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#### Highlights

- Flood risk evaluation and **reduction** in **outdoor** built environments are investigated.
- **The proposed behavioural design-based** approach **jointly considers** evacuation **and** hydrodynamic scenarios
- Novel Key Performance Indicators are proposed
- Such approach is applied to a significant case study
- Risk **reduction** strategies are proposed and their effectiveness evaluated

# Assessing the flood risk to evacuees in outdoor built environments and relative risk reduction strategies

Gabriele Bernardini<sup>1</sup>, Fiorenza Finizio<sup>2</sup>, Matteo Postacchini<sup>2</sup>, Enrico Quagliarini<sup>1,\*</sup>

<sup>1</sup> DICEA Dept, Università Politecnica delle Marche, via Brecce Bianche 60131 Ancona

phone: +39 071 220 4248, mail: g.bernardini@univpm.it; e.quagliarini@univpm.it

<sup>2</sup> DICEA Dept, Università Politecnica delle Marche, via Brecce Bianche 60131 Ancona

phone: +39 071 220 4539, mail: m.postacchini@univpm.it

\*Corresponding author: e.quagliarini@univpm.it; phone: +39 071 220 4248

## Abstract

Climate-change induced disasters, like floods, are expected to increase in the future. In outdoor built environments, **flood risk to evacuees** depends on interactions between floodwater spreading, built environment features, flood-induced modifications, and individuals' reaction in emergency phases. Disaster risk reduction strategies should mitigate the immediate flood impacts and improve the community resilience, while being easy-to-implement and effectively supporting evacuees during the initial phases of the emergency. Simulation-based methodologies could support safety planners in evaluating the effectiveness of such strategies, especially if basing on a micro-scale-oriented approach that represents emergency interactions between each individual and the surrounding outdoor built environment. This study adopts an existing micro-scale simulator (FloopEDS) reproducing experimental-based flood evacuation behaviours. According to a behavioural design-based approach, **simulation** results focus on individual responses in the outdoor built environment through Key Performance Indicators (KPIs) aimed at providing evidence of critical interactions between evacuees, floodwaters and the outdoor built environment. A case study is selected by considering different flood scenarios to test such KPIs. Risk reduction solutions are then provided, and their effectiveness is checked by simulations. Results show the micro-scale and behavioural design-based approach capabilities in proposing multi-scenarios solutions (e.g.: architectural elements to support evacuees; emergency planning).

**Keywords:** flood risk; flood evacuation; risk assessment and planning; behavioural design; risk reduction strategies; flood hydrodynamics.

## 1 Introduction

Climate change-induced disasters, such as floods, are significantly affecting built environments and their probability is expected to increase in the future. Thus, disaster risk reduction, **which** is the series of activities aimed at preventing new and reducing existing disaster risk and managing residual risk<sup>1</sup>, is a key challenge for guaranteeing the safety of our communities, especially those placed in urban built environments [1–5]. Floods represent one of the most important disasters in existing and future cities, because of their effects on the built environment (defined as a system of buildings, underground spaces, open spaces such as streets and squares) and the people who live in them [3,6–13]. Flood risk assessment and reduction in urban areas are usually based on three factors [2,7,14–16]:

- Site hazard, due to both probability of occurrence of flood and location of urban areas in risk-prone regions;
- The vulnerability of the built environment to floodwater;
- Community's exposure, addressed in terms of exposed people (number and characterization) and social-economic factors.

In this general context, the evacuation and loss of life modelling in flood-affected urban scenarios was widely undertaken by previous studies in the last 15 years, due to the critical issues for individuals' safety that appear during the initial phases of such an emergency [17–25]. In fact, although safety planners can usually assume that exposed individuals know “what they must do” and “where they must go”, recent research has demonstrated that this assumption is incorrect [26]. During an evacuation, exposed individuals are affected by their own and the floodwaters interaction with the built environment. In addition, some of them could engage in “risky behaviours” during flood events, such as wasting time or trying to cross areas of fast-flowing and/or deep water.

These phenomena are relevant especially considering urban city **centres** because the number of exposed individuals is higher than in other **environments at risk of flooding** [8,16,22,24,27,28]. Furthermore, in urban areas, buildings can have a significant impact on floodwater depths and velocities [11,16,29,30]. For instance, where buildings are close together and roads are narrow, this can increase the velocity and depth of the floodwater thus increasing the flood hazard. In

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<sup>1</sup> <https://www.undrr.org/terminology/disaster-risk-reduction> , last access 12/04/2021

addition to damages to buildings and goods [2,7], the following conditions can increase the risk to exposed people [10,11,17,20,22,27,31–34]:

1. people are located in the outdoor built environment (e.g. the open spaces such as streets, squares) or in underground spaces (e.g. metro systems) at the beginning of the flood event;
2. people are evacuating in outdoor areas during the flood;
3. when people are not allowed to reach safer places inside a building adjacent to a flooded street.

These scenarios imply more significant threats for people due to the possibility to evacuate and to maintain stability while moving, and affect the overall number of casualties, especially in outdoor built environments [18,21,28,35–38]. Technicians of local authorities and Civil Protection Bodies can adopt Decision Support Systems (DSS) and related simulation tools for risk assessment purposes and for suggesting reliable risk reduction strategies [15,22,28,39–42]. Following such demand, many DSS and modelling tools have been provided over the time [9,11,20,24,25,28]. They have moved towards the inclusion of behavioural aspects characterizing experimental-based individual-floodwater interactions, so as to pursue reliable simulation and assessment approaches focusing on the evacuees' safety analysis as a paramount issue for flood risk [1,9,17,19,20,22,42].

### 1.1 Modelling flood evacuation for risk assessment and risk reduction strategies

The analysis of real-world flood evacuations outlined significant differences between behaviours in flood emergencies and other kinds of disasters (like earthquake, fire, general-purpose) [35,37,43]. From a qualitative point of view, evacuees are more likely to move toward immobile objects such as buildings, fences, handrails, during floods, unlike during other kinds of disasters [17,35,37,44–47]. Meanwhile, social identification issues lead evacuees to remain close to other neighbouring individuals and to share evacuation path decisions between evacuees in the same group. From a quantitative point of view, experimental activities (with volunteers or mannequins) mainly demonstrated that water depth  $D$  [m] and speed  $V$  [m] are key factors affecting the evacuees' motion on foot [21,37,48,49]. Individual features in terms of height, body mass, age and gender affect both the motion speed and the stability in floodwaters [21,22,38]. General rules were set to correlate floodwater characteristics and individuals' speed [48,49], as well as human body stability criteria for buoyancy or body failure (sliding and toppling under floodwaters effects) [35,38,50–52]. Such results show that flood risk assessment needs the adoption of models based on specific flood evacuation behaviours and related motion quantities, as suggested by behavioural design-based perspectives pursued by recent works [26,43]. Meanwhile, micro-scale modelling

approaches [22,53] can be preferred because they are able to represent these experimentally-based behaviours for each involved evacuee. In this sense, results from recent works, e.g. concerning  $D-V$  correlations, have been introduced in micro-scale pedestrian evacuation simulators and their capabilities have been thus demonstrated [17,18,22,25,54].

As for other kinds of disasters (e.g. earthquake, fire, tsunami) affecting the built environment [55–58], this behavioural design-based and micro-scale approach can support the development of flood emergency and evacuation simulators [22,26,43]. Safety designers can use these tools while performing risk assessment actions to evaluate the probable safety levels for evacuees. In particular, the response of “each individual receptor at risk” [24] can be assessed depending on the surrounding hazardous conditions each evacuee should face while moving in the flooded environment. Thus, risk reduction strategies aimed at supporting each individual in emergency conditions can be defined and promoted. Combined hydrodynamic-pedestrian evacuation simulators are used to this end [17,18,22,59]. The hydrodynamic model is aimed at reproducing the time evolution of the floodwater spreading (i.e. speed and depth) depending on the type of flood and the layout of the built environment [29,30]. The evacuation model represents individuals’ interactions with floodwaters, emergency behaviours and choices of the evacuees, depending on surrounding floodwater conditions [18,22,48].

Simulation results are then analysed by Key Performance Indicators (KPIs) to evaluate the safety levels of the evacuees in the emergency process [3,16,24,42,60]. Time-dependent risk assessment indices and GIS-based implementation were provided [10,34], while additional works also included KPIs relating to flood damage assessment of the built environment [2,16,41,61]. Considering behavioural design-based KPIs, evacuation models are widely used to estimate evacuation timing and the loss of life in the urban spaces, according to different Life Safety Models and hazard or risk rating metrics [10,11,22,34,54,62]. However, additional aspects of the evacuation process which are generally assessed by other kinds of evacuations (e.g. fire safety, earthquake), should be included in risk assessment analysis for the definition of risk indices in the outdoor built environment, such as the evacuation curve/flows, the use of open spaces, the presence of spontaneous gathering areas [1,17–19,56].

