relevant to commercial devices currently used in Italy; (ii) the performance assessment, via *MSAs* (for both *UPD* and *GC* performance levels), of several case studies of new and existing buildings retrofitted with rubber-based isolation systems, using the *Kikuchi Bearing Element*; (iii) the calculation and critical examination of the corresponding annual failure rates (for both *UPD* and *GC*), (iv) the comparison between new and retrofitted buildings with base isolation, in terms of structural performances and failure rates and (v) the comparison between base-isolated and similar new designed fixed-base RC buildings.

15

Case studies

16

Archetype Buildings

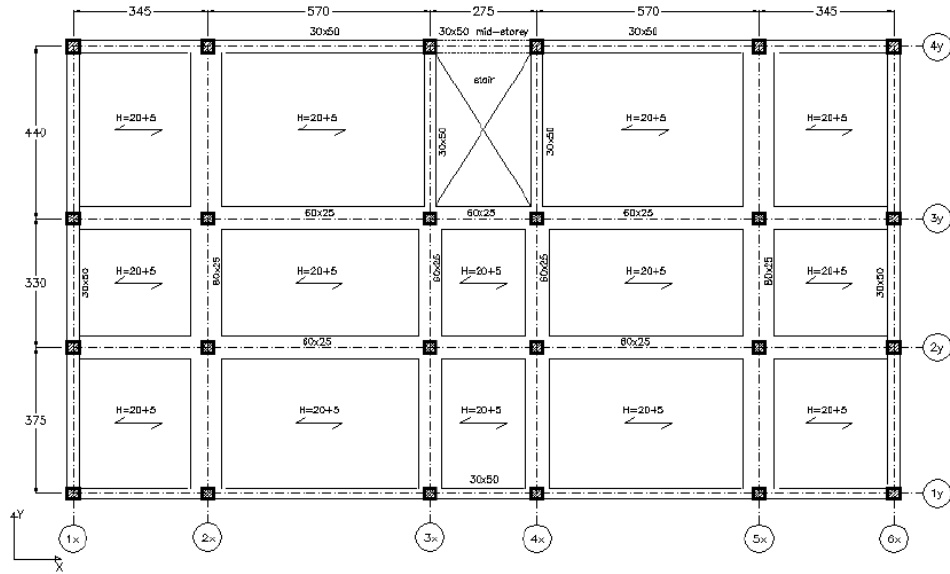
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The examined (new and existing) buildings are located in two different sites (namely, the city of Naples, southern Italy, and the city of L'Aquila, central Italy), characterized by medium and

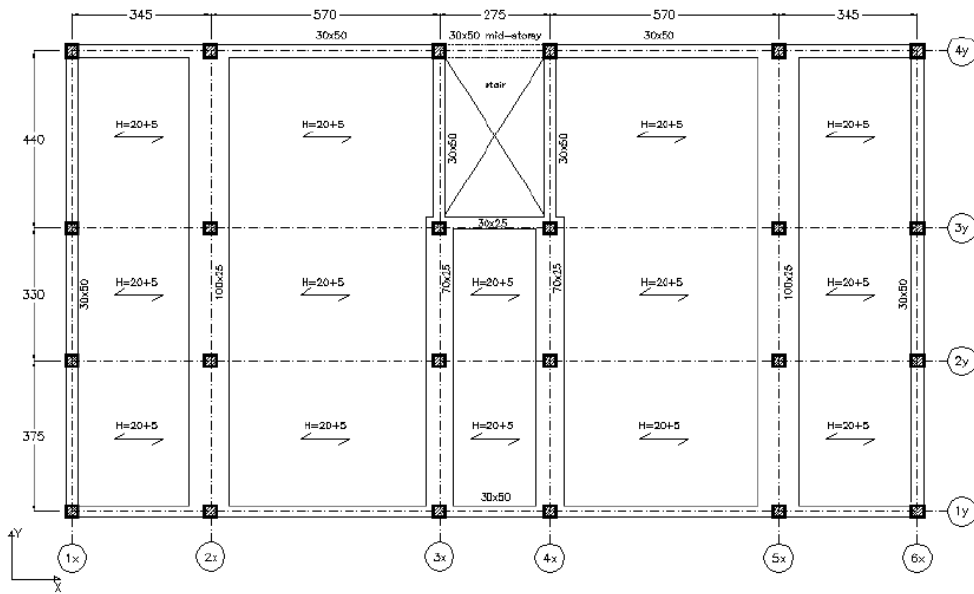
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1 high seismicity for Italy, respectively. All buildings are intended for residential use, featuring a
2 regular plan of approximately 240 square meters and 6 stories above ground. The ground level
3 height is equal to 3.4 m while that of all the other stories is equal to 3.05 m. The building struc-
4 ture includes knee beams staircase. All floor plans are identical except for columns and beams
5 dimensions and reinforcements.

6 The existing buildings have been defined in a previous study [Ricci et al., 2019] by means of
7 simulated design, in accordance with outdated Italian Seismic Codes. In particular, the building
8 located in Naples (labelled as NA_{EX} in what follows) has been designed for gravity loads only
9 (Gravity Loads Design, GLD) according to [D.M. 30/5/1974]; The building located in L'Aquila
10 (labelled as AQ_{EX} in the following), has been defined based on a simulated seismic load design
11 (Seismic Load Designed, SLD), considering low seismic forces, according to past seismic clas-
12 sifications [D.M. 14/2/1992], and outdated technical regulations [D.M. 24/1/1986]. Figure 1
13 shows the typical floor plan of the (a) AQ_{EX} building and (b) NA_{EX} building. In both cases the
14 outer beams are all deeper than the slab, while all internal beams are flat. In the NA_{EX} building,
15 the internal beams are positioned only in the y-direction. All the stories feature the same slab,
16 whose total thickness is equal to 250mm (including hollow bricks). It is worth noting that in the
17 base-isolated configuration, a supplementary floor has been added at the bottom of the first sto-
18 rey columns and a grid of RC beams has been implemented at the same level. According to the
19 technical practice of the period, masonry infills featuring a double layer (120+80 mm thickness)
20 of hollow clay bricks, with 100 mm inner cavity, have been considered. More details about the
21 existing buildings (i.e. cross-section dimensions, reinforcement ratios, material properties etc.)
22 can be found in [Ricci et al., 2019].



(a)



(b)

Figure 1. Floor plan for (a) AQ_{EX} and (b) NA_{EX} existing archetype buildings.

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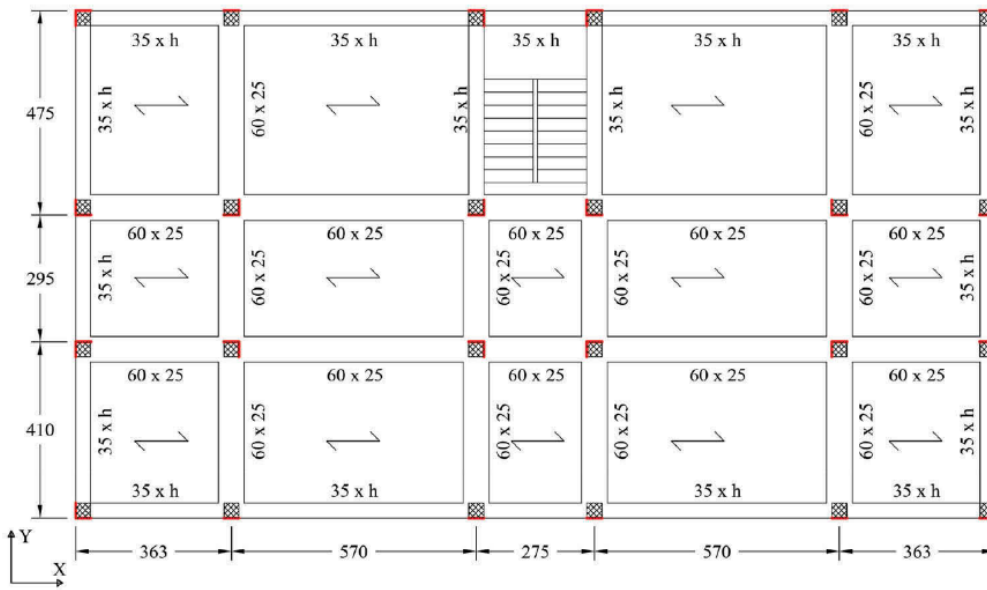
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7 The seismic design of the new base-isolated buildings has been performed based on linear dy-
 8 namic analyses according to the current Italian Seismic Code called *NTC2018* [CS.LL.PP.,
 9 2018] and its explicatory notes [CS.LL.PP., 2019]. The superstructure of the new base-isolated
 10 buildings (AQ_{NEW} and NA_{NEW}) features four frames in the long (X-) direction and six external
 11 frames in the short (Y-) direction (see Figure 2). The masonry walls, realized with a single layer

1 (300 mm thickness) of hollow clay bricks, are regularly distributed in plan and elevation, featur-
 2 ing different percentages of openings. A good connection of the infill panels with the RC frame
 3 has been assumed in the numerical model for the performance assessment. Structural elements'
 4 dimensions and reinforcements have been defined and verified according to the prescriptions
 5 provided by the current version of the Italian Seismic Code [CS.LL.PP., 2018, Chpt. 7.10.4.2].
 6 More details about the structural details and masonry infill characteristics of the new base-
 7 isolated buildings can be found in [Ragni et al., 2018a].



8
 9 *Figure 2. Floor plan for new isolated buildings.*

10 *Seismic Hazard*

11 The hazard model adopted in the present study has been defined based on a preliminary Proba-
 12 bilistic Seismic Hazard Analysis (PSHA) performed using OPENQUAKE [Monelli et al., 2012].
 13 The spectral acceleration, $S_a(T^*)$, associated with a suitable conditioning period, T^* , has been as-
 14 sumed as Intensity Measure (IM) to derive the hazard curves for the building sites. For the sake
 15 of clarity and accuracy, the conditioning period used to define the IM has been chosen as close
 16 as possible to the design value of the effective fundamental period of each base-isolated build-
 17 ing. Hazard curves have been discretized in ten Intensity Measure (IM) levels, corresponding to
 18 the following Return Periods (RPs): 10, 50, 100, 250, 500, 1000, 2500, 5000, 10000 and 100000
 19 years. The first 7 levels (from 1 to 7) correspond to Return Periods values typically adopted by

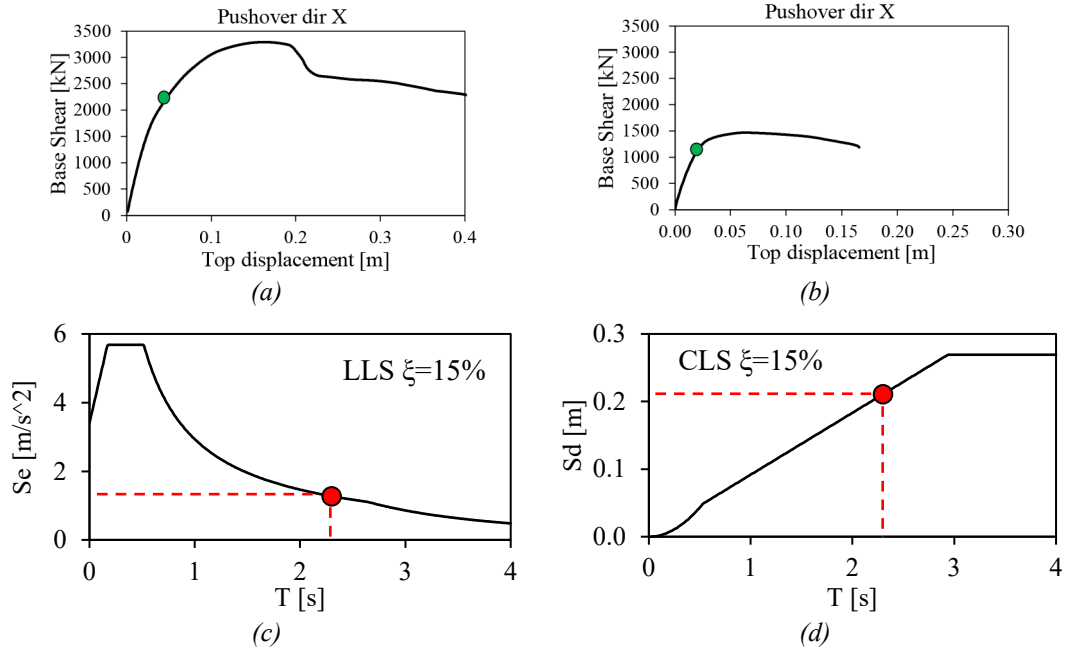
1 the current Italian Seismic Code for site hazard curves. In order to properly assess the safety
2 margins against collapse and estimate an annual exceedance rate down to 10^{-5} , three additional
3 larger hazard levels have been included (corresponding to Return Periods equal to 5000, 10000
4 and 100000 years, respectively) [Iervolino *et al.*, 2018]. Subsequently, the Conditional Spec-
5 trum (CS) method [Lin *et al.* 2013, NIST 2011], combined with a post processing procedure en-
6 suring consistency of selected records with magnitude-distance disaggregation [Spillatura,
7 2018], has been used to select 20 seismic records pairs for each *IM*. All the information about
8 seismic hazard assessment and record selection can be found in [Iervolino *et al.*, 2018] and
9 have been carried out within the *RINTC* project for different building typologies, including the
10 base-isolated buildings under consideration. It is worth noting that, while the Ground-Motion
11 Prediction Equation (*GMPE*) selected for computing the seismic hazard for fixed-base RC
12 buildings (featuring fundamental periods lower than 2.0 s) is that proposed by [Ambraseys *et al.*,
13 1996], the *GMPE* by [Akkar and Bommer, 2010] has been employed for predicting the response
14 of base-isolated structures, characterized by longer fundamental periods (of the order of 3.0 s).
15 As a matter of fact, indeed, the *GMPE* by [Ambraseys *et al.*, 1996] is not suitable for base-
16 isolated buildings being limited to a maximum period equal to 2.0 s. Specific considerations
17 about the effects (on the failure rate for the *GC* performance level) of changing the *GMPE* for
18 base-isolated structure are provided in the last section (Risk Assessment) of the paper.