Outputs from the macro (territorial or urban) to the micro (building, street, square, underground space) scales are used for KPI-based evaluation of the effectiveness of risk reduction strategies aimed at reducing probable outcoming emergency interferences between the evacuees and the surrounding conditions by [1,17,19,22,24,27]:

- implementing modifications to the built environment, such as those relating to building components, emergency path configurations, and building systems as countermeasures during the flood;
- providing exposed people with information such as how to react when they receive a flood warning, where to go in case of an evacuation or which flood risk level can occur in the urban spaces, by also using emergency and wayfinding signage systems;

- adapting emergency management strategies to give direct support to evacuees (i.e. position of gathering areas; shelters allocation and relief distribution), if other “preventive” risk reduction solutions (e.g. flood barriers, drainage systems, early warning systems) fail.

Furthermore, reliable and widespread micro-scale solutions concerning the built environment elements were provided, including, for instance, stability-increasing solutions such as street furniture and handrails, or areas where to gather and wait for the rescuers’ arrival, such as raised platforms<sup>2</sup> [35,37,45]. Nevertheless, the assessment of their capabilities should be investigated in an organized manner through a KPIs-based approach and considering their impact from both micro and macro-scales.

## 1.2 Work aims and proposed approach

This work provides a micro-scale-oriented and behavioural design-based methodology for the assessment of flood risk and the evaluation of risk reduction strategies in outdoor built environments, focusing on open spaces such as streets and squares. The methodology investigates the initial phases of a flood emergency, that is the evacuation. According to this micro-scale standpoint [24], the proposed methodology is based on the joint simulation of hydrodynamic conditions and evacuation behaviours of each individual at risk, over space and time. Experimental-based flood evacuation behaviours are included in the evacuation simulation model. KPIs are provided to consider the effects of the interactions between each individual and the conditions of surrounding floodwaters and the outdoor built environment, at the: 1) micro-scale, that is for each street and square composing the analysed built environment, thus identifying homogenous risk areas; 2) macro-scale, that is for the whole outdoor built environment. Finally, the work proposes risk reduction solutions focused on micro-scale interventions that can [9,26,27,42,63]: a) directly support individuals in emergency conditions; b) be easily implemented and architecturally integrated into the outdoor built environment; c) have a sustainable use also in non-disaster conditions.

This whole approach is applied to the city centre of Senigallia (Italy), recently hit by a flood induced by long-duration rainfall and levee-failure [16]. Thanking the application to this case study, this work wants to mainly demonstrate the capabilities of the proposed risk assessment and risk reduction methodology, rather than deeply represent a specific real-world scenario.

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<sup>2</sup> see <https://www.rogersarchitects.com/mta-flood-mitigation-street-furniture/> for an example of architecturally-integrated solutions in urban areas (last access: 11/03/2021)

## 2 Phases and methods

This work was organized in three main phases. In the first phase, according to the micro-scale and behavioural design-based approach, criteria for emergency simulations were defined through the use of an existing hydrodynamic-evacuation simulator (Section 2.1). In the second phase, behavioural design-based KPIs were defined to evaluate risk levels in flood scenarios and propose risk reduction strategies (Section 2.2). Finally, a case study application was provided (Section 2.3) by analyzing different flood scenarios. Then, risk reduction strategies were proposed and verified by considering the riskiest scenario.

### 2.1 Simulation modelling

The combined simulator (FloodPEDS) is based on a hydrodynamic model which simulates floodwater conditions in an urban environment and a behavioural model which reproduces evacuees' choices (for details, see [17])<sup>3</sup>. The hydrodynamic model is based on the Nonlinear Shallow Water Equations (NSWEs hereafter). It is generally used for the representation of shallow water problems, that typically occur in the coastal area, in rivers or open channels, in the urban environment [64]. The behavioural model for evacuation relies on previous work providing a complete overview of organized evacuation behaviours during flood [37]. Starting from literature outcomes, this work included empirical analyses on real flood emergencies and proposed their related general rules for simulation. These rules were implemented in a micro-scale agent-based modelling approach, namely the Social Force Model (SFM) [65]. The SFM was adopted to describe the individual's motion in the built environment. In the SFM, attractive and repulsive forces are applied to each simulated individual to represent interactions among them and with the built environment, by also including: 1) attraction forces between the individuals and immobile objects in the built environment; 2) effects of individuals' speed reduction due to floodwaters  $D$  and  $V$ . The complete model description and the model notations are provided in Appendix A. A summary of the main modelling criteria is discussed in this section.

Firstly, it is considered that the maximum simulation time depends on the hydrodynamic conditions. In particular, when (almost) steady conditions within the domain are reached, the evacuation simulation can end. In fact, beyond this time limit, the evacuation conditions are not affected by variations in the hydrodynamic conditions during the time.

The hydrodynamic model provides the time evolution of water depth  $D(x,y,t)$  and depth-averaged flow speed  $V(x,y,t)$  in the outdoor built environment, where evacuees move. Two parameters can be defined, i.e. the specific force per unit

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<sup>3</sup> The executable file for the behavioural model ("beta version") is available in the journal supplementary materials, by including the case study scenario inputs and output dataset presented by this work.



width  $M(x,y,t)$  [ $\text{m}^3/\text{m}$ ] =  $(D \cdot V^2)/g + D^2/2$  (where  $g$  is the gravity acceleration [ $9.81\text{m/s}^2$ ]) and the descriptor of critical surrounding conditions for human body stability  $DV(x,y,t) = D(x,y,t) \cdot V(x,y,t)$  [ $\text{m}^2/\text{s}$ ] [18,35,38,48]. The SFM-based simulator for the evacuation process uses these inputs to determine [17,37,38]:

- the evacuees' speed depending on  $M$ ;
- his/her possibility of body stability loss, depending on  $DV$ ;
- the path choices, to minimize the  $M$  values and the distance towards a safe area where he/she can gather.

At the end of the simulation, the model provides data on:

- the *arrived evacuees*, as the individuals who gained a safe area;
- the *latecomers*, as the individuals (located along the outdoor built environment) who are still moving towards a safe area;
- *spontaneously gathering evacuees*, as the individuals who spontaneously gather in groups in areas where  $M$  values are lower than the ones of the surrounding outdoor spaces;
- the *casualties*, by considering the individuals who are exposed to floodwater conditions where they become unstable ( $DV > 1.20 \text{ m}^2/\text{s}$ ). In addition, the other thresholds for adults in good conditions having a height ( $h_i$ ) and mass ( $m_i$ ) product  $h_i m_i > 50$ , that are  $D(x,y,t) < 1.2\text{m}$  and  $V(x,y,t) < 3.2\text{m/s}$ , are still considered valid [31,38].

More details are offered in Appendix A.

The model considers a gaussian distribution for  $v_{pref,i}(x,y,t)$  (calculated as function of  $M(x,y,t)$ ) considering a standard deviation of  $0.2\text{m/s}$  [49,66]. In addition, an error for path selection (10%) is assumed to represent the evacuees who do not decide to select a safe area as an evacuation target because of safer local conditions [37,59]. Therefore, the evacuation process in each scenario is simulated more than once, and the mean values (and related standard deviation) are calculated [53,67]. For each scenario, the convergence of simulated behaviours is considered reached if the standard deviation associated with each output is lower than 10% [17]. At least 5 simulations per scenario have been run.

It is worthy of notice that the behavioural model assumptions imply some limitations concerning rules for the simulation of evacuees' speeds and stability in floodwater. In fact, this work is mainly focused on demonstrating the capabilities of the proposed micro-scale and behavioural design-based approach, rather than on representing specific individual features or case study conditions. We simulated the evacuation of adults (having  $h_i m_i > 50$ ) homogeneously defined [38], thus ignoring additional risk affecting individual features. Their safety threshold for stability is homogeneously considered too, thus focusing on the average response of such kind of evacuees. Specific individuals' features such as height,

body mass, age, gender or motion abilities, that affect both speeds and stability [21,22,49], were then not considered in the current simulations.

## 2.2 Behavioural Key Performance Indicators for scenarios comparisons and criteria for risk reduction strategies

Simulations were performed in different “*flood scenarios*” and “*risk reduction scenarios*”. Thus, KPIs compared the simulation results by considering [18,56,57]:

1. different **open spaces (such as streets and squares)** in the outdoor built environment, within the same “*flood scenario*”, to **point out** where to implement possible risk reduction strategies;
2. different “*risk reduction scenarios*”, to evaluate their improvement of safety conditions.

Two groups of KPIs were proposed. *KPIs relating to the evacuation process* (Section 2.2.1) represent the effects of individual-floodwater interactions on the evacuation. According to the stochastic evacuation simulation approach described in Section 2.1, each KPI was estimated on the simulation outputs and then it was associated at least to its average value and its standard deviation. *KPIs relates to the built environment* (the whole simulation area or a part of it, e.g. a street or a square) trace the risk levels depending on the specific floodwater characterization and **the adopted** risk reduction strategies (Section 2.2.2). The KPIs notations are provided in Appendix B.

### 2.2.1 KPIs relating to the evacuation process

The overall *number of evacuees who have arrived in a safe area within the simulation time*  $P_e$  [persons] describes the number of people who can reach effective safe conditions within the simulation time. This KPI can be also represented in percentage terms  $P_{e,\%}$  [%], with respect to the initial people hosted in the outdoor built environment.  $P_e$  should be maximized to improve the **evacuees’** safety [35,57,68,69].  $P_e$  related to each safe area in the built environment assesses if it is underused/not used at all by the evacuees. The *difference in arriving evacuees* [%] describes the use of each safe areas depending on the individuals’ selection of paths and safe areas. In fact, some individuals can spontaneously try to move towards a safe area different from the initially selected one because of local floodwater levels conditions [37], as reported in the model description in Appendix A. Thus, the *difference in arriving evacuees* [%] was calculated as the percentage difference between the number of evacuees reaching the safe area and the number of evacuees who “initially chose” the safe area.

The evacuation time  $T_e$  [s] is linked to  $P_e$  [18,70]. The average evacuation time  $T_{e,0.50}$  refers to the 50<sup>th</sup> percentile of evacuation time and represents the median trend in the evacuation process. According to Section 2.1, local conditions altering simulation results for the early and latecomers exist [53,71], e.g. the initial positions of individuals, as well as uncertainties in  $v_{pref,i}(x, y, t)$  and in path selection. To avoid such behavioural effects, the first 5% and last 5% of arrived evacuees were excluded in evacuation time estimation. To this end, the evacuation times [s] of the individuals' 5<sup>th</sup> ( $T_{e,0.05}$ ) and 95<sup>th</sup> ( $T_{e,0.95}$ ) percentile were additionally calculated.

The overall average evacuation curve represents the number of arrived evacuees  $P_e(t)$  during the time (graphical visualization) [67,72]. Average, maximum and minimum evacuation curves were assessed to graphically express the deviation within the sample. Moreover, the evacuation curve for each safe area was calculated.

The effective average flow of evacuees arrived in a safe area  $F_e$  [persons/s] describes the swiftness of the evacuation process [73,74].  $F_e$  was calculated as the ratio between the number of arrived individuals ( $P_e=5\%$ ,  $P_e=50\%$  and  $P_e=95\%$ ) and the related time difference between  $T_{e,0.05}$  and  $T_{e,0.50}$  (for  $P_e=50\%$ ;  $F_{e,0.50}$ ) or  $T_{e,0.95}$  (for  $P_e=95\%$ ;  $F_{e,0.95}$ ).  $F_{e,0.95}$  resumes the overall process swiftness.  $F_{e,0.50}$  shows the median trend in the evacuation flows, determining the slope of the evacuation curve in its central part. These values should be maximized to speed up the evacuation and to increase the safety of individuals (by reducing their exposure to potentially risky floodwaters conditions). The value was evaluated for the whole process and for each safe area.

The number of out-of-time evacuees (including casualties)  $P_O$  [persons] shows how many evacuees cannot reach a gathering area within the simulation time.  $P_O$  was also expressed in percentage terms ( $P_{O,\%}$  [%]). Moreover,  $P_{O,street}$  provides the number of out-of-time evacuees for each space (e.g. street) in the outdoor built environment. According to the rules for evacuation stop in the behavioural simulation model (see Section 2.1) [35,68], it could be possible to identify the percentages of out-of-time evacuees considering :

- latecomers by  $P_{O,la}$  [%], which are the evacuees located near a safe area or in not risky condition at the end of the simulation (i.e. lowest  $DV$  levels);
- spontaneous gathering evacuees by  $P_{O,sp}$  [%];
- casualties (considering evacuees exposed to  $DV > 1.2 \text{ m}^2/\text{s}$ ) by  $P_{O,ca}$  [%].

Such values were calculated for each street (e.g.  $P_{O,ca,street}$ ) in both absolute and relative terms. Latecomers, spontaneous gathering evacuees and casualties were represented on the outdoor built environment layout to graphically show the areas affected by such phenomena. In general terms,  $P_O$  should be minimized as long as it is complementary to  $P_e$ . In particular,  $P_{O,ca}$  should be primarily minimized.

The *street crowding*  $P_{cr,street}$  [persons] specifies how many evacuees go through a given street in the urban layout while evacuating [57,73,75]. The higher  $P_{cr,street}$ , the higher the number of individuals who can be exposed to local floodwater conditions and to possible individual-individual interactions (by including queuing phenomena).  $P_{cr,street,\%}$  [%] was normalized by the maximum  $P_{cr,street}$  value within the simulated area.

### 2.2.2 KPIs relating to the built environment

The *KPIs relating to the built environment* were calculated for the entire simulation area or for a single outdoor space (i.e. a street, a square). They trace the risk level depending on the main behavioural design-based risk factors (i.e. *out-of-time evacuees*; *DV* levels; crowding levels), and with respect to the whole simulation time. To support the prioritization of interventions in the built environment, they were also offered via risk maps of the built environment [7,60,76].

The complete description of these KPIs is reported in Appendix C. The following dimensionless KPIs were considered:

- $R_{area,scen}$  [-] and  $R_{street,scen}$  [-] respectively assess the conditions of the whole area and of a single outdoor space. They were evaluated considering the following comparable scenarios sets: (a) the same implemented risk reduction solutions and different floodwater events; (b) the same floodwater event and different risk reduction solutions. They define the worst scenarios within the comparable ones and investigate the effectiveness of risk-reduction solutions;
- $R_{street}$  [-] assesses the risk indices of a given outdoor space in comparison to other streets and squares, by considering a given scenario. In particular, it highlights the riskiest parts of the outdoor built environment under certain hydrodynamic conditions. Thus, it **points out** where risk reduction strategies should be focused.

These KPIs were based on three main behavioural design-based factors: (a) the risk for *out-of-time evacuees*, due to the presence of *casualties*, *latecomers* and *spontaneously gathering evacuees* (e.g., for the whole area  $R_{O,area,scen}$ ); (b) the risk due to the floodwater level in the built environment (e.g., for the whole area  $R_{DV,area,scen}$ ); (c) the crowding risk, which considers how many evacuees can move in the built environment or in a street/square into it (e.g., for the whole area  $R_{cr,area,scen}$ ).

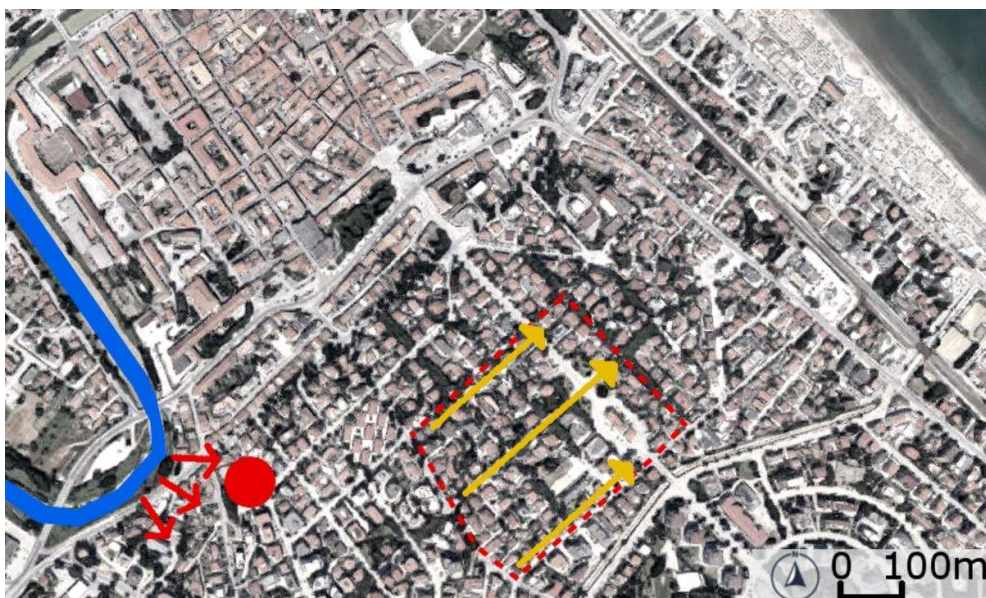
These risk factors were combined according to the Analytical Hierarchy Process (AHP) methodology [10,77,78], since they do not necessarily have the same relevance. The selected KPIs were pairwise compared in the AHP, **basing on Saaty's** relative importance **scale** (1-equal to 9-extreme). **This procedure allows calculating the** related priority weights, according to the principal eigenvector of the decision matrix in the AHP method. The proposed priority weights were **considered acceptable** if the Ratio of Consistency RC associated with the performed pairwise comparison was lower than 10%. The