19 *Isolation System*

20 Two different typologies of rubber-based isolation systems have been considered herein for
21 both new and existing buildings. In particular, the first typology (labelled as *HDRB*) is com-
22 posed by High Damping Rubber Bearings only (*HDRBs*) while, the second typology (labelled
23 as *HDRB+FSB*) is based on a proper combination of *HDRBs* (placed below the columns along
24 the perimeter of the building) and Flat Sliding Bearings (*FSBs*) (placed below the inner columns
25 of the building). The catalogues of the main Italian manufacturers have been used to select
26 commercial devices, featuring suitable values of effective stiffness and vertical capacity. The
27 seismic design of the mentioned isolation systems has been performed through modal response

1 spectrum analysis, in accordance with the latest release of the Italian Seismic Code [*CS.LL.PP.*,
2 *2018, 2019*].

3 Two different approaches have been followed for the design of the rubber-based isolation sys-
4 tems for new and existing buildings, respectively, according the current technical practice in
5 Italy [*Dolce et al. 2010*]. For the latter, the design approach consists in limiting the seismic
6 force transmitted to the superstructure under the “elastic” limit of the superstructure, defined by
7 means of Push Over Analysis (*POA*), thus avoiding the structural damage up to the design
8 earthquake intensity level associated with the Life-safety Limit State (*LLS*). The elastic limit, in
9 terms of base shear (V_y), of the superstructure (in the fixed-base configuration) has been identi-
10 fied in the *PO* curves as the force level corresponding to the occurrence of the first plastic hinge
11 in the weaker direction of the building (i.e. the minimum base shear at the first yielding), as
12 shown in Figure 3 (*a*) and (*b*). Once the elastic limit has been identified, the target fundamental
13 period of the base-isolated building has been derived (Figure 3 (*c*)) and the corresponding value
14 of the maximum displacement (S_{dmax}) has been evaluated using the displacement spectrum asso-
15 ciated with the Collapse Limit State (*CLS*) (Figure 3 (*d*)). The latter value has been opportunely
16 increased using a specific coefficient to account for torsional effects. Finally, commercial de-
17 vices have been selected from the manufacturers’ catalogues. More details about the design
18 choices (i.e. design criteria, device performances and isolation systems configurations) can be
19 found in [*Cardone et al., 2019b*].



1 *Figure 3. Elastic limit for the (a) AQ_{EX} and (b) NA_{EX} building in the fixed-base configuration*
 2 *and (c-d) Design procedure for the AQ_{EX} building.*

3 For new base-isolated buildings, the design of the isolation system has been performed by linear
 4 dynamic analyses, aimed at simultaneously limiting the displacement demand to the superstruc-
 5 ture, and ensuring its elastic behaviour at *LLS*. Target fundamental periods ranging from 2.4 s to
 6 3.3 s have been thus derived, for the selected case-study buildings, as illustrated in [Ragni *et al.*,
 7 2018a]. Then, effective periods have been calculated based on the dimensions of isolators, ac-
 8 cording to indications of the main Italian manufacturers, and on nominal properties of the isola-
 9 tion bearing at the average design shear strain at the *CLS*.

10 Table 2 summarizes the geometric characteristics and design safety verification outcomes for
 11 the rubber-based isolation systems adopted in this study. All the *HDRBs* are characterized by a
 12 soft compound (shear modulus G equal to 0.4 MPa) and equivalent viscous damping ratio (ξ)
 13 equal to 15%. In Table 2, the devices are identified by a three-number code composed by the
 14 nominal diameter (ϕ), the total rubber layer thickness (t_e) and the single rubber layer thickness
 15 (t_r). Similarly, the selected *FSBs* are identified by their vertical load capacity (V), displacement
 16 capacity ($d_{tot}=d_{tot,x}=d_{tot,y}$, expressed in mm) and pot diameter (Φ_p). The effective fundamental pe-
 17 riod of the base-isolated building (T_{is}) and the nominal (design) maximum displacement capaci-
 18 ty of the devices ($d_{max,HDRB}$ and $d_{max,FSB}$) are also shown. For *HDRBs*, $d_{max,HDRB}$ is the value corre-

1 sponding to the attainment of a maximum design rubber shear strain equal to 2 (i.e. 200%), ac-
2 cording to the explicatory notes of the *NTC2018* [*CS.LL.PP. 2019*] and the manufacturers' cata-
3 logues. For *FSBs*, $d_{max,FSB}$ is conventionally assumed equal to $1.2d_2$, in compliance with [*CEN-*
4 *EN 2005*], where d_2 represents the design displacement of the isolation system at the *CLS*. It is
5 worth noting that, the value $1.2d_2$ turns out to be approximately equal to the design displace-
6 ment capacity of *HDRBs* increased by 50 mm. Finally, in Table 2 the demand/capacity ratios in
7 terms of shear strain (*D/C shear*), compression load (*D/C comp*) and tensile stress (*D/C tens*)
8 are summarized for each case study for the design condition. As can be observed, all the rubber-
9 based isolation systems have been designed using similar *D/C* ratios, very close to 1, in particu-
10 lar for shear and compression.

11 Adopting a rubber-based isolation system composed by *HDRBs* only, no design solutions was
12 found for the existing building located in Naples (*NA_{EX}*). On the other hand, an isolation system
13 composed by two different typologies of *HDRBs* have been used for the *AQ_{EX}* building (labelled
14 as *HDRB-AQ_{EX}* in Table 2). A design solution has been found for both case-studies using
15 *HDRB+FSB* isolation systems (see Table 2).

16 More details on the design criteria and results of the design safety verifications can be found in
17 [*Ragni et al., 2018a, Cardone et al. 2019b*].

18

1 Table 2. Geometric characteristics and design safety verification outcomes for the rubber-based
 2 isolation systems considered in this study.

Case study	HDRB $\phi/t_e/t_r$	FSB $V/d_{tot}/\phi_p$	d_{max} [mm] HDRBFSB	T_{is} [s]	D/C shear	D/C comp	D/C tens
HDRB-AQ _{EX}	550/154/7+600/152/8	-	300	-	2.49	0.81	0.99 0.79
HDRB+FSB-AQ _{EX}	600/152/8	3500/700/250	300	350	2.68	0.82	0.93 0.14
HDRB+FSB-NA _{EX}	450/102/6	3500/500/250	200	250	3.30	0.89	0.98 0.00
HDRB-AQ _{NEW}	550/154/7+600/150/6	-	300	-	2.46	0.86	0.97 0.33
HDRB-NA _{NEW}	500/126/6+550/126/7	-	250	-	2.52	0.74	0.84 0.00
HDRB+FSB-AQ _{NEW}	600/176/8	3500/800/250	350	400	3.04	0.85	0.98 0.19
HDRB+FSB-NA _{NEW}	500/102/6	3500/500/250	200	250	2.79	0.88	0.79 0.00

3
 4 **Definition of Performance Levels**

5 The seismic performances of the examined case studies have been evaluated considering two
 6 specific performance levels, namely the *Global Collapse (GC)* and the *Usability-Preventing*
 7 *Damage (UPD)* performance levels.

8 The occurrence of the *UPD* has been assessed based on a multi-criteria approach combining the
 9 following main concepts: (i) reparability of non-structural elements, (ii) complete protection of
 10 structural elements and (iii) no interruption of use of the building towards frequent seismic
 11 events. The top displacement threshold associated with the attainment of the *UPD* performance
 12 level has been defined, for each case-study, by means of pushover analysis performed on the
 13 superstructure in the fixed-base configuration (see Table 3). More details about the mentioned
 14 approach are available in the Appendix A of [ReLUIS-RINTC 2018]. As stated in [Ragni et al.,
 15 2018a, Cardone et al., 2019b], the isolation system and the superstructure represent two ele-
 16 ments of the same in-series system. As a consequence, the *GC* is assumed to occur if either the
 17 superstructure or the isolation system fails. For what concerns the superstructure, the collapse is
 18 associated with the occurrence of the first of the following conditions [Ricci et al. 2018],
 19 (checked on the capacity curve of the building in the fixed-base configuration): (i) 50% de-
 20 crease of the lateral strength on the pushover curve; (ii) the first column classified as shear-
 21 controlled (prior to or after flexural yielding) reaches a chord rotation equal to 0.10, correspond-
 22 ing to the loss of axial load carrying capacity [Ricci et al. 2019]. In other words, superstructure
 23 collapse (hence the whole system collapse) occurs when, in one of the two main directions, the

1 maximum value of the top displacement derived from dynamic analyses reaches the top dis-
 2 placement corresponding to the first of the aforementioned limit conditions (see Table 4). More
 3 details can be found in [Ragni *et al.*, 2018a, Cardone *et al.*, 2019b].

4 *Table 3. UPD superstructure limit displacements [mm]*

Direction	Existing Buildings		New Buildings			
			HDRB		HDRB+FSB	
	AQ _{EX}	NA _{EX}	AQ _{NEW}	NA _{NEW}	AQ _{NEW}	NA _{NEW}
X	51	37	59	60	59	42
Y	64	49	57	56	66	61

5
 6 *Table 4. GC superstructure limit displacements [mm]*

Direction	Existing Buildings		New Buildings			
			HDRB		HDRB+FSB	
	AQ _{EX}	NA _{EX}	AQ _{NEW}	NA _{NEW}	AQ _{NEW}	NA _{NEW}
X	205	170	501	581	488	565
Y	110	130	271	342	267	324

7
 8 The failure modes considered for HDRBs are cavitation, shear and buckling. The failure
 9 criteria assumed to assess the occurrence of cavitation and shear are similar to those proposed in
 10 [Ragni *et al.*, 2018a], where the *HDR Bearing Element* was adopted to describe the non-linear
 11 cyclic behaviour of *HDRBs*. In particular, the cavitation failure mode of a single bearing is sup-
 12 posed to occur in the post-cavitation branch, for an axial tensile strain equal to 0.5. For the shear
 13 failure, a limit shear strain equal to 3.5 has been considered. The global collapse condition (of
 14 the whole building due to the isolation system collapse) is conventionally reached when (at
 15 least) 50% of the devices of the isolation system simultaneously fail due to cavitation (tension
 16 failure mode of the isolation system) or shear (shear failure mode of the isolation system), re-
 17 spectively. It is worth noting that, with regard to the shear failure, the choice of 50% of the total
 18 number of devices is merely conventional and on the safety side. In fact, very few experimental
 19 evidences are available regarding the redistribution capacity within the isolation system after the
 20 failure of a certain number of bearings and on their post-collapse behaviour in shear [Nakazawa
 21 *et al.* 2011]. In the case of tension (associated with the post-cavitation) the choice of 50% is also
 22 conventional and on the safety side, because usually only few bearings (under corner columns

1 or staircases) are subjected to this kind of failure mode. More details about the described as-
2 sumptions can be found in [Ragni et al., 2018a]. On the other hand, in this paper, the collapse
3 criterion adopted for buckling is different from past studies. As a matter of fact, indeed, in the
4 previous studies (using the *HDR bearing element*), a simplified force-based criterion was adopt-
5 ed in which the P/P_{cr} ratio (i.e. the ratio between the current axial load P and the critical buck-
6 ling load P_{cr}) was monitored [Ragni et al., 2018]. The buckling collapse of the isolation system
7 was conventionally deemed to occur when at least 50% of the *HDRBs* reached, at the same
8 time, a P/P_{cr} ratio ≥ 1 .

9 In this study, the collapse criterion associated with buckling has been revised, since
10 *HDRBs* have been modelled with the *Kikuchi Bearing Element*, which explicitly simulate the
11 post-buckling behaviour of *HDRBs*. Consequently, a failure criterion in terms of compressive
12 strain has been adopted. In particular, for any single device, buckling failure mode occurs for an
13 axial compression strain equal to 0.5, even if experimental results showed that rubber bearings
14 can sustain even higher vertical axial deformation after buckling [Monzon et al. 2016]. Howev-
15 er, mechanisms other than those considered in the building FEM model could take place for
16 very large vertical displacements. Thus, the limit threshold of 0.5 for the compression strain has
17 been prudently assumed for the analysis reliability. Such individual criterion, coupled with the
18 global collapse criterion, i.e. the simultaneous achievement of a compression strain equal to 0.5
19 for one half (50%) of the devices, appears realistic.

20 For *HDRB+FSB* isolation systems, two additional failure criteria have been considered
21 for *FSBs*: (i) the attainment of a critical uplift value corresponding to $H/2$, where H is the total
22 height of the device, and (ii) the attainment of a critical value of horizontal displacement corre-
23 sponding to a limit value of compression stress, equal to 60 MPa according to [prEN 1337-5].
24 The first criterion ($H/2$) has been set based on the information provided by the main Italian
25 manufacturers. As a matter of fact, indeed, as the horizontal displacement increases, the effec-
26 tive resisting area of the device reduces, and as a consequence the contact pressure increases.
27 Numerical simulations [Cardone et al. 2019c] showed that the aforesaid compression rate limit
28 threshold is usually reached for a value of the horizontal displacement approximately equal to

1 the design displacement capacity of the device ($d_{max,FSB}$) increased by an extra-displacement
 2 $\alpha\Phi_p$, with $\alpha \approx 1/2$. All that considered, in this study the ultimate displacement capacity of the
 3 *FSBs* has been conventionally assumed equal to $d_{max,FSB}+1/2\Phi_p$.

4 The global collapse of an *HDRB+FSB* isolation system due to *FSBs* is deemed to occur
 5 when the horizontal displacement of the centre of gravity of the isolation floor is equal to the
 6 aforesaid limit value or when at least 50% of the devices reach the mentioned uplift threshold.

7 Failure modes and collapse conditions considered in this study for rubber-based isolated struc-
 8 tures are summarized in Table 5.

9 *Table 5. Failure modes and collapse conditions for rubber-based isolated buildings*

	Failure modes	Collapse conditions
Superstructure	Superstructure collapse	The relative displacement between the top of the building and the isolation level is equal to the lower value between: (i) the top displacement from POA corresponding to a peak strength reduction of 50% on the negative slope and (ii) the top displacement from POA corresponding to the first brittle failure in a structural element
	Compression	50% of elastomeric devices reaches an axial compression strain (ϵ_c) greater than or equal to 0.5
Isolation System	Tension	50% of elastomeric devices reaches an axial tensile strain (ϵ_t) greater than or equal to 0.5
	Shear	50% of elastomeric devices reaches a shear strain (γ_r) greater than or equal to 3.5
	Overstroke and uplift	(i) The horizontal displacement of the center of gravity of the isolation floor is equal to the ultimate displacement capacity or (ii) the 50% of devices reaches the critical up-lift value.

10

11 **Modelling approach**

12 *Modelling assumptions*

13 The modelling strategy adopted for both isolation system and superstructure takes into
 14 account the most recent progress in the field of nonlinear finite element modelling. In particular,
 15 big efforts have been made to represent the complex behaviour of rubber bearings.

16 The main challenge of a bearing model for a reliability analysis is to reasonably simulate
 17 the response under a wide range of seismic input levels, especially beyond the design conditions

1 and up to the collapse of the device. Many aspects of *HDRBs* behaviour should be considered
2 under extreme loadings [Kelly, 1997 and Kumar et al. 2014] such as coupled bidirectional mo-
3 tion in horizontal directions, coupling of vertical and horizontal motion, cavitation and
4 post-cavitation behaviour in tension, strength degradation in cyclic tensile loading due to cavit-
5 ation, variation in critical buckling load capacity due to lateral displacement, post buckling be-
6 haviour, strength degradation in cyclic shear loading due to Mullins effect, shear fracture, post
7 failure behaviour and tension fracture. However, none of the numerical models available in the
8 literature is able to capture all these phenomena at the same time [Grant et al., 2004; Tubaldi et
9 al., 2017; Ragni et al., 2018b, Kumar et al., 2014, Ishii and Kikuchi, 2019], but among them,
10 the latest version of the *Kikuchi Bearing Element* [Ishii and Kikuchi, 2019], recently imple-
11 mented in OpenSees, has been chosen in this work.

12 The *Kikuchi Bearing Element* is a fully 3D model that differently to the others takes into
13 account the coupled behaviour in the vertical and horizontal direction through its large dis-
14 placement formulation. In particular, it is able to capture the well-known geometric nonlinear
15 effect called “ $P-\Delta$ ” effect: the reduction of the horizontal stiffness related to the increase of ver-
16 tical load and horizontal displacement. Such peculiarity appears very important especially for
17 medium-high level of vertical pressure as emerged from the experimental results used for the
18 model calibration within this work [Brandonisio et al. 2017] (see “Model Calibration” section)
19 and also highlighted in other studies, i.e. [Koh and Balendra, 1989].

20 The *Kikuchi Bearing Element* is based on the *two-springs model* philosophy, but compris-
21 ing the nonlinear behaviour of the springs and using a different arrangement of them. More in
22 detail, the three-dimensional analytical model features triaxial interaction between the two hori-
23 zontal components, and the vertical component. The shear bidirectional behaviour is based on
24 the use of *Multi Shear Spring model (MSS)* [Wada and Hirose, 1987] while the vertical Euler
25 column buckling behaviour is based on the *Multi Normal Spring model (MNS)*. The arrange-
26 ment of *MSS* and *MNS* is shown in Figure 4. In this way the model incorporates both the influ-
27 ences of material and the geometrical nonlinearities.

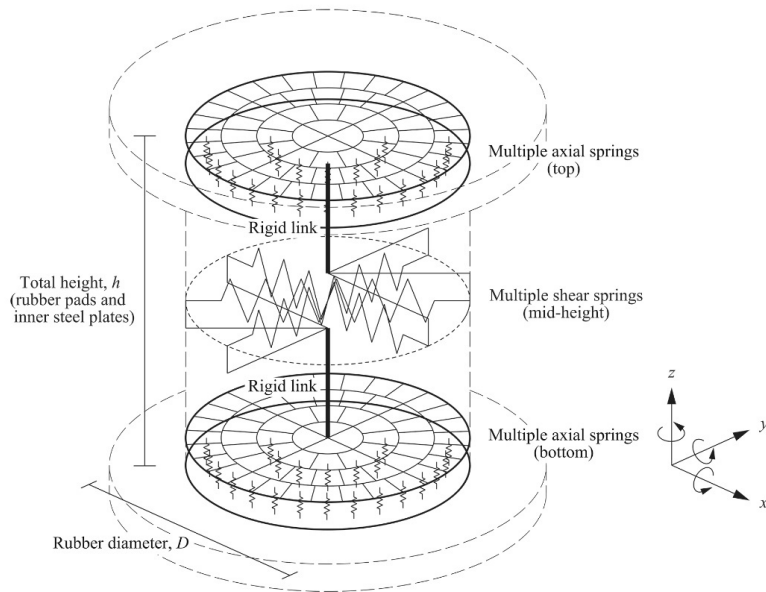


Figure 4. Multi spring mechanical model for circular elastomeric bearing (from Ishii and Kikuchi 2019).

Thus, the model is able to properly predict the behaviour in the post-buckled condition even for squared bearings and variable vertical load due to the rocking motion of the superstructure during an earthquake. This is an essential feature for reliability analysis because the actual hysteresis behaviour of isolation bearings under a structure subjected to severe earthquake shaking is not the same as that obtained from cyclic shear tests of a bearing with constant axial stress, because of the influence of the variation of vertical load due to overturning forces. In particular, external bearings may show a strongly asymmetric hysteretic cycle with a substantial pure shear behaviour for one side of the cycle (lowest compression) and a possible post-buckled behaviour in the other side (higher compression) [Kikuchi et al., 2010, Takaoka et al. 2011].

For the *Multi Shear Spring (MSS) model*, the *KikuchiAikenHDR* material has been used. The original version implemented in Opensees features only a limited set of pre-calibrated rubber compounds, but they can be slightly adjusted to better fit a specific rubber compound using three correction coefficients controlling the equivalent shear modulus (c_g), the equivalent viscous damping ratio (c_h) and the ratio of shear force at zero displacement (c_u), respectively. Being based on a limited number of parameters, the calibration process of such model appears simple. On the other hand, for the same reason, important phenomena, such as stiffening for

1 high shear deformation and scragging, are neglected. As a consequence, in this work, the shear
 2 behaviour of HDRBs has been calibrated with reference to a specific cycle (i.e. the third cycle,
 3 according to [EN15129, 2009]) under the hypothesis that the behaviour in the virgin state [Tu-
 4 baldi et al 2017, Ragni et al 2018b] is not significant towards the final performance assessment.

5 For the *Multi Normal Spring (MNS) model*, the *AxialSP* material, already implemented in
 6 the OpenSees material library, has been used. Such material is fully defined by the following
 7 parameters and consequently not calibrated: (i) initial elastic vertical stiffness E_{init} , (ii) post elas-
 8 tic stiffness in tension ($1/100E_{init}$) and compression ($1/2E_{init}$), (iii) cavitation stress and (iv) com-
 9 pression yielding stress. According to [Ishii and Kikuchi, 2019] the following relationship can
 10 be used to derive the elastic E_{init} :

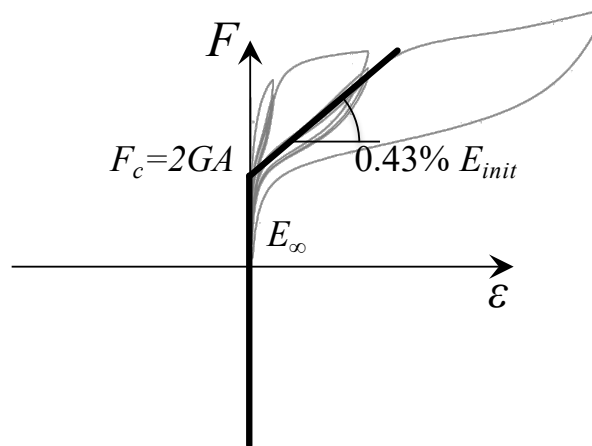
$$E_{init} = K_{bulk} \left\{ 1 - \frac{2}{\bar{\lambda}} \frac{I_1(\bar{\lambda})}{I_0(\bar{\lambda})} \right\} \quad (1)$$

11 where K_{bulk} is the bulk modulus of the rubber compound, usually equal to 2000MPa, I_1 and I_0
 12 are the modified Bessel function of the first kind of order 1 and 0 respectively whereas $\bar{\lambda}$ is the
 13 dimensionless parameter

$$\bar{\lambda} = \frac{D}{t} \sqrt{\frac{3G}{K_{bulk}}} \quad (2)$$

14 Moreover, values equal to 1MPa and -100MPa are usually adopted for cavitation stress
 15 and compression yielding stress, respectively [Ishii and Kikuchi 2019]. Comparing the numeri-
 16 cal results obtained adopting the mentioned values of the model parameters with those derived
 17 by several calibration tests performed within this work on common rubber devices generally
 18 used in the Italian context, a sensible overestimation of the “ P - Δ ” effects has been observed.
 19 The key point of the different ability to predict the post-buckling behaviour can be found in the
 20 hidden hypothesis that is at the base of this model: the behaviour of the single normal spring in
 21 tension, representing a single fiber, is the same of the whole bearing. This hypothesis could be
 22 true depending on the isolator geometry. As a matter of fact, for isolators with very large prima-
 23 ry shape factors and conventional values of the secondary shape factors (e.g., $S_1=30$ and $S_2=3$),

1 the compression buckling could be triggered by the cavitation of the perimetral fibers subjected
 2 to tension. Differently, slender bearings with lower primary shape factors and larger secondary
 3 shape factors could experience buckling before the local cavitation of the rubber. The primary
 4 shape factor of the rubber bearings examined in this work is around 20, lower than that of the
 5 bearings tested within [Yamamoto 2009, Kikuchi et al. 2010 Ishii and Kikuchi 2019] that are
 6 higher than 30. Thus, to avoid the local cavitation of the bearing before the buckling, the mate-
 7 rial used for the *MNSs* has been replaced by a simple elastic material with stiffness equal to E_{init} .
 8 Obviously, in the described condition, the model is not able to capture the nonlinear axial be-
 9 haviour associated with cavitation. As a consequence, the *Kikuchi Bearing Element* has been
 10 implemented in the building model in-series with a rigid plastic spring describing the global
 11 cavitation of the rubber. The external spring is characterized by a rigid behaviour under com-
 12 pression and in the range of tension forces lower than the cavitation threshold, while it is
 13 properly calibrated to describe the inelastic post-cavitation behaviour above the mentioned
 14 threshold (see Figure 5). In particular, as the *AxialSP* material does not feature any cyclic deg-
 15 radation of the post-cavitation behaviour, median values of the post-cavitation stiffness and
 16 force threshold have been adopted in the model (similar to the third-cycle concept used for the
 17 shear behaviour), leading to a cavitation force of $2GA$ and a post-cavitation stiffness equal to
 18 $0.43\% E_{init}$, based on experimental result of [Warn 2006]. In this way, the global building model
 19 is able to capture the influence of cavitation on the rocking motion during an earthquake.

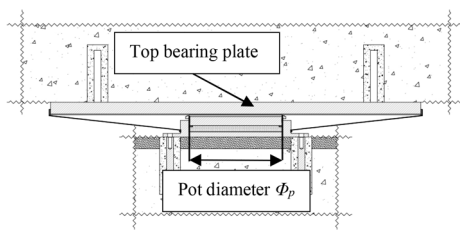


20

21 *Figure 5. Uniaxial constitutive model of the vertical in-series rigid-plastic spring for cavitation*
 22 *behaviour (superimposed on test from Warn 2006).*

As far as the modeling of flat sliding bearings is concerned, the element flatSliderBearing has been used adopting a velocity-dependent and axial-load-dependent friction model [Constantinou et al., 1990], and assuming a friction coefficient at the maximum load capacity equal to 1% for fast velocities and 0.5% for low velocities, based on the results of manufacturer's type tests. More details about slider modeling can be found in [Cardone et al., 2019a].