lower RC, the more confident the priority weight estimation. As a result of the AHP application, KPIs always range from 0 to 1 (which corresponds to the maximum risk). KPIs were based on a two-level Decision Hierarchy. A similar approach was already used in flood risk assessment (e.g. [10]) and also in other kinds of disasters in outdoor built environments (e.g. earthquakes [79]).

### 2.3 Case study definition

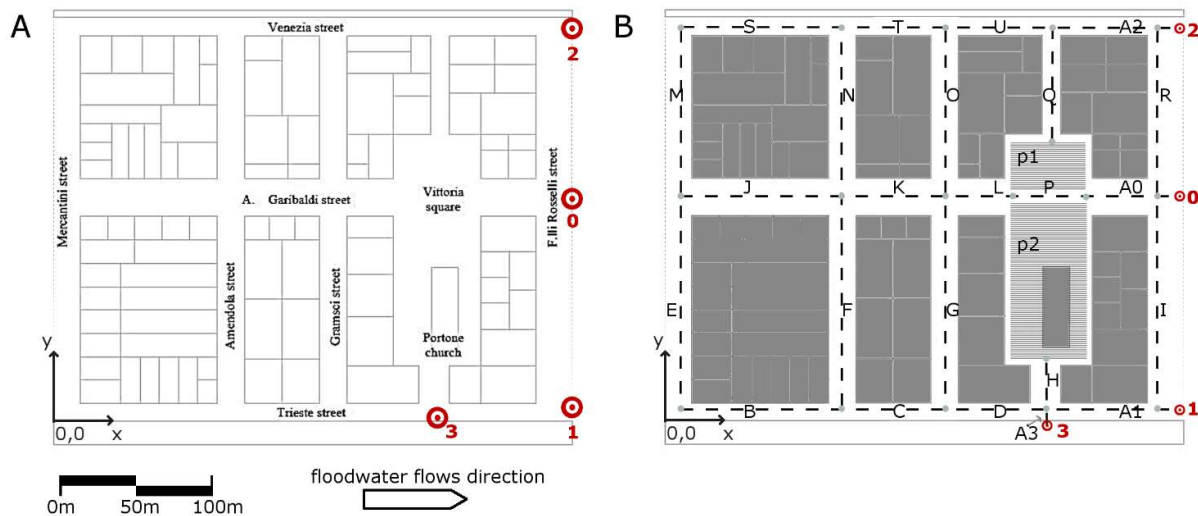
An area in the city centre of Senigallia (AN, Italy), recently affected by floods, was chosen as a case study. Senigallia is located along the Adriatic coastline and built on a floodplain, near the estuary of the Misa River. Moreover, it has a compact urban fabric, characterized by scarcely permeable surfaces and narrow streets. As a consequence, the water spreading during floods flows like in an open compound channel.

Figure 1 shows the location of the area (red dashed rectangle) in the urban fabric. Figure 1 also graphically shows: the main streets along the upstream-downstream direction (yellow arrows); a portion of the Misa River (in blue), which is the flood source; the Anna Frank gardens (red circle), discussed in the following as source locations of the used boundary conditions. This area was chosen because of the relevant inundation that occurred in May 2014, especially affecting the main central street in the built environment (A. Garibaldi street, in Figure 2-A) and the upstream part of the domain. The choice of such a scenario (which is representative of the urban built environment as discussed above) also allowed easily retrieving input data on geometrical, hydrodynamics and exposed people, since it was investigated in previous works (e.g. [17,80]).



**Figure 1.** Overview of the case-study area: domain limits (red dashed perimeter); main upstream-downstream streets (yellow arrows); the Misa river as the source of the flood (blue line and red arrows); the place where data were collected during the 2014 flood (red circle, *Anna Frank* gardens). Adapted from Google Maps, last access: 20/10/2019.

The geometrical layout of the urban scenario (also used in FlooPEDS preliminary tests [17]) was divided into a series of rectangular **subdomains**. In each subdomain, floodwaters conditions could be taken as homogeneous, according to the solver structured grid with spatial resolution of  $(\Delta x, \Delta y) = (0.8, 0.5)\text{m}$ . Figure 2 traces the domain, having an area of about  $90,000\text{ m}^2$  ( $x = [0, 350]\text{m}$ ;  $y = [0, 265]\text{m}$ ). Figure 2-B also shows the division of the outdoor built environment into streets (dashed lines) and squares (hatched rectangles), and the position of the safe areas. Comparing Figure 2-A and Figure 2-B, the three main streets along the upstream-downstream direction (yellow lines in Figure 1) are: A. Garibaldi street as the outdoor spaces (i.e. streets) J, K and L, Trieste street as B, C, D, A1; Venezia street as S, T, U, A2.



**Figure 2.** Simplified domain modelling: (a) a general overview of the simulation area limits (dashed light grey lines) by including domain origin, metric scale, floodwater flows main direction (arrow on the bottom), place names and safe areas with the related identification number (red circles); (b) streets (dashed lines connecting two grey circles) and squares (hatched areas) with related identification codes, and buildings (grey blocks).

Two flood scenarios were simulated: (1) levee-failure (Section 2.3.1) and (2) river-overflow (Section 2.3.2). The latter case was based on existing data and statistics, although extreme and precautionary assumptions were made. The hydrodynamic conditions were imposed at the upstream boundary and linearly varied between each of the steps according to



the specific assumptions (see  $D$  and  $V$  reported in Table 1 and Table 2). A reflecting condition was imposed both laterally and at the downstream boundary.

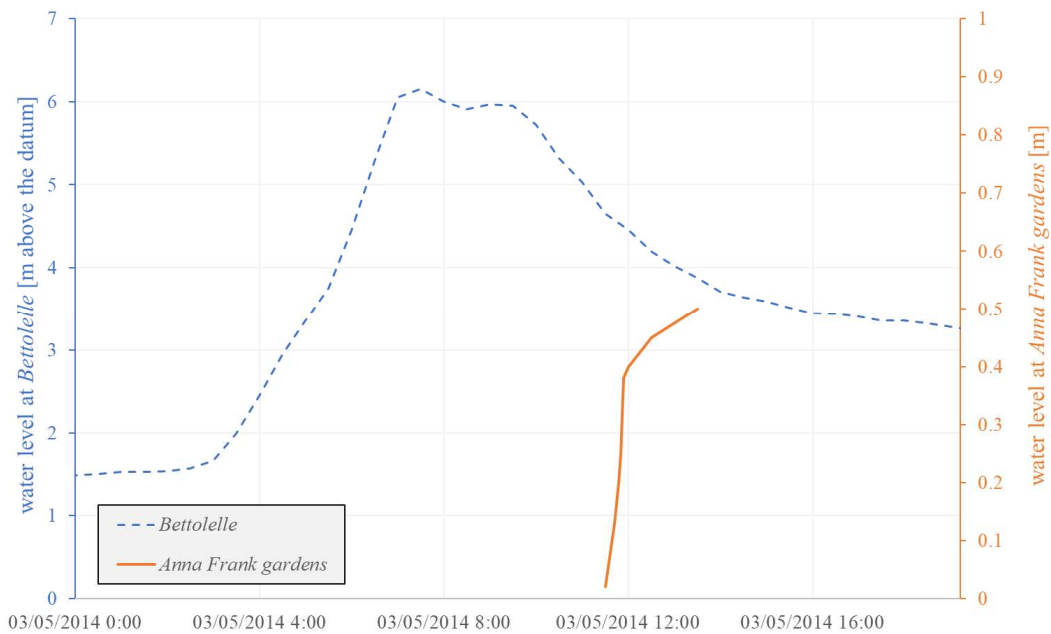
The input data about the evacuation scenario are described in Section 2.3.3. Finally, KPIs application for scenarios comparison is described in Section 2.3.4.

### 2.3.1 Levee-failure scenario

Information on the levee-failure was collected from analyses on the actual flood features (water depth  $D$  and speed  $V$ ) observed during the event in the case study area. The event time series were reconstructed from videos recorded during the 2014 flood in the *Anna Frank* gardens (red-circled area in Figure 1, located close to both river and study area). A reduced distance (about 300m) exists between such location and the west boundary of the numerical domain. Thus, hydrodynamic simulations used these recorded time series. Input data concerning  $D$  and  $V$  recorded on May 3<sup>rd</sup>, 2014 from 11.30 am to 1.30 pm (see Table 1) were assigned as upstream boundary conditions. Figure 3 shows the hydrograph referring to the most downstream available water level measurements (the hydrometer is located at *Bettolelle* station, which is about 7 km far from the case-study area).

**Table 1** Levee-failure input data used as boundary conditions (at  $y=0$  in Figure 2) for the hydrodynamic simulations

$t$ [s]	$D$ [m]	$V$ [m/s]
0	0.02	0.06
720	0.13	0.31
1080	0.20	0.45
1200	0.25	0.57
1440	0.38	0.85
1800	0.40	0.90
3600	0.45	1.01
7200	0.50	1.12



**Figure 3.** Water level evolution during the May 2014 flood: hydrograph (dashed line) recorded at *Bettollelle* station; water level chosen as the boundary condition in the case-study domain (solid line), reconstructed using the data recorded at the *Anna Frank* gardens (see red circle in Figure 1; data are offered by Table 1).

### 2.3.2 River-overflow scenario

We assumed that an overflow hazard might characterize a river stretch close to the city centre (see Figure 1) where:

- (a) the cross-section significantly reduces up to a width smaller than 20m, depending on the flow condition; and (b) the flow reaches the bank almost perpendicularly.

Boundary conditions were based on analyses aimed at identifying the return period of the Misa River discharge. Depending on the method applied for such estimate<sup>4</sup>, the mean discharge ranges between 400 and 600 m<sup>3</sup>/s for return periods  $T_R=(100-500)$  years (e.g., [80]), while the maximum discharge ranges between 300 and 900 m<sup>3</sup>/s for  $T_R=(50-200)$  years. Under the worst-case scenarios, the highest water level can be assumed for this reach of the river (e.g. about 2m over the right bank over which overflow is assumed to occur). Such assumption is consistent with: 1) the features of the left bank, which is some meters higher than the right bank; 2) a discharge related to a large return period, i.e. of the order of 900

<sup>4</sup> *Autorità di Bacino Regione Marche, Delibera C.I. n. 67/2016, Elaborato "A"*; website: [http://www.regione.marche.it/Portals/0/Paesaggio\\_Territorio\\_Urbanistica/AdB/PAIMarche/DelComIst/allegati/del160325\\_67\\_ElaboratoA.pdf](http://www.regione.marche.it/Portals/0/Paesaggio_Territorio_Urbanistica/AdB/PAIMarche/DelComIst/allegati/del160325_67_ElaboratoA.pdf). Hydrological and hydraulic report for the construction of the hydropower plant "Bettollelle" in the Misa River; website: <http://www.ambiente.marche.it/Portals/0/Ambiente/Pubblicazioni/V00508/6fb572e4-92eb-4ba3-b225-314fb2f15852.pdf> (last access 21/11/2019)



m<sup>3</sup>/s. It was thus assumed that the water overflows through a bank length  $b=(110\div120)$ m, with a head over the bank  $h_I=2$ m, which was taken as constant along  $b$ . As a consequence, the geometry of the bank was provided as almost rectangular. The water discharge  $Q$  flowing down from the bank was estimated using the typical law applied to broad-crested weirs.  $Q$  was assumed as proportional to both  $b$  and  $h_I^{3/2}$  as in Equation 12:

$$Q = 1.7C_d b \left( h_I + \frac{v_I^2}{2g} \right)^{3/2} \quad (12)$$

where  $v_I$  is the flow velocity and  $C_d$  is the discharge coefficient. A suitable choice of the involved terms (e.g.,  $v_I \sim 5$ m/s during flood conditions,  $C_d \sim 0.6$ ) leads to a discharge equal to about 700m<sup>3</sup>/s.

Finally, the overflowing discharge was completely transferred to the study area (about 600m far from the overflow location), i.e. neglecting dissipation and water infiltration. Although strong, such an assumption represents an ideal extreme condition. It allows properly understanding the benefits of risk reduction strategies when the flood condition is significantly different from the levee-failure one.

The overflow phenomenon can be thought significantly rapid along the rising limb of the hydrograph. Table 2 reports the selected input data ( $D$ ,  $v$ ) and the assumed discharge  $Q$  at each stage. Depending on the water depth at the upstream boundary ( $D=1.1$ m) and domain width (265 m along the  $y$ -direction), the velocity modulus varies between 2.30 and 2.40 m/s.

**Table 2** River-overflow input data used as boundary conditions (at  $y=0$  in Figure 2-A) for the hydrodynamic simulations

$t$ [s]	$Q$ [m <sup>3</sup> /s]	$D$ [m]	$v$ [m/s]
0	670	1.10	2.30
50	685	1.10	2.35
600	700	1.10	2.40

### 2.3.3 Evacuation simulation setup for the case study

Each evacuation simulation involved 300 individuals to represent the number of individuals located in adjacent buildings. In particular, for each building, the building surface [m<sup>2</sup>] and the intended use (i.e.: residential, commercial, other public buildings) were assessed through an infield survey. Then, the following occupant load values were applied

with respect to each intended use according to the Italian Fire Safety Code [81]: residential, 0.05pp/m<sup>2</sup>; commercial, 0.4 pp/m<sup>2</sup>; other public buildings, 0.7pp/m<sup>2</sup>. This process allowed calculating the possible occupant capacity for each building. According to a conservative approach, individuals were considered as located outdoor (i.e. near the building access) and not able to enter the nearest building and move vertically.

When the evacuation started, individuals tried to move towards the safe areas according to the modelling criteria (see Section 2.1 and Appendix A). Safe areas were characterized by ground elevations and were placed at the downstream area exits, as described in [17,18]. They are shown in Figure 2 and represent the evacuation target for the evacuees.

### 2.3.4 KPIs application for scenarios comparison

KPIs defined in Section 2.2 were firstly applied to derive the outdoor built environment safety in the pre-strategies proposal scenario (in the following, the “*original scenario*”). The most critical floodwater conditions between the analyzed flood scenarios (levee-failure and river-overflow) were retrieved. The outcoming flood scenario was considered for the proposal of risk reduction strategies. Finally, such strategies were implemented within the outdoor built environment and their effectiveness was evaluated by comparing KPIs. Equation 11 shows the percentage difference  $dKPI_{red-pre}$  [%] of a given KPI by considering the *original scenario* ( $KPI_{pre}$ ) in respect to the one with risk reduction strategies ( $KPI_{red}$ ) [57]:

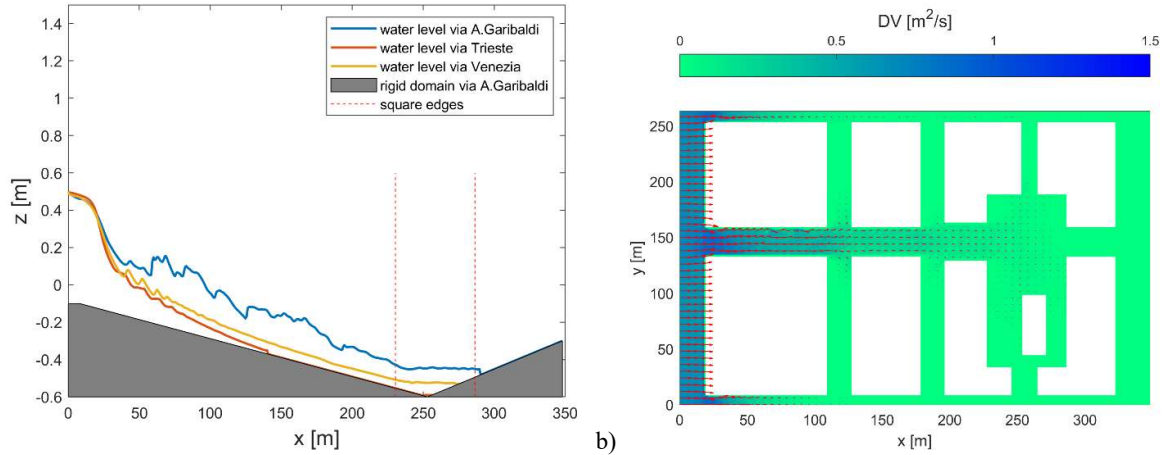
$$dKPI_{red-pre} = \frac{KPI_{red} - KPI_{pre}}{KPI_{pre}} \cdot 100[\%] \quad (11)$$

For risk indices  $R_{area,scen}$  and  $R_{street,scen}$ , negative  $dKPI_{red-pre}$  values imply a reduction of the risk levels.