It is worth noting that such low damping coefficients implies a negligible effect of the sliders on the isolation system behaviour (i.e. extra-damping). This must be assessed by suitable acceptance tests on materials or devices.



\mathbf{a}_{Slow}	constant for coefficient of friction at low velocity	0.02073
\mathbf{n}_{Slow}	exponent for coefficient of friction at low velocity	0.9
\mathbf{a}_{Fast}	constant for coefficient of friction at high velocity	0.04146
\mathbf{n}_{Fast}	exponent for coefficient of friction at high velocity	0.9
\mathbf{a}_0	constant rate parameter coefficient	0.00458
\mathbf{a}_1	linear rate parameter coefficient	0
\mathbf{a}_2	quadratic rate parameter coefficient	0

Figure 6. FSB device and model parameters

Model calibration

The results of an experimental campaign [Brandonisio et al 2017] performed at the SisLab (Materials and Structures Test Laboratory) of the University of Basilicata on three circular HDRBs, have been used for the model calibration of the rubber bearings. The main characteristics of the tested bearings are reported in Table 6. As can be seen, the mentioned bearings feature different geometrical dimensions but the same soft rubber compound (labelled as S - Soft), characterized by nominal values of shear stiffness G and damping factor ζ equal to 0.4MPa and 15% respectively. In Table 6, Φ denotes the outer rubber diameter, Φ' the inner steel shim diameter, t_r the single rubber layer thickness, t_e the total rubber layer thickness, S_1 the primary shape factor ($S_1=\Phi'/4t_r$) and S_2 the secondary shape factor ($S_2=\Phi'/t_e$).

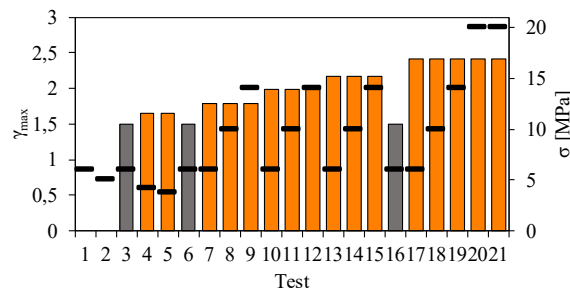
Table 6 Geometrical characteristics of the tested HDRBs

HDRB code	Φ [mm]	Φ' [mm]	t_r [mm]	t_e [mm]	S_1	S_2
SI-S-500-176	500	490	5.5	176	22.7	2.8
SI-S-600-217	600	590	7	217	21.4	2.8
SI-S-700-207	700	690	9	207	19.5	3.4

1

2 More in detail, a specific sequence of tests has been performed on each device. First of
3 all, the static compression stiffness test (*Axial Test*, test 1-2) and horizontal *Shear Cyclic Test*
4 (*SCT*, test 3) have been carried out. Then, a series of *Shear Quasi static Test (SQT)*, alternated
5 with the repetition of the *SCT* (tests 6 and 16), have been conducted (Figure 7). The *SQTs* are
6 half cycle (positive shear deformation only) tests, organized in groups of three with the same
7 maximum shear displacement and increasing vertical compression (6 MPa, 10 MPa and 14
8 MPa). Some special tests have been also performed to better assess extreme conditions. More
9 details can be found in [Brandonisio et al. 2017]. It should be noted that the whole test sequence
10 has been performed on a same device, thus results are strongly affected by the load history de-
11 pendent behaviour of the rubber effect, in the case of multiple repeated cycles [Mullins, 1969,
12 Tubaldi et al. 2017 and Ragni et al. 2018b].

13 Among the three sets of tests, those carried out on the SI-S 700-207 have been chosen to
14 calibrate the numerical model because it is the most complete series. The other two sets (tests on
15 SI-S 500-176 and SI-S 600-217) have been used to verify the ability of the calibrated model to
16 reproduce the experimental results.

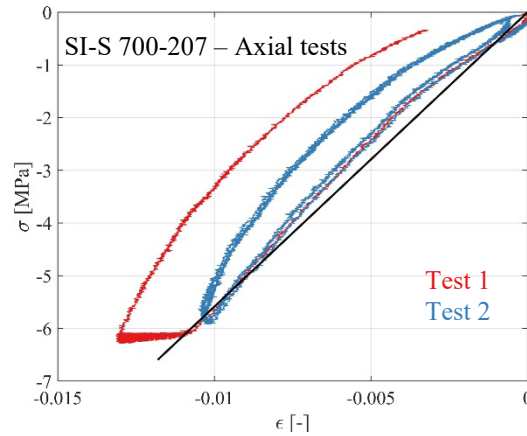


17

18 *Figure 7. SI-S 700-207 test sequence (grey bars refer to strain amplitude of SCTs, orange bars*
19 *refer to strain amplitude of SQTs, while horizontal dashes represent the vertical compression*
20 *stress)*

21 More in detail, the rubber compound material used for the isolators model is the
22 X0.4-0MPa [Bridgestone Corporation, 2017] with a shear modulus equal to $G=0.4$ MPa and a

1 bulk modulus equal to $K_{bulk}=2000\text{MPa}$. Figure 8 shows results of the first two axial tests which
 2 are properly predicted by the model. Obviously, as the vertical spring doesn't feature any vis-
 3 cous component, it is not able to predict the unloading branch. However, such limitation is not
 4 crucial during a seismic event as the vertical load variation is a dynamic action.



5

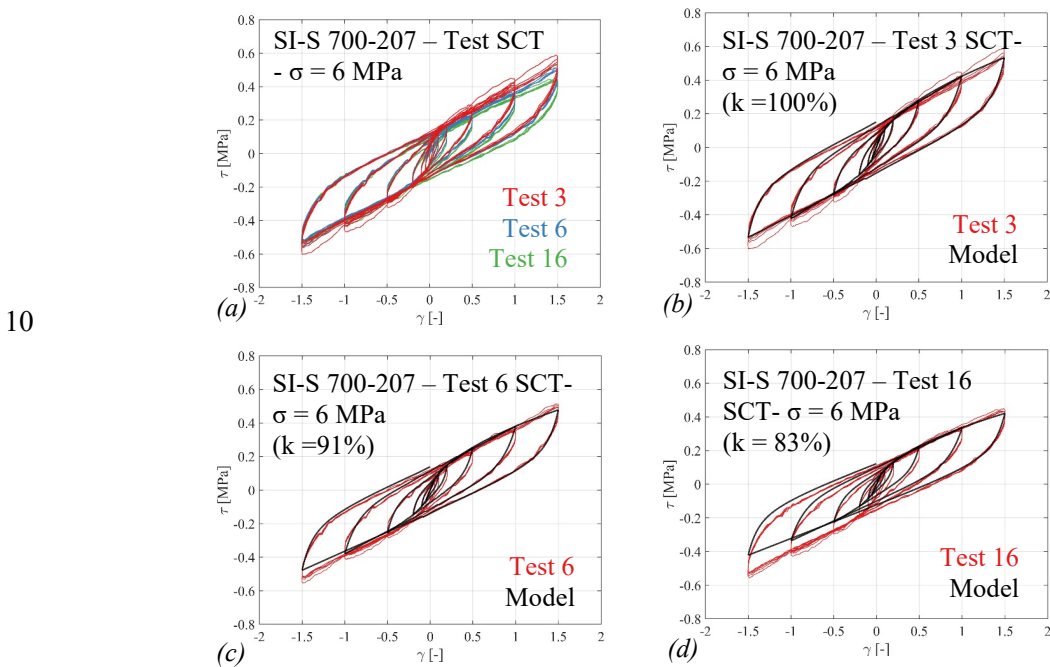
6 *Figure 8. Comparison of axial test experimental results and calibrated model for SI S 700 207*
 7 *HDRB*

8 As far as the shear cyclic behaviour is concerned, values equal to 1.15, 0.75 and 0.75
 9 have been adopted for the correction coefficients c_g , c_h and c_u , respectively, to fit the third cycle
 10 (according to [EN15129, 2009]) of the first *SCT* (i.e. test 3 of Figure 9). To predict the hysteret-
 11 ic response of the subsequent *SCTs* (test 6 and 16 in Figure 9), c_g has been further corrected (as
 12 percentage k of the initial value) to reproduce the scragging effects due to previous test. It
 13 should be noted that the reduction percentage calibrated based on Test 6 and 16 is taken con-
 14 stant in simulating the *SQTs* following each *SCT*. Moreover, it is worth noting that the same re-
 15 duction percentage has been applied to the axial springs of the model to simulate *SQTs*, even if
 16 further investigation would be needed on the influence of repeated shear tests on the axial prop-
 17 erties of the device.

18 Figure 9(a) compares the results of the three *SCTs* (Test 3, 6 and 16) in order to highlight
 19 the stress softening due to the load history dependence. The half cycles of the *SQTs* performed
 20 between the *SCTs* influence only the positive range of shear deformation, confirming the de-
 21 formation-induced anisotropy of the material [Tubaldi et al 2017, Ragni et al 2018b]. Figure 9
 22 (b)-(c)-(d) show a very good agreement between the experimental and the numerical results rel-

1 evant to the *SCTs*. Obviously, the model cannot predict the first loading branch of the *SQTs*, be-
 2 ing the model calibrated on the third cycle, nor the model can follow the asymmetrical behav-
 3 iour of the rubber. The simulation of the *SQTs* are reported in Figure 10, which confirms the
 4 ability of the model to also simulate the device response under large displacements and large
 5 axial loads.

6 It worth to note that the stiffness percentage reduction has been used only to simulate the
 7 experimental tests, while unadjusted values are used in the multi-stripe analyses because several
 8 repeated cycles on a same device are not representative of an earthquake scenario. More details
 9 regarding the model calibration can be found in [Micozzi 2020].



11

12 *Figure 9. Superimposed SCTs for SI-S 700-207 HDRB and comparison between experimental*
 13 *results and calibrated model.*

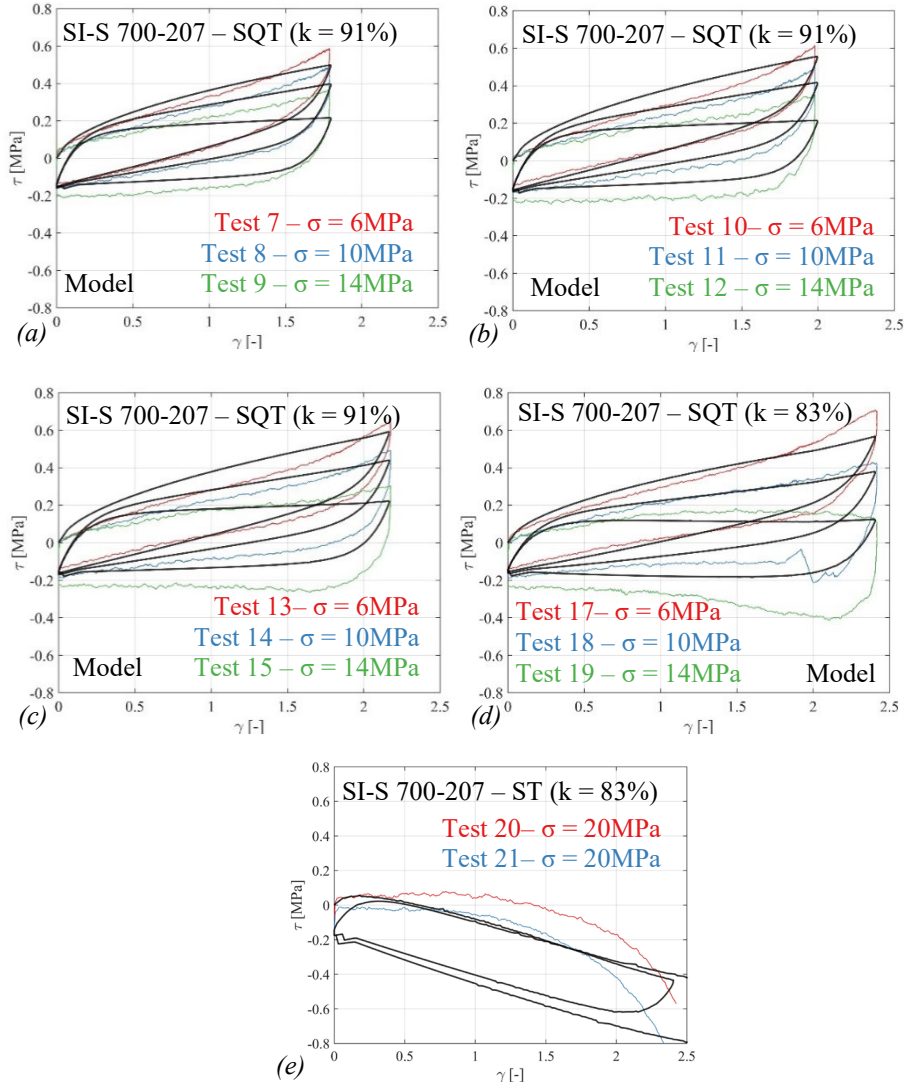


Figure 10. Comparison between SQT experimental results and calibrated model for SI-S 700-207 HDRB

As far as the superstructure is concerned, pragmatic choices have been done in order to limit the computational efforts, maintaining as much as possible the most reliable and advanced features of the current state-of-the-art. In particular, a lumped plasticity model has been chosen for beam and column elements of the superstructure, whereas elastic beams have been used for the base floor grid above the isolation system. The choice of representing the superstructure with a nonlinear model is justified by the results of recent studies on this topic [Cardone *et al.*, 2013, Cardone and Flora, 2016], which pointed out the effects of the inelastic behaviour of the

1 superstructure on the seismic response of base isolated buildings. The model also includes the
2 staircase structure (inclined beams and cantilever steps) as well as masonry infill panels.