## 3 Results

### 3.1 Flood scenarios

Figure 4 shows the hydrodynamic outputs for the levee-failure scenario. In this scenario, the maximum discharge (peak condition) occurs after 7200s. Both panels of Figure 4 refer to this moment in hydrodynamic simulation results. Figure 4-A shows the streamwise evolution of the water-surface profile along the West-East streets of the analysed domain (yellow lines in Figure 1). Figure 4-B illustrates the top view of the  $DV$  map overlapped to the numerical domain.



**Figure 4.** Hydrodynamic results of the levee-failure simulation after 7200s (peak condition): a) streamwise sections; b)  $DV$  map (red arrows are the speed vectors; buildings-obstacles are the white areas).

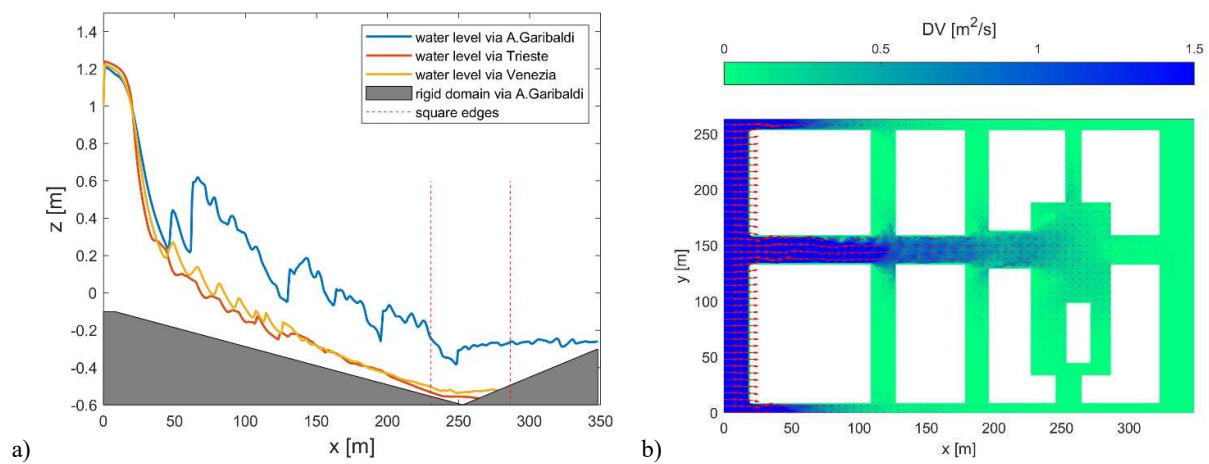
In more details, the flow depth is higher along the streets J, K, L, A0 (blue line in Figure 4-A) than along the other two parallel streets, that are streets B, C, D, A1 (red line) and streets S, T, U, A2 (yellow line). The colour map shown in Figure 4-B confirms this result: larger values of  $DV$  are met along streets J, K, L, A0 (see the lighter colours at  $y \sim 150$  m and darker colours at  $y \sim 1$  m and  $y \sim 256$  m). Concerning the crossing streets, the leftmost one is characterized by the largest flow, as it is the closest to the source/boundary condition, with the water level being the highest ( $z = 0.5$  m) and  $DV$  reaching the maximum value of  $0.8 \text{ m}^2/\text{s}$ . Conversely,  $DV$  becomes nearly zero downstream, i.e. within the square area located around  $x = 260$  m (square P-p1-p2, indicated by red vertical lines in Figure 4-A).

The speed vectors in Figure 4-B show the main circulation patterns generated within the domain. The speed reduces while moving downstream. Moreover, the water flow entering the crossflow streets ( $x \sim 115$  m,  $x \sim 190$  m) is visible as bending arrows (see also the little perturbations in the water-surface level in Figure 4-A).

Figure 5 shows the outputs of the river-overflow tested scenario. In this scenario, the maximum discharge (peak condition) occurs after 600s. Both panels of Figure 5 refer to this moment in hydrodynamic simulation results. Figure 5-A shows the streamwise section and the water-level profiles relevant to the central section of the streamwise streets. The two lateral streets are illustrated in red (streets B, C, D, A1) and yellow (streets S, T, U, A2), while streets J, K, L, A0 are plotted in blue. As for Figure 4-B, Figure 5-B shows the  $DV$  distribution through a colour map. The largest  $DV$  values occur at the upstream boundary, where  $DV = 1.3 \text{ m}^2/\text{s}$ . In contrast to the levee-failure case, high speeds and reduced depths occur at the intersections between the streets J, K, L, A0 and: (1) the crossflow streets, that are streets F and N, and streets G and O (also see  $DV$  at the intersection at about  $(x, y) = (115, 150)$  m in Figure 5-B); (2) the square (P-p1-p2). Considering

the street intersections, Figure 5-B also shows how speed vectors (red arrows) are not straight but visibly bend towards the crossflow streets. Furthermore, Figure 5-A shows a large perturbation of the water surface just downstream of the intersections (e.g., see the blue line at  $x \sim 120\text{m}$  and  $190\text{m}$ ). Such a feature is due to both large flow intensity and rapid friction reduction at the intersections. In particular, the friction changes from a relatively large value (due to both bottom and vertical obstacles/blocks) to a much smaller value (due to the only bottom contribution).

Given the above, the river-overflow scenario is significantly more severe than the levee-failure scenario, considering that it is based on ideal and largely conservative assumptions.



**Figure 5.** Hydrodynamic results of the river-overflow simulation after 600s (peak condition): a) streamwise section; b)  $DV$  map.

Hydrodynamic results provided useful insights for the following behavioural simulations. It is observed that the levee-failure case reaches almost steady conditions after 600s, while steadiness is reached after 300s in the river-overflow case. Thus, the total time of behavioural simulations is respectively assumed equal to 600s and 300s.

### 3.2 Original scenario: simulation results

Table 3 offers the simulation results concerning the evacuation process for the two considered scenarios. The number of arrived evacuees, the related evacuation times and the evacuation flows are compared. Figure 6 represents the related evacuation curves. The two flood scenarios are characterized by significant similarities about: (a) the evacuation path selection; (b) the position of *out-of-time evacuees*.

Regarding the path selection, evacuees prefer to move towards the outdoor spaces which are orthogonal to the flood-water direction in both scenarios (streets F and N, streets G and O; squares p1 and p2; streets I and R). In fact, the  $DV$

conditions **in these areas** are less critical (Figure 4 and Figure 5). As shown by Figure 4, this phenomenon is more relevant in river-overflow, because  $DV$  values are generally higher in comparison to the levee-failure scenario. This evacuees' choice affects the use of the safe areas. As shown by Table 3, the safe area 0 seems to be the less used one in both conditions, because it is placed in the main floodwater flow direction. Nevertheless, about half of the evacuees **can** gain a safe area within the simulation time in both cases. In fact, according to Table 3,  $P_e$  is similar for both the flood scenarios (percentage difference of about 6% on the average values).

About data on the *out-of-time evacuees*, Table 4 outlines areas and causes that prevent them from reaching a safe area within the simulation time. In general terms, at the end of the evacuation, **most out-of-time evacuees** are located **along the** streets E and M, streets F and N, streets G and O, and the upstream part of streets J and K. Figure 7 summarizes the positions of *out-of-time evacuees*. In both cases, evacuees located downstream are latecomers influenced by:

- their initial position, far from the selected safe area;
- floodwater **interactions** because  $M$  values along the chosen paths decrease their speed.

When the simulation ends, most of these evacuees are located in the crossflow streets immediately downstream in the domain. In fact, they remain close to buildings because of attractive forces [17] and because  $DV$  levels are lower than in the main streets, which are parallel to the main floodwater flow.