3 Regarding the RC members, in particular, the model selected for the description of the
4 section flexural behaviour is the well-known model by Ibarra [Ibarra and Krawinkler, 2005, Ibarra
5 et al., 2005], implemented in OpenSees as *modIMKmodel*. To consider shear failures before
6 or after flexural yielding in beam/column elements and in beam column joints, all the hinges
7 have been pre-qualified either as (i) *ductile*, in which the shear failure is avoided and the
8 moment-rotational backbone model is not modified, or (ii) *shear critical*, in which the backbone
9 is reduced after the shear failure, following a softening branch up to zero based on the empirical
10 proposal by [Aslani and Miranda, 2005]. More details about this collapse criterion can be found
11 in Ricci et al. 2019. In the (ii) case, if the shear failure occurs before yielding the element is defined
12 as “brittle”, whereas if shear failure occurs between yielding and the ultimate bending
13 moment the element is characterized by a flexure-shear interaction failure mechanism. Regarding
14 the beam-column joint, the joint panel model called “*scissors model*” has been used. It is a
15 very simple and computationally efficient joint model, but also sufficiently accurate in predicting
16 the experimental beam-column joint panel behaviour for simulating the seismic response of
17 non-ductile RC frames [De Risi et al., 2017]. The adopted constitutive model accounts for two
18 possible failure mode of the beam-column joints: joint shear failure prior to or after the
19 achievement of yielding of the adjacent beams/columns (in strong column - weak beam or weak
20 column-strong beam hypothesis).

21 The contribution of masonry infills is modelled with an equivalent compression-only
22 strut. The skeleton curve of the diagonal strut has been derived according to a modified version
23 of the *Decanini model* [Sassun et al., 2016]. The effects of the openings have been taken into
24 account through suitable reduction factors [Decanini et al., 2014].

25 More information on the superstructure modelling can be found in [Camata et al, 2017,
26 Ricci et al., 2018, Ricci et al. 2019].

27

28

1

2 **Non-Linear Time History Analysis (NTHA)**

3 *Seismic Input*

4 Multi-Stripe non-linear dynamic analyses (*NTHA*) have been performed to evaluate the seismic
5 performances of the examined case-studies towards *GC* and *UPD* performance levels. As men-
6 tioned before, 10 earthquake intensity (*IM*) levels have been investigated. Considering that the
7 fundamental periods of the examined case-studies range from 2.5 to 3.3 s, a unique conditioning
8 period (T^*) equal to 3.0 s has been assumed for the seismic performance assessment. The values
9 of $S_a(T^*)$ for each *IM* level and for the two considered sites (expressed in terms of geometric
10 mean) are summarized in Table 7. Each “stripe” of seismic response has been then analysed
11 running a set of 20 ground motion pairs featuring the mentioned conditioning period. It is worth
12 noting that, according to Italian Seismic Code (NTC2018), the *IM* associated with level 2 and 6
13 (labelled as *IM2* and *IM6* in what follows) correspond to the earthquake intensity levels for the
14 verification of the *Damage* and *Collapse Limit States*, respectively.

15 For the *GC* performance level, the analyses results are provided in terms of number of
16 failures as a function of the *IM* level. More in detail, the total number of records causing a col-
17 lapse condition for the examined case-study is reported as a function of the *IM* level. Moreover,
18 using different colours, information about the specific failure mode causing collapse (the first
19 one occurring during the analysis) is provided for each *IM* level. On the other hand, for the *UPD*
20 performance level, diagrams summarizing the demand-capacity ratios (D/C) associated with
21 each ground motion pair, as a function of the earthquake intensity level, are presented (for each
22 direction). In particular, the capacity (C) is obtained as described before (see “Definition of Per-
23 formance Levels” section), while, the demand (D) is represented by the maximum top dis-
24 placement of the superstructure (with respect to the isolation system) derived from *NTHA* (see
25 Table 3).

26 It is worth noting that, when the isolation system collapse anticipates the occurrence of
27 the maximum top displacement registered during the analysis, the top displacement associated

1 with collapse has been assumed as displacement demand (D) in the calculation of the D/C ratio
 2 at the UPD performance level. For each IM level, the total number of records leading to a “fail-
 3 ure condition” in terms of UPD (conventionally reached for D/C ratios larger than 1) is also
 4 provided.

5 *Table 7. Spectral accelerations $Sa(T^*=3s)$, expressed in unit of g, for each earthquake intensity*
 6 *level*

IM	1	2	3	4	5	6	7	8	9	10
RP (years)	10	50	100	250	500	1000	2500	5000	10000	100000
L'Aquila	0.0002	0.011	0.031	0.062	0.11	0.177	0.271	0.384	0.576	1.053
Naples	0.001	0.009	0.026	0.044	0.067	0.093	0.126	0.162	0.216	0.348

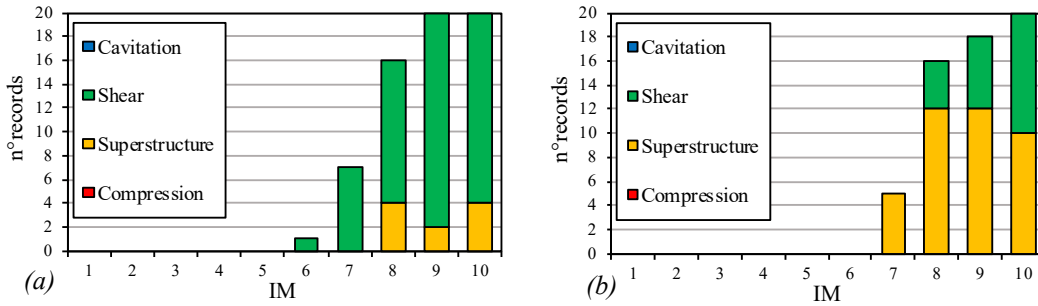
7

8 *NTHA results for new buildings*

9 Figure 11 (a) and Figure 13 (a) show the results relevant to the GC performance level for the
 10 new buildings equipped with HDRBs only, located in L'Aquila and Naples, respectively (i.e.
 11 HDRB-AQ_{NEW} and HDRB-NA_{NEW}). As can be seen, results registered for HDRB-AQ_{NEW} (see
 12 Figure 11(a)) show no failures at IM levels from 1 to 5. Two failures occur at $IM6$. Then, the
 13 number of failures rapidly increases reaching 20 at $IM9$. The shear failure emerged as the preva-
 14 lent failure mode. The collapse of the superstructure occurs as first failure mode only in a few
 15 cases. Such result is directly related to the main peculiarities of the numerical model used to
 16 simulate the $HDRBs$ behaviour. In fact, the large displacements formulation of the *Kikuchi*
 17 *Bearing Element* produces a progressive reduction of the horizontal stiffness of the device,
 18 which leads to an increase of the horizontal displacements, but generally also a reduction of the
 19 shear force transmitted to the superstructure.

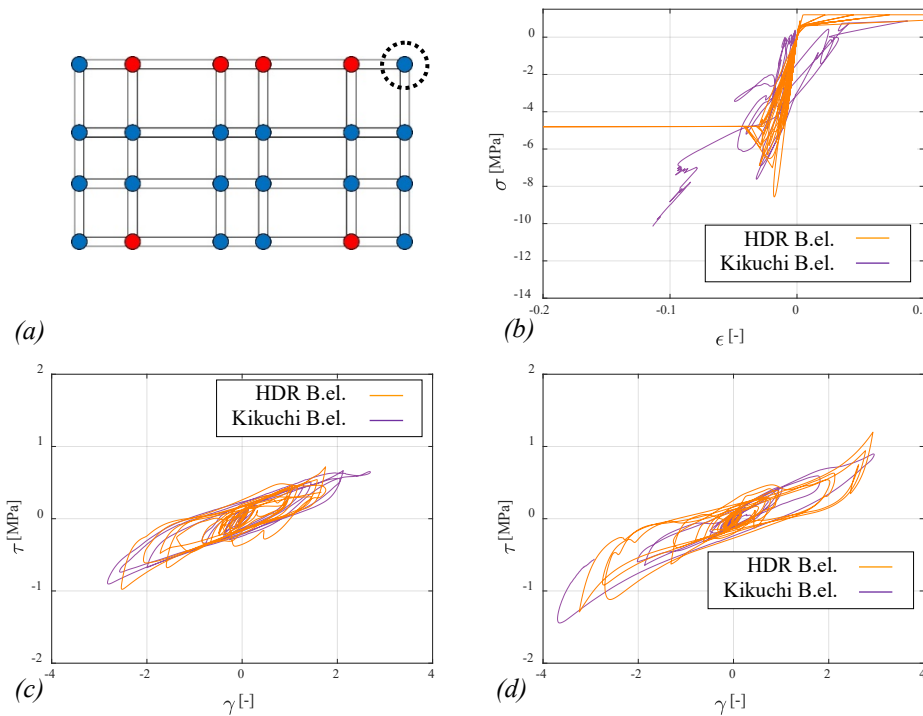
20 As the value of 3.5 for the ultimate shear strain of $HDRBs$ is somehow a safety-side choice (for
 21 example, in [Nishi et al., 2019] most of the bearings show shear rupture for strain higher than
 22 4.0), a second shear deformation limit of 4 is also examined to better quantify how this limit af-
 23 fects the final results. The results considering a shear strain limit equal to 4 are shown in Figure
 24 11(b). The total number of failures decreases at $IM6$ (-1), $IM7$ (-2) and $IM9$ (-2), while remain-
 25 ing the same for the other IM levels. Moreover, in many cases, the occurrence of a shear failure,

1 associated with the revised threshold, is anticipated by the superstructure collapse. As a conse-
 2 quence, overall the assumption on the ultimate rubber shear strain little affects the final results
 3 (as shown later in Figure 26).



4
 5 *Figure 11. GC results for HDRB-AQ_{NEW}: (a) shear limit 3.5, (b) shear limit 4.0*

6 To better understand the behaviour of the new *Kikuchi Bearing Element* used, Figure 12 shows
 7 the vertical and horizontal strain-stress cycles for a corner bearing during a *IM9* earthquake. The
 8 *HDR Bearing Element* results of the past research is also showed for comparison purpose.



9
 10 *Figure 12. (a) Bearing position, (b) vertical and (c)(d) horizontal hysteresis cycles comparison*
 11 *for HDR Bearing element and Kikuchi Bearing element of the HDRB-AQ_{NEW} case study for a*
 12 *IM9 earthquake*

13 The previous figure highlights the differences between the two models. In particular, the *HDR*
 14 *Bearing Element* is able to capture the first cycle stiffness and the softening behaviour due to

1 repeated cycles, while the *Kikuchi Bearing Element* is calibrated on the third cycle because it is
2 not suitable to model the scragging behaviour. Moreover, the *HDR Bearing Element* shows re-
3 markable hardening behaviour at large strains, which does not take place with the *Kikuchi Bear-*
4 *ing Element* due to the $P-\Delta$ effects. Finally, it can be observed that the *Kikuchi* hysteresis cycle
5 does not show to a real buckling condition (i.e. the secant stiffness of the loading curve is al-
6 ways positive), but the lower stiffness usually leads to larger displacements. The vertical behav-
7 iour is also quite different. In this case, both the models account for the reduction of the vertical
8 stiffness for increasing horizontal displacements, but *HDR Bearing Element* recognise buckling
9 of the bearing (zero tangent stiffness in compression) while *Kikuchi Bearing Element* correctly
10 predict only a vertical stiffness reduction, without a real buckling reached (no vertical or hori-
11 zontal zero stiffness). The final result is a more realistic prediction of the isolation response for
12 *Kikuchi Bearing Element*. More details can be found in [Micozzi 2020].

13 Differently, no failures have been registered at *IM* levels from 1 to 9 for *HDRB-NA_{NEW}* (see Fig-
14 ure 13(a)). On the contrary, 18 failures (17 shear failures and 1 superstructure collapse) can be
15 observed at *IM10*. It should be observed that the isolation systems of the two examined cases
16 (*HDRB-AQ_{NEW}* and *HDRB-NA_{NEW}*) have been designed with the same margins towards the limit
17 conditions associated to the Seismic Code prescriptions (see Table 2). Thus, the differences in
18 terms of failure rates are mainly related to the different trends of the seismic hazard of the ex-
19 amined sites, in particular for seismic intensity levels larger than *IM6* (see Figure 27). Finally,
20 similarly to the case-study building located in L'Aquila, the results for *HDRB-NA_{NEW}* have been
21 re-processed considering a shear threshold equal to 4.0 (see Figure 13 (b)) obtaining a reduction
22 of the total number of failures at *IM10* (-4) but a significant increase of the number of cases of
23 superstructure collapse (+6).