Differences in the evacuation results in each flood scenario are affected by “how” the floodwater events specifically develop during the simulation time depending on the hydrodynamic conditions themselves. In the river-overflow scenario,  $DV$  values quickly increase during the first part of evacuation time, by immediately reaching critical conditions for individuals' stability. As a result, a significant number of *out-of-time evacuees* (42%) are influenced by critical  $DV$  conditions, thus provoking casualties (compare to Figure 7-B), too. On the contrary, in the levee-failure scenario, the stability threshold is not reached in the simulation domain, by provoking no casualty.

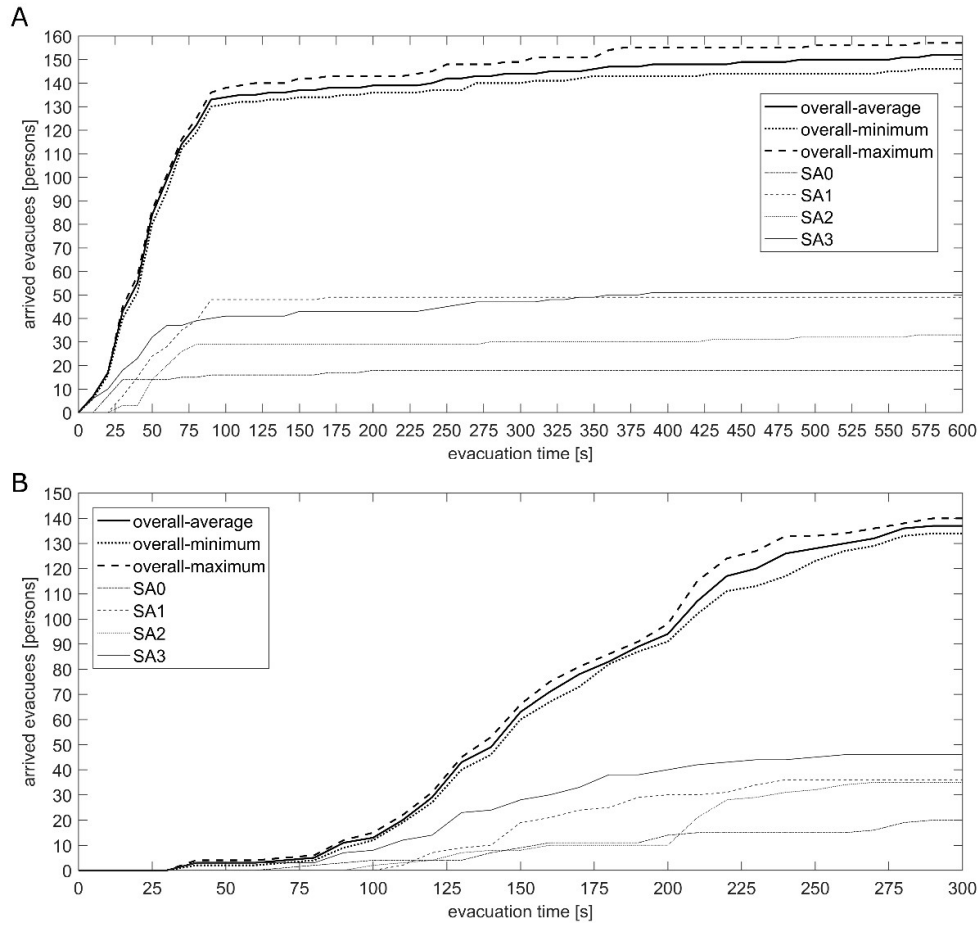
Additional differences are related to “how” the evacuation process develops over time. The overall evacuation curves in **both scenarios** share the same sigmoidal function trend (compare to Figure 6). However, the evacuation process in the levee-failure scenario seems to be faster than the one in river-overflow, especially in the first part of the evacuation. In fact, according to Table 3,  $F_{e,0.50}$  for the levee-failure is at least more than 3 times greater than the one in the river-overflow. Such a result is graphically shown by the slope of the overall average evacuation curves, **which is** higher for the river-overflow scenario, **as shown in Figure 6-B**. This output is essentially due to the lower  $DV$  level in levee-failure when compared to **the one observed** in the river-overflow (compare to Section **Error! Reference source not found.** results). Levee-failure scenario implies lower importance of individual-floodwaters interactions while moving (i.e. higher evacuation speeds; lower possibility to stop moving because of critical  $DV$  levels). Thus, most evacuees can reach a safe

area within the first 100s in the evacuation simulation. When the evacuation time increases ( $t > 100$ s), the levee-failure scenario is mainly characterized by the arrival of *latecomers*. In fact, evacuees can still move in the considered area, but they are slowed down by the *DV* levels. Figure 6 shows a significant asymptotic trend in the evacuation curve essentially due to such a phenomenon. Meanwhile,  $T_{e,0.95}$  for the levee-failure scenario increases and the final overall  $F_{e,0.95}$  proves to be fairly lower than the one for the river-overflow scenario. The same trend can be noticed for each of the safe areas. It is worthy to notice that safe area 3 is more affected than the others by the critical *DV* levels noticed in the upstream part of the urban scenario, as shown, for instance, by  $F_{e,0.50}$  in the levee-failure scenario.

Finally, during the evacuation process, several evacuees change their initial evacuation target, which is the nearest safe area. They can change their target because of [17]: (a) group motion criteria; (b) surrounding critical *DV* levels retrieved along the path initially selected. The percentage of evacuees changing their initial target in respect of the total number of arrived evacuees is equal to 34% for the river-overflow and 39% for the levee-failure scenario (see the supplementary material: S1). In both cases, evacuees' target selection for safe area 1 is essentially affected by the spatial proximity of safe area 0 and safe area 3. No significant differences are noticed for the other safe areas.

**Table 3.** Simulation results for levee-failure and river-overflow scenarios, in the original scenario, according to Section 2.2.1 KPIs. Safe areas positions are shown in Figure 2.

Scenario (max sim. time [s])	Reference safe areas	$P_e$ (st. dev.) [persons]	$P_{e,\%}$ (st. dev.) [%]	$T_{e,0.05}$ [s]	$T_{e,0.50}$ [s]	$T_{e,0.95}$ [s]	$F_{e,0.50}$ [persons/s]	$F_{e,0.95}$ [persons/s]
<i>levee-failure (600s)</i>	all	152 (4)	51 (3)	10	46	377	1.71	0.39
	safe area 0	18 (3)	6 (19)	10	22	113	0.45	0.17
	safe area 1	49 (2)	16 (5)	24	56	86	0.44	0.59
	safe area 2	33 (3)	11 (8)	28	58	479	0.29	0.07
	safe area 3	51 (3)	17 (6)	9	42	301	0.60	0.17
<i>river-overflow (300s)</i>	all	137 (2)	46 (2)	85	159	265	0.50	0.44
	safe area 0	20 (1)	15 (1)	73	158	279	0.06	0.07
	safe area 1	36 (2)	26 (2)	111	151	230	0.13	0.15
	safe area 2	35 (2)	26 (1)	108	208	251	0.08	0.13
	safe area 3	46 (2)	33 (1)	45	126	237	0.16	0.18

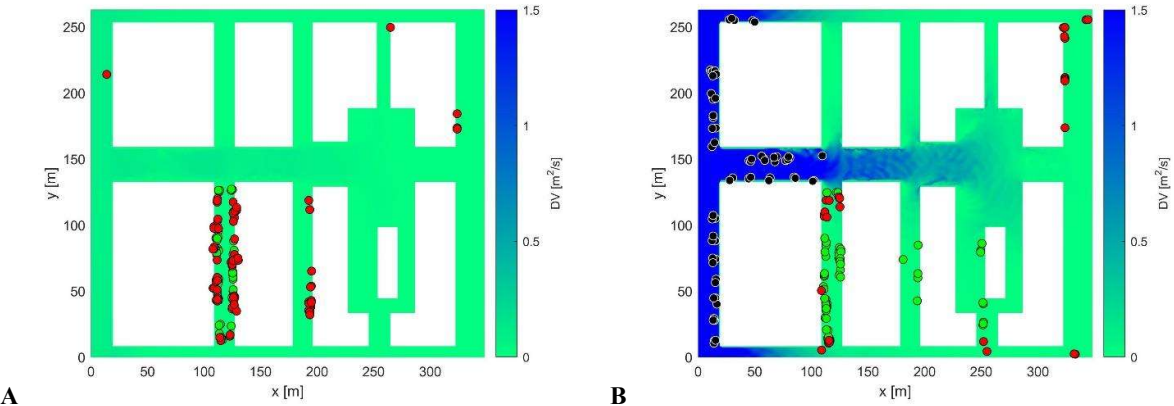


**Figure 6.** Evacuation curves for the original scenario in case of: a) levee-failure; b) river-overflow. Evacuation curves are offered for the whole process (including minimum and maximum curves) and for each safe area.