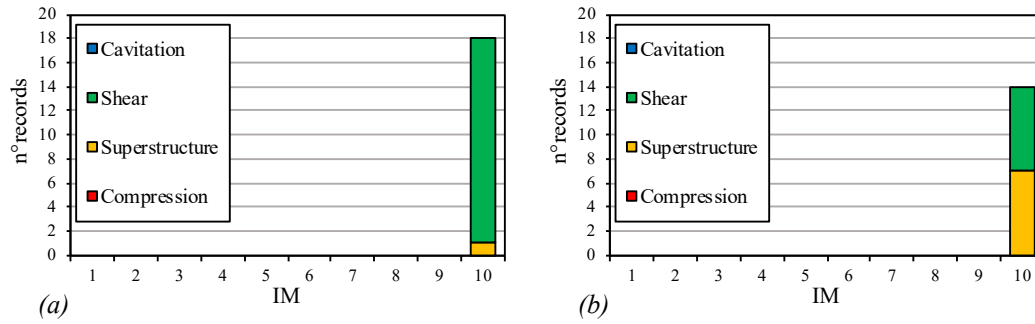
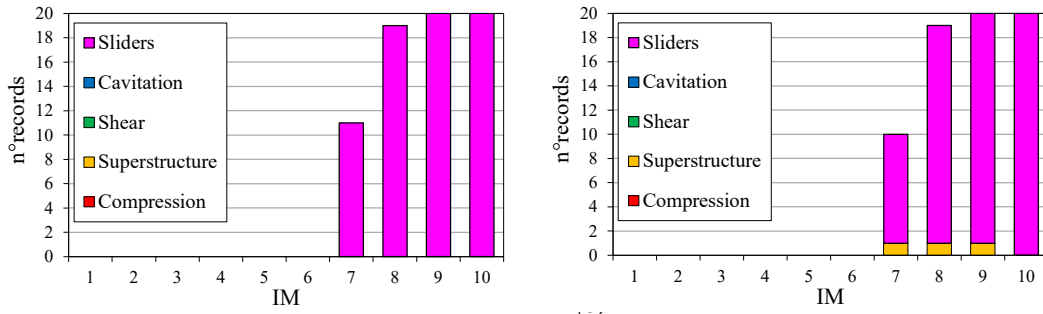


Figure 13. GC results for HDRB- NA_{NEW} : (a) shear limit 3.5, (b) shear limit 4.0

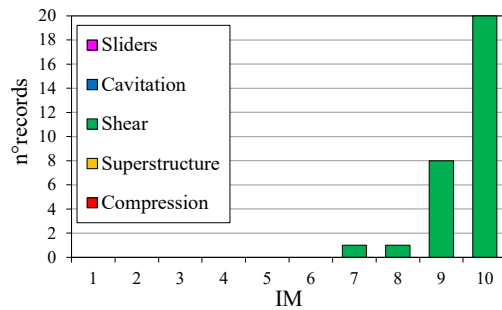
The results relevant to the GC performance level for new buildings equipped with HDRB+FSB isolation system are shown in Figure 14(a) and Figure 15(a). In both cases, no collapses are registered until IM7. However, while for HDRB+FSB- NA_{NEW} only one failure is registered at IM7 and IM8, for HDRB+FSB- AQ_{NEW} the total number of failures is already significant at IM7 (11), reaching 20 at IM9 and IM10. In both the cases, the isolation system collapse represents the prevalent collapse condition. However, while the attainment of the ultimate displacement of the sliders is the dominant failure mode for HDRB+FSB- AQ_{NEW} , the shear failure of HDRB is the dominant failure mode for HDRB+FSB- NA_{NEW} . This result can be ascribed to the ultimate displacement capacity of FSBs assumed for the two models respect to the HDRBs capacity. As done for HDRBs, two different allowable extra-stroke displacement are considered for FSBs, equal to $\alpha=1/2$ and $\alpha=2/3$ the slider diameter, corresponding to a limit contact pressure in the PTFE pads of around 60 MPa and 80 MPa, respectively. Results with these two different thresholds are shown in Figure 14 (a) and (b). For HDRB+FSB- AQ_{NEW} , the ultimate displacement capacity of FSBs turns out to be always lower than HDRBs while the contrary holds for HDRB+FSB- NA_{NEW} (see Table 8), although the design criteria are the same. The difference is the design safety margin towards shear failure of the commercial devices selected for the two cases (see Table 2). It is then clear that, for HDRB+FSB- AQ_{NEW} , even modifying the conventional failure criterion for FSBs (which is associated with the attainment of a critical contact pressure in the PTFE pads), the results in terms of total number of collapses are almost the same and the differences in terms of failure mode are marginal (see Figure 14). On the other hand, for

1 *HDRB+FSB-NA_{NEW}*, the ultimate displacement capacity of FSBs does not affect the results at all
 2 (see Figure 15).



3

4 *Figure 14. GC results for HDRB+FSB-AQ_{NEW}: (a) $\alpha=1/2$, (b) $\alpha=2/3$*



5

6 *Figure 15 GC results for HDRB+FSB-NA_{NEW} ($\alpha=1/2$)*

7

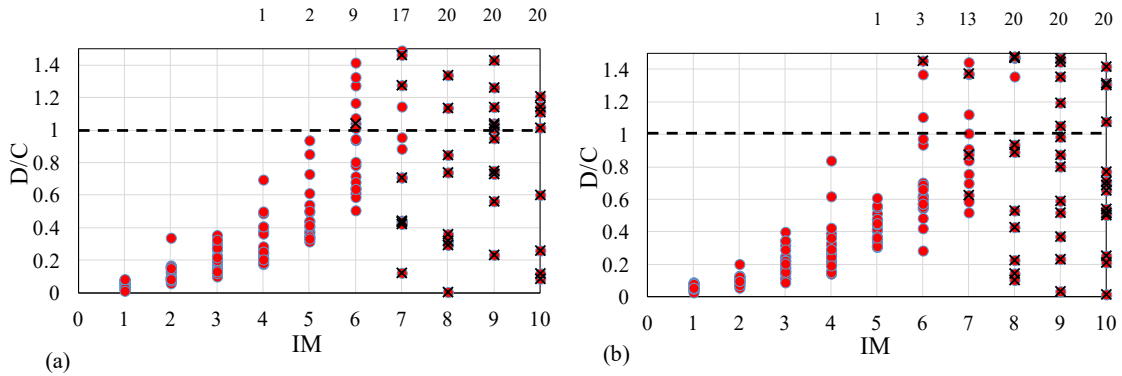
8 *Table 8. Ultimate displacement capacity of HDRBs and FSBs (mm units) for each case study*
 9 *with HDRB+FSB isolation system*

Case study	HDRB	FSB	
		$\alpha=1/2$	$\alpha=2/3$
HDRB+FSB-AQ _{EX}	532	475	517
HDRB+FSB-NA _{EX}	357	375	417
HDRB+FSB-AQ _{NEW}	616	525	567
HDRB+FSB-NA _{NEW}	357	375	417

10

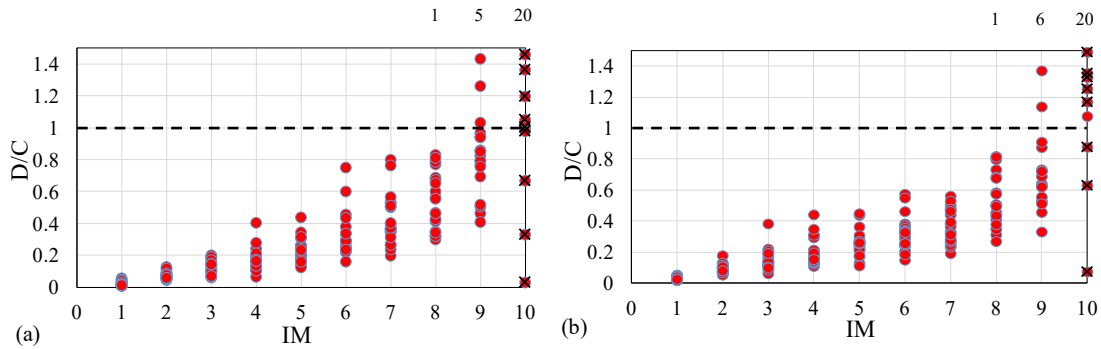
11 The results in terms of *UPD* performance level are reported in Figure 16 to Figure 19.
 12 For each *IM*, the *D/C* values registered during the analysis are provided. Moreover, the total
 13 number of failures ($D/C \geq 1$) is reported on the top of the diagrams. It is worth noting that, if the
 14 collapse of the isolation system is registered, also *UPD* is considered attained, whichever is the
 15 *D/C* ratio (spot highlighted with black X). As can be seen, no failures are registered until *IM4*
 16 for the case-studies located in L'Aquila (*HDRB-AQ_{NEW}* and *HDRB+FSB-AQ_{NEW}*), see Figure 16

1 and Figure 18, respectively. In particular, D/C values of the order of 0.2 (on average, consider-
 2 ing both directions) are obtained at IM_2 , representing the earthquake intensity level associated
 3 with the verification of the *Damage Limit State*, according to NTC2018. The different seismic
 4 hazard of the two sites significantly affects the results moving the first failures at IM_7 for the
 5 case studies located in Naples ($HDRB-NA_{NEW}$ and $HDRB+FSB-NA_{NEW}$), see Figure 17 and Fig-
 6 ure 19. Obviously, as observed for the previous case-studies, the D/C values registered at IM_2
 7 are much lower than 1, being of the order of 0.15 (on average, considering both directions).



8 ● Demand (D) calculated as Maximum Top Displacement registered during the analysis
 8 ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

9 *Figure 16. Displacement D/C ratio of the superstructure (UPD) for HDRB- AQ_{NEW} : (a) X direc-*
 10 *tion and (b) Y direction.*

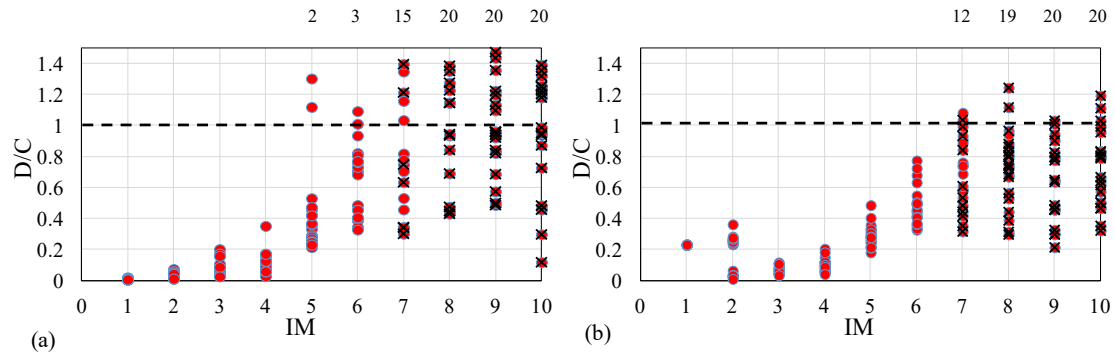


11 ● Demand (D) calculated as Maximum Top Displacement registered during the analysis
 11 ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

12 *Figure 17. Displacement D/C ratio of the superstructure (UPD) for HDRB- NA_{NEW} : (a) X direc-*
 13 *tion and (b) Y direction.*

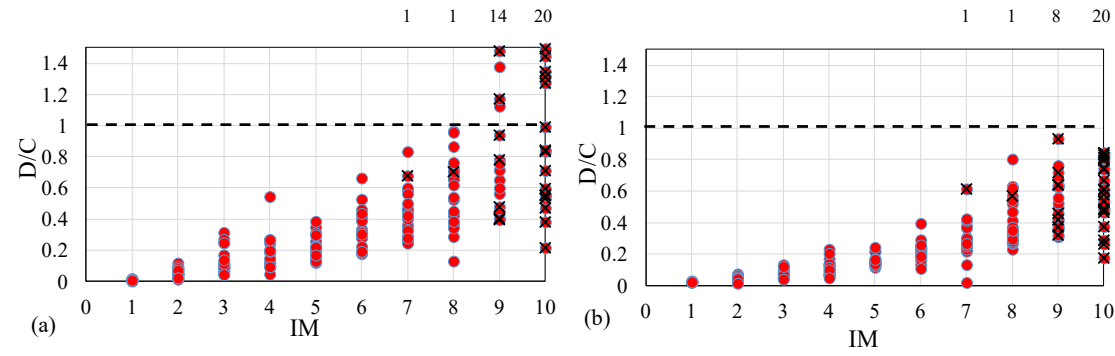
14 Definitely, large safety margins towards the *UPD* performance level are observed for all
 15 the examined case studies of new base-isolated buildings with rubber isolators, thus confirming
 16 the main outcomes presented in [Ragni et al., 2018a] where the same isolation systems were
 17 modelled using the *HDR Bearing Element*. In other words, the modelling assumptions (*Kikuchi*

1 *Bearing Element* instead of *HDR Bearing element*) seem to produce limited consequences on
 2 the results, in the range of low-to-medium horizontal displacements. Results concerning the *GC*
 3 performance level are also little affected in terms of number of collapses, although the collapse
 4 modes considerably change.



● Demand (D) calculated as Maximum Top Displacement registered during the analysis
 ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

5
 6 *Figure 18. Displacement D/C ratio of the superstructure (UPD) for HDRB+FSB-AQ_NEW: (a) X*
 7 *direction and (b) Y direction.*



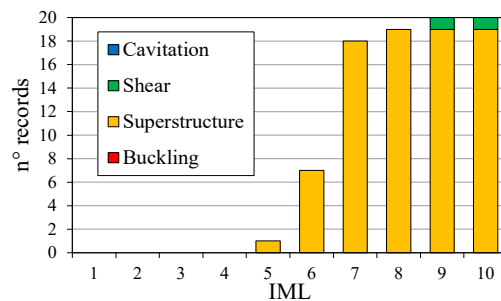
● Demand (D) calculated as Maximum Top Displacement registered during the analysis
 ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

8
 9 *Figure 19. Displacement D/C ratio of the superstructure (UPD) for HDRB+FSB-NA_NEW: (a) X*
 10 *direction and (b) Y direction.*

11
 12 *NTHA results for existing buildings*

13 As mentioned before (see “Case studies” section), using *HDRBs* only no solution are found for
 14 the retrofit of the existing building located in Naples, due to the very low shear force capacity of
 15 the superstructure. As a consequence, a single case-study building with *HDRBs* only (i.e.
 16 *HDRB-AQ_EX*) has been investigated.

1 Generally speaking, a limited number of failures is observed at *IM6* for all the examined case-
 2 studies (see Figure 20, Figure 21(a) and Figure 22), while such number becomes significant
 3 starting from *IM7*. Considering that the superstructure geometrical characteristics (number of
 4 floors, spans and plan layout) and the isolation system configuration of the new buildings (i.e.
 5 *HDRB-AQ_{NEW}*, *HDRB+FSB-AQ_{NEW}* and *HDRB+FSB-NA_{NEW}*) are equal to those of the corre-
 6 sponding existing building retrofitted with rubber-based isolation systems (i.e. *HDRB-AQ_{EX}*,
 7 *HDRB+FSB-AQ_{EX}* and *HDRB+FSB-NA_{EX}*), a comparison in terms of total number of collapses
 8 and failure modes is appropriate. First of all, the total number of collapses sensibly increases
 9 passing from new to existing buildings, especially at *IM6* and *IM7*. Moreover, as expected, a
 10 considerable increase of the number of cases with superstructure collapse are observed, for each
 11 *IM*. This is mainly ascribed to the lower ultimate displacement capacity of the existing buildings
 12 (see Table 4), due to lower ductility capacity of the RC frames and premature shear failure of
 13 some RC members. As a consequence, lower safety margin towards the global collapse of the
 14 superstructure are obtained for existing buildings, compared to new buildings.

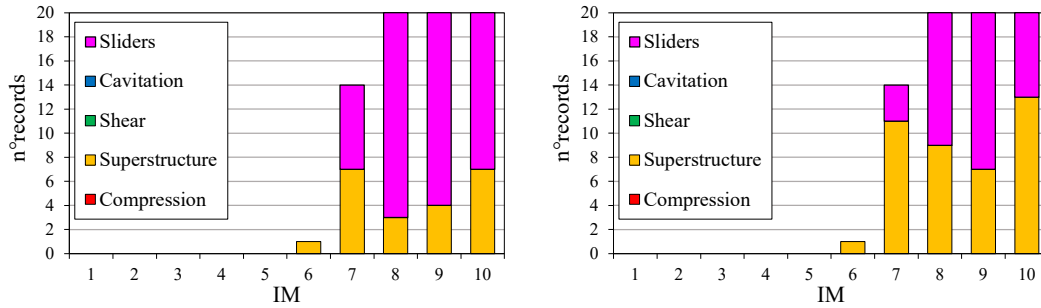


15
 16 *Figure 20. GC results for HDRB-AQ_{EX}*

17 Further specific considerations must be done for the *HDRB+FSB* case studies. Indeed, assuming
 18 an extra-stroke equal to 1/2 the slider diameter for *HDRB+FSB-AQ_{EX}* ($\alpha=1/2$ in Figure 21(a)),
 19 the collapse of sliders is still the dominant (first occurring) failure mode. Passing from $\alpha = 1/2$ to
 20 $\alpha = 2/3$ (see Figure 21(b)), the number of cases in which the superstructure collapse is the first
 21 occurring failure mode increases, although the total number of collapses remains substantially
 22 the same.

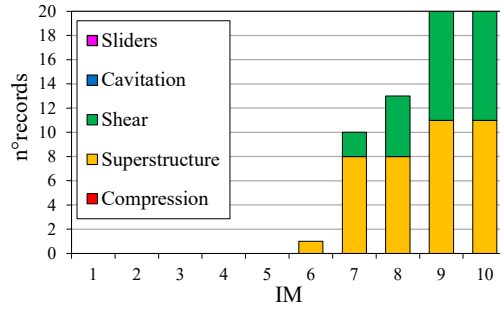
23 Figure 22 shows the results for *HDRB+FSB-NA_{EX}* case-study. The collapse of the superstructure

1 remains the dominant failure mode. For what concerns the isolation systems, however, like for
 2 *HDRB+FSB-NA_{NEW}*, the shear failure of *HDRBs* always anticipates the slider failure (see Table
 3 8).



4

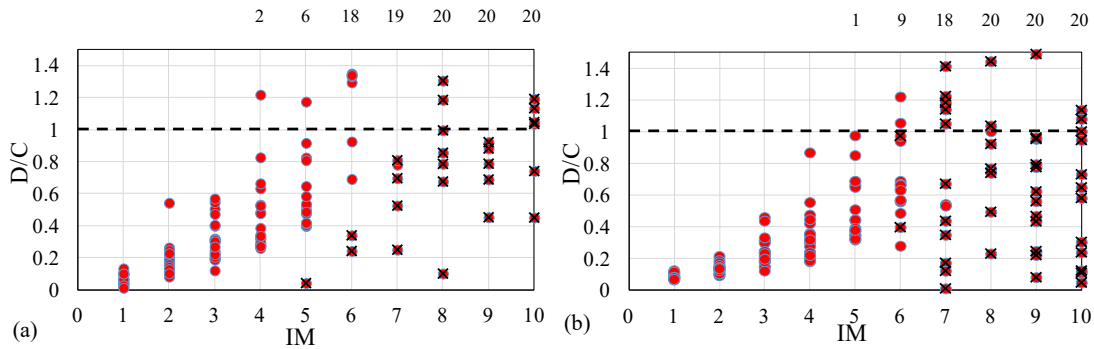
5 *Figure 21. GC results for HDRB+FSB-AQ_{EX} (a) $\alpha=1/2$ and (b) $\alpha=2/3$.*



6

7 *Figure 22. GC results for HDRB+FSB-NA_{EX} ($\alpha=1/2$).*

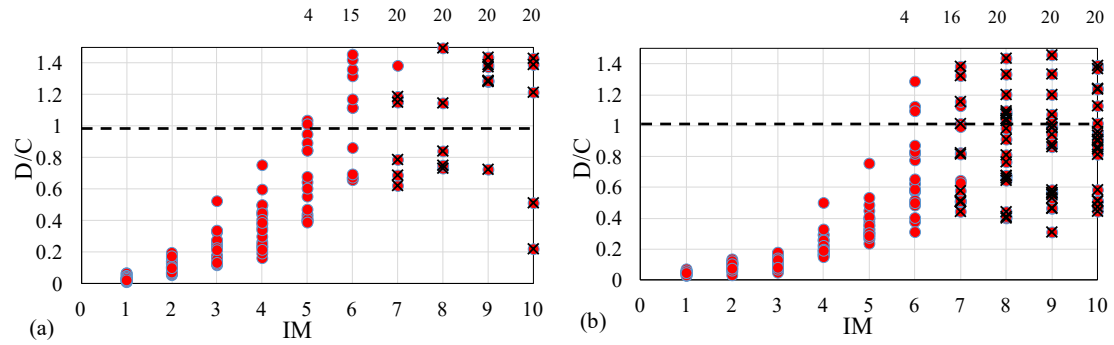
8 The results relevant to the UPD performance level are summarized in Figure 23 to Figure 25.
 9 Generally speaking, existing buildings retrofitted with rubber-based isolation systems works ef-
 10 fectively in limiting non-structural damage. Indeed, no failures are observed for seismic intensi-
 11 ties much higher than the *IM2*.



● Demand (D) calculated as Maximum Top Displacement registered during the analysis
 ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

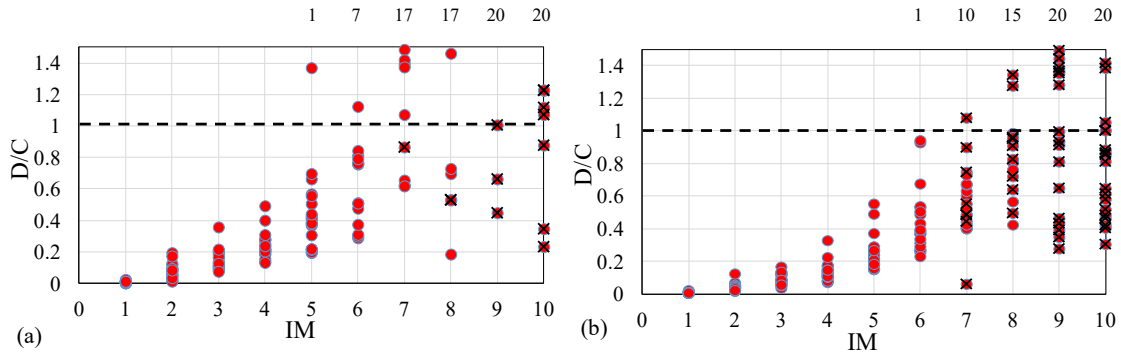
12

1 *Figure 23. Displacement D/C ratio of the superstructure (UPD) for HDRB-AQ_{EX}: (a) X direc-*
 2 *tion and (b) Y direction.*



- Demand (D) calculated as Maximum Top Displacement registered during the analysis
- ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

3
 4 *Figure 24. Displacement D/C ratio of the superstructure (UPD) for HDRB+FSB-AQ_{EX}: (a) X*
 5 *direction and (b) Y direction.*



- Demand (D) calculated as Maximum Top Displacement registered during the analysis
- ✕ Demand (D) calculated as Current Top Displacement associated to the system collapse

6
 7 *Figure 25. Displacement D/C ratio of the superstructure (UPD) for HDRB+FSB-NA_{EX}: (a) X*
 8 *direction and (b) Y direction.*

9 From the previous results, some preliminary conclusions can be drawn. First, as already
 10 argued in [Kitayama and Constantinou 2018] and [Shao et al. 2019], to increase the reliability
 11 of base-isolated buildings towards global collapse, the ultimate displacement/strength capacity
 12 of both the superstructure and isolation system must be enhanced. Second, while the
 13 strength/displacement capacity of the RC superstructure can be deemed to be well known,
 14 knowledge regarding the ultimate capacity of the isolation system should be deepen. For exam-
 15 ple, since the ultimate shear capacity of rubber bearings is currently not tested during the quali-
 16 fication process, mandatory tests may be introduced in the Codes in the near future [Nishi,
 17 2019]. Similarly, the extra-stroke behaviour of the sliders may be experimentally verified. Al-

ternatively, larger safety margins towards the ultimate displacement capacity of the isolation system should be prescribed.

Risk assessment

Results illustrated in the previous sections, concerning the structural system vulnerability, have been used to calculate the annual failure rate, λ_f , for both the *GC* and *UPD* performance levels (Figure 26) and for each case study under consideration, with the R2R software [Baraschino et al. 2019]. The procedure is the classical one reported in [Shome and Cornell, 1999] and corrected conservatively by assuming that for *IM* levels with return periods higher than 100000 years (the maximum considered for *MSA*) the failure is always attained, i.e. by adding 10^{-5} to the annual failure rate computed. More details can be found in [Iervolino et al. 2018]. In Figure 26, the blue markers refer to the new isolated buildings whereas the red ones to the retrofitted buildings. For any building model, light colours refer to past results, obtained by using the *HDR Bearing Element* [Ragni et al. 2018a, Cardone et al. 2019b], while dark colors to results obtained in this study.

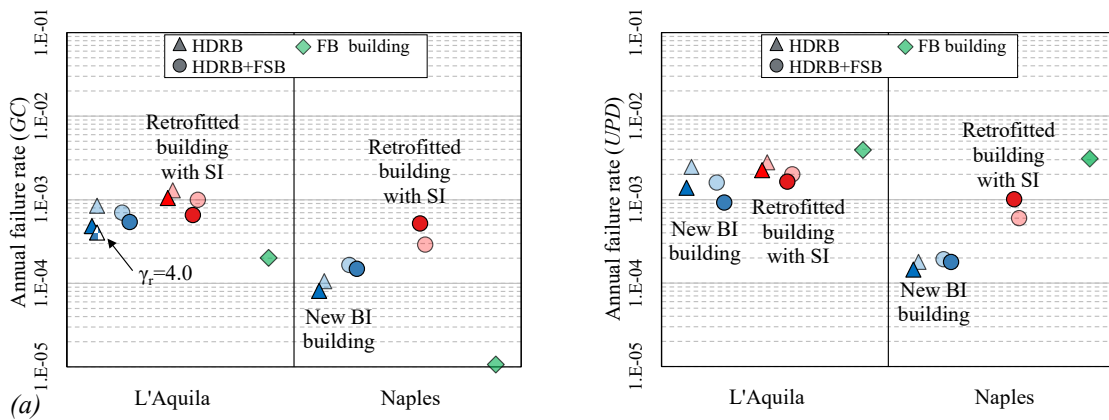
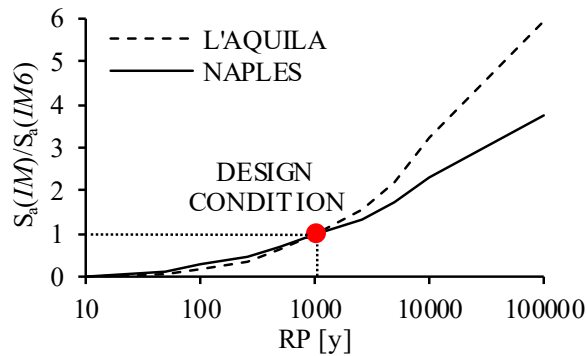


Figure 26. Annual failure rate of *GC* (a) and *UPD* (b) performance levels, for different case studies. Lighter markers represent results of past research. *BI*=base isolated, *SI*=seismically isolated, *FB*=fixed base

As can be seen, the annual failure rate in terms of *GC* has a limited variability within all isolated buildings, for a given site. For example, for high seismicity regions (L'Aquila) λ_f is around $\approx 10^{-3}$ for both new and retrofitted buildings with seismic isolation, whereas for the new buildings located in Naples it is around 10^{-4} . These results confirm that, even if the Code prescription should

1 lead to an equivalent level of security, the hazard of the site strongly influences the actual reliability level, as already highlighted by other studies developed within the RINTC project [Suzuki and Iervolino 2019] or dealing with the risk targeting approach [Fajfar 2018, Gkimpraxis et al. 2019, Gkimpraxis et al. 2020, Flora et al. 2020]. The influence of the seismic hazard on the annual failure rate is clearly explained by Figure 27 where the hazard curves of L'Aquila and Naples, normalized by the design seismic intensity level ($IM6$, $RP=1000y$), are shown.



7
8 *Figure 27. Normalized hazard for L'Aquila and Naples sites*

9 While the curves reported in Figure 27 are similar for return periods lower than 1000y, for higher return periods the hazard related to l'Aquila site increase faster than Naples site, leading to anticipated collapses.

12 For what concerns the annual failure rate relevant to the UPD performance level, it is worth noting that for the buildings located in L'Aquila the annual failure rate for retrofitted buildings is similar to that of new buildings. The reason is that the *SLD* buildings (existing building designed as fixed-base in compliance with the pre-96 Italian Seismic Code, considering a design base shear around 0.07 the weight of the building) has structural characteristics similar to the new isolated buildings. On the contrary, for the buildings located in Naples the strength of the existing *GLD* buildings (designed for gravity loads only) is significantly lower than the corresponding new isolated buildings. As a consequence, the annual failure rate relevant to the *UPD* performance level for existing buildings located in Naples is higher than for new isolated buildings.

22 A further remark about the *UPD* performance level is that the obtained annual failure rates are larger than those relevant to the *GC* performance level, but very close to them. This means that

1 the seismic performances of base-isolated buildings are very high in terms of damage control.
2 On the other hand, base-isolated buildings are less reliable than expected in terms of global col-
3 lapse. In other words, base-isolated buildings do not suffer any damage for a wide range of
4 seismic intensities, greater than the associated damage-control design intensity level, but when
5 damage develops the probability of collapse increases rapidly beyond the collapse-prevention
6 design intensity level.

7 For what concerns the modelling approach adopted for rubber isolators, Figure 26 com-
8 pares the annual failure rates derived, for the same base-isolated buildings, using the *HDR Bear-*
9 *ing Element* [Ragni et al. 2018a, Cardone et al. 2019b] with those obtained in this study using
10 the novel *Kikuchi Bearing Element*. In most of the cases, there is a slight tendency towards a re-
11 duction of the failure rates passing from the *HDR* to the *Kikuchi Bearing Element*, but differ-
12 ences are in most of the cases negligible both for *GC* and *UPD* performance levels.

13 Finally, comparing the annual failure rate of base-isolated buildings with the correspond-
14 ing values relevant to similar fixed-base buildings (6-storeys RC frame buildings with same ge-
15 ometry, same reference seismic Code, etc.), one can find that fixed-base structures have an an-
16 nual failure rate lower than base-isolated structures in terms of *GC* performance level, but sig-
17 nificantly larger in terms of *UPD* performance levels, in accordance with the findings of other
18 authors [Kitayama and Constantinou 2018, Shao et al. 2019]. Obviously, also in this case results
19 are significantly site-specific, i.e. strongly affected by the local seismic hazard.

20 At first sight, the obtained results point out that all base-isolated buildings are character-
21 ized by similar reliability levels for both *UPD* and *GC* performance levels, whereas fixed-base
22 structures exhibit a *UPD* reliability level lower than base-isolated buildings but a *GC* reliability
23 level significantly greater. Nevertheless, two important remarks should be done. The first one is
24 that in the *UPD* definition no considerations about the floor accelerations are made, because on-
25 ly the in-plane damage of infills is considered as monitored damaging parameter. Consequently,
26 the significant damage reduction due to the lower floor accelerations experienced by isolated
27 structures is not taken into account in this study. Some works concerning the out-of-plane be-
28 haviour of masonry infills are currently in progress [Gesualdi et al. 2020] within the RINTC

1 project and could be integrated in the UPD performance level in the near future, as also consid-
2 eration about other non-structural components (suspended ceilings, furniture, acceleration sensi-
3 tive devices).

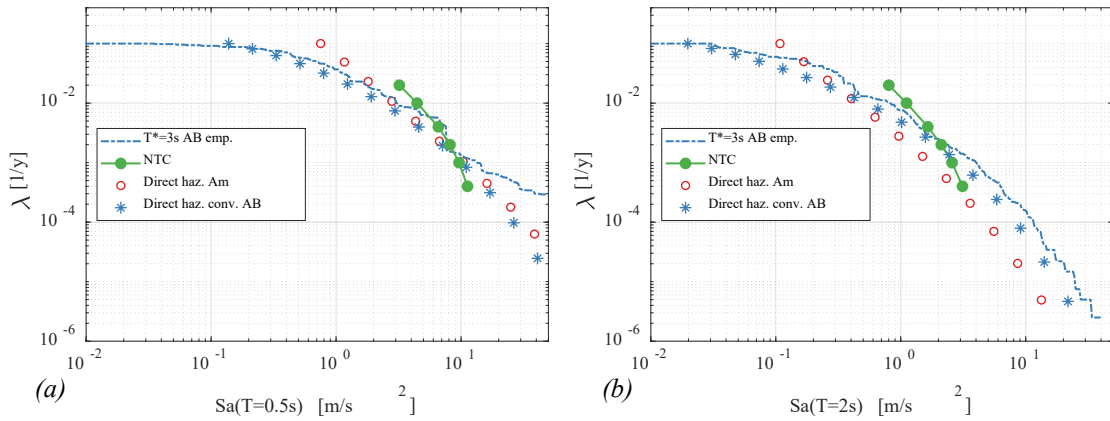
4 The second important remark is that the comparison previously carried out between
5 fixed-base and base-isolated structures has a qualitative nature because the two cases consider a
6 different hazard description. In details, different choices made for the *GMPE* used during the
7 hazard assessment may have affected the results. Indeed, for fixed-base structures the *GMPE* of
8 Ambraseys [*Ambraseys et al., 1996*] has been used. It is valid for periods lower than $T_{max} = 2s$
9 and uses as intensity measure the maximum spectral acceleration between the signals registered
10 in the two horizontal directions (usually referred to as Sa_{larger} , according to the notation of
11 [*Boore and Kishida, 2017*]). Since the isolation period is always higher than the period limit of
12 the *GMPE* of Ambraseys, the *GMPE* by Akkar and Bommer has been used for base-isolated
13 buildings, and as a consequence the geometrical mean of the spectral acceleration of the two
14 horizontal components (Sa_{GM}) has been used as intensity measure.

15 A bias between the Code hazard (considered in the design) and the effective hazard asso-
16 ciated with the seismic input (used for the risk assessment) may have further influenced the re-
17 sults.

18 For this reason, a comparison between the two hazard curves used in the analyses has
19 been carried out, as shown in Figure 28. An intensity measure conversion has been applied to
20 the *GMPE* of Akkar and Bommer, by using the relationships suggested in [*Beyer and Bommer*
21 *2006*], in order to compare the hazard curves derived with the two approaches. In particular, the
22 comparison between the direct hazard curves of Ambraseys and the converted direct hazard
23 curves of Akkar and Bommer is made for two reference periods, i.e. (a) $T=0.5$ s and (b) $T=2$ s.
24 From the comparison, it is evident that the two hazard curves are almost coincident for short pe-
25 riods, whereas for larger periods the Akkar and Bommer hazard curve, used for base-isolated
26 buildings, is significantly higher than the Ambraseys hazard curve used for fixed-base build-
27 ings. In the same figure, the “real” hazard curve used in the analyses has been also reported. It
28 has been directly derived from the sets of records selected for *NTHA*, following the procedure

1 illustrated in [Lin et al. 2013, NIST 2011]. It is worth noting that that even if the conditioning
2 period (T^*) is different from the selected periods of the hazard curves, empirical and direct haz-
3 ards are very close each other due to the insensitivity to the conditioning period of the empirical
4 hazard curves when CS-based ground motion selection is used [Lin et al. 2013]. It is then con-
5 firmed that the ground motion selection used for base-isolated structures, based on the *GMPE* of
6 Akkar and Bommer, is consistent with the direct hazard curve of Akkar and Bommer and larger
7 than the direct hazard curve of Ambraseys for large periods. It should be also noted that the se-
8 lected fixed-base building has an elastic period around $T=0.5$ s, however its effective period of
9 vibration significantly increases with the earthquake intensity level due to the strong nonlinear
10 behaviour of the RC frame [Lin et al. 2013]. As a consequence, the seismic hazard for large pe-
11 riods may have a significant influence on the seismic response of fixed-base buildings. Obvi-
12 ously, to exactly evaluate how much this difference in the hazard influences the results in terms
13 of the annual failure rate, fixed-based structures should be analysed with a set of ground mo-
14 tions consistent with the Akkar and Bommer hazard curve or, alternatively, both base-isolated
15 structures and fixed-base structures should be analysed using set of records consistent with a
16 hazard curve defined in a wide range of periods, e.g. defining the hazard curve by the Lanzano
17 *GMPE* [Lanzano et al. 2019] (see also [Micozzi 2020]).

18 Finally, in Figure 28 the Code hazard [CS.LL.PP. 2019] used in the design stage is also
19 reported (and called *NTC*). Although the *NTC* hazard curve is steeper than both the direct haz-
20 ard curves and the empirical ones, there is a quite good agreement between *NTC* hazard and
21 Akkar and Bommer hazard calculated from the record selection in the range of the design annu-
22 al rate of exceedance ($RP = 1000y$ or $\lambda=10^{-3}$).



1

2 *Figure 28. Hazard curves for the site of L'Aquila: (a) $S_a(T=0.5)$, (b) $S_a(T=2.0)$ directly com-*
 3 *puted from hazard assessment from Ambraseys (Am) and Akkar and Bommer (AB) GMPEs, em-*
 4 *pirically computed from record selection (emp) conditioned at $T^*=3s$ and code hazard (NTC)*

5 Conclusions

6 An insight on the response under different seismic intensity levels and on the seismic risk of
 7 rubber-based isolated buildings has been presented. The analyses have been performed within
 8 the *RINTC* research project on both new designed isolated buildings and existing RC buildings
 9 retrofitted with seismic isolation. The isolation systems have been designed in accordance with
 10 the current Italian Seismic Code and all the case studies have been assessed by means of multi-
 11 stripe nonlinear time history analysis, computing the annual failure rate for two performance
 12 levels, namely *Global Collapse (GC)* and *Usability Preventing Damage (UPD)*. A multi-criteria
 13 approach has been followed for the definition of the aforesaid performance levels as base-
 14 isolated buildings are in-series systems (being composed by the isolation system and the super-
 15 structure) and isolation devices can undergo different failure modes.

16 One of the most advanced numerical models currently available for the description of the
 17 nonlinear cyclic behaviour of *HDRBs* (namely the *Kikuchi Bearing Element*) has been used in
 18 the analyses, due to its capability of simulating the behaviour of *HDRBs* under large displace-
 19 ments and high axial loads. The model parameters have been calibrated against experimental
 20 results of an extensive experimental investigation.

21 The results of this study show that Code-conforming base-isolated structures work effec-
 22 tively in limiting the probability of damage, but they may exhibit a low margin with respect to
 23 the global collapse of structure, especially for high seismicity regions. On the other hand, code-

1 conforming fixed-base RC buildings show larger annual failure rates relevant to damage pre-
2 vention but lower annual failure rates regarding the collapse.

3 The new results obtained with the *Kikuchi Bearing element* does not seem to significantly
4 modify, at least for the examined case studies, the numerical prediction of the annuals failure
5 rates in terms of both *Global Collapse* and *Usability Preventing Damage* in comparison to al-
6 ready adopted model in past research, thus confirming the robustness of the analysis approach.

7 Finally, the results derived from risk assessment have been critically examined and com-
8 pared in the light of the different hazard definition for base-isolated and fixed-base structures. A
9 common hazard, suitable for both base-isolated and fixed-base structure, may lead to a reduced
10 gap between the annual failure rate in terms of *GC* performance level observed for base-isolated
11 and fixed-base structures. Alternatively, further investigations about the reliability of simplified
12 methods based on the fragility curves conversion should be carried out.

13 **Acknowledgements**

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15 2019-2021 research program, funded by the Italian Dept. of Civil Protection. The authors are
16 grateful to Prof. Iunio Iervolino (University of Naples, Federico II) for his valuable assistance in
17 deriving hazard curves and for the helpful discussion on risk assessment.

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