**Table 4.** Out-of-time evacuees  $P_O$  (and their characterization) in the levee-failure and river-overflow simulations, for the original scenario, according to the KPIs in Section 2.2.1. Percentage values are calculated for the main or secondary related conditions.

Main condition	Secondary conditions	$P_O$ (st. dev.)[persons]		$P_{O,\%}$ (st. dev.) [%]		$P_{O,la} - P_{O,sp} - P_{O,ca}$ [%]	
		Levee-failure (600s)	River-overflow (300s)	Levee-failure (600s)	River-overflow (300s)	Levee-failure (600s)	River-overflow (300s)
all		148 (4)	163 (2)	49 (3)	54 (1)	55-45-0	22-36-42
evacuees who stop upstream (streets E		2 (1)	53 (1)	2 (1)	32 (1)	100-0-0	0-0-100

and M) because of floodwater conditions (e.g. stability loss)							
total number of evacuees located downstream		146 (3)	110 (2)	98 (1)	68 (1)	54-46-0	33-54-13
	evacuees who stop in the main street (streets K, L, A0)	5 (3)	18 (3)	3 (2)	11 (2)	0-100-0	0-18-82
	evacuees who stop near safe area 3	0 (0)	10 (5)	0 (0)	6 (3)	0-0-0	100-0-0
	evacuees who stop near a downstream safe area	4 (2)	12 (2)	2 (1)	8 (1)	100-0-0	100-0-0
	evacuees who stop in the square (square P-p1-p2)	8 (1)	14 (1)	0 (0)	0 (0)	0-0-0	38-62-0



**Figure 7.** Position of out-of-time evacuees at the end of the behavioural simulations in case of: a) levee-failure; b) river-overflow. Latecomers (red circles), spontaneously gathering evacuees (green circles), casualties (black circles) are shown on the  $DV$  map.

$R_{area,scen}$  in Table 5 and  $R_{street,scen}$  in Figure 7 confirm that the river-overflow leads to a worse outcome. In this scenario, the higher impact is due to the floodwater conditions (see  $R_{DV,area,scen}$  in Table 5), which increase the number of *out-of-time evacuees* (see  $R_{O,area,scen}$  in Table 5) and *casualties* (see  $R_{street,scen}$  in Figure 7). On the contrary, crowding conditions

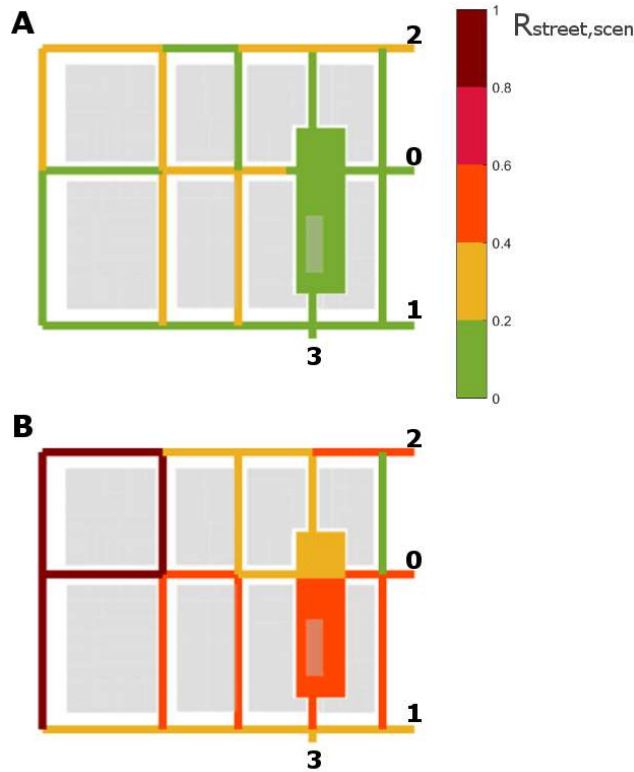


(see  $R_{cr,street,scen}$  in Table 5) are higher for the levee-failure scenario since the lower  $DV$  levels reduce the number of casualties and allow evacuees to effectively move in the outdoor built environment.

Figure 8 summarizes the risk of each outdoor space in the scenario by comparing the river-overflow and the levee-failure scenario. Raw data are reported in the tables of supplementary material: S2. In both cases, higher risk levels are reached at the upstream streets (E, J, M, N in Figure 2), mainly because of large  $DV$  values and of a high number of out-of-time evacuees (essentially, casualties). Streets F, G and N have medium-high  $R_{street,scen}$  values for the other streets orthogonal to the floodwater direction. This effect is due to their related number of latecomers and of spontaneously gathering evacuees thanking the limited  $DV$  levels (compare to Figure 7). This phenomenon is more important in the river-overflow scenario. Finally, some parts of the outdoor built environment placed downstream (e.g. A0, A2, H, I, p2, R) are mainly affected by higher crowding levels and so their risk is comparable to the ones of streets F and G, especially in the river-overflow scenario.

**Table 5** Risk index for the whole area ( $R_{area,scen}$ ) and the related influencing factors, by comparing river-overflow and levee-failure scenarios.

Scenario	$Ro_{area,scen}$	$RdV_{area,scen}$	$R_{cr,area,scen}$	$R_{area,scen}$
Levee-failure	0.27	0.21	1.00	0.30
River-overflow	0.87	1.00	0.81	0.91



**Figure 8.**  $R_{street,scen}$  for: a) levee-failure; b) river-overflow. Buildings (light grey blocks) and safe area codes are supplied. The KPI scale is shown by the color map (0.2 ranges discretization). Raw data are shown by supplementary material: S2.

### 3.3 Risk reduction strategies proposal

In the *original scenario*, the percentage of evacuees reaching a safe area is almost the same for both river-overflow and levee-failure. Nevertheless, the results of Section 3.2 underline how the riskiest scenario is represented by the river-overflow one because of the critical conditions due to *DV* levels leading to a higher number of *out-of-time evacuees* and *casualties*. Thus, this flood scenario is considered in the following to propose risk reduction strategies.

Figure 9 summarizes  $R_{street}$  in the river-overflow scenario (raw data are offered by supplementary material: S3) and highlights riskier areas, this suggesting practical solutions to support evacuees during hazardous phases.

The riskiest streets are located upstream, essentially because of the number of *out-of-time evacuees* (i.e. streets E, J, M). In such outdoor spaces, most of the evacuees stop moving because they can lose their stability because of floodwaters conditions. Direct support against the critical *DV* levels should be provided to the individuals located along streets E and M, to lead them moving towards streets S, J and B or staying here in safe conditions. Evacuees moving along street J should be similarly supported. In addition, the upstream streets that are orthogonal to the floodwater direction (i.e. streets

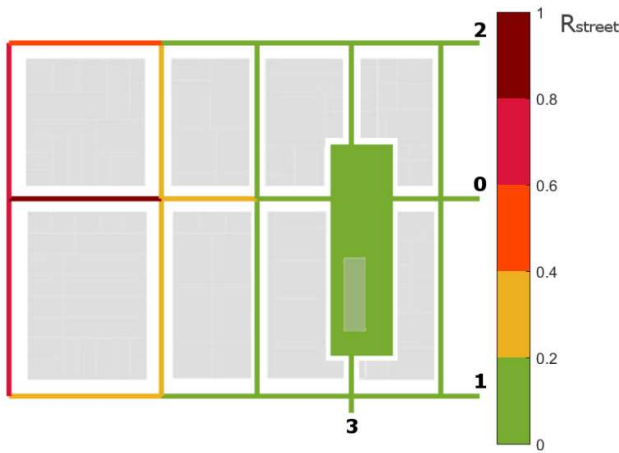
F and G) are riskier than the others because of the number of *latecomers* and *spontaneously gathering evacuees* here thanks to the limited *DV* levels. The evacuees who stop moving here should maintain a safe position while waiting for the rescuers' arrival.

Finally, despite the higher crowding level, streets placed downstream are characterized by a negligible risk level in respect to  $R_{O,street}$  and  $R_{DV,street}$  (that are essentially null and void).

In view of the above, two different risk reduction solutions can be provided:

- the implementation of handrails **can essentially support** evacuees while moving or facing severe *DV* levels conditions (see Section 3.3.1);
- the implementation of handrails plus raised platforms/sidewalks **can** “separate” the evacuees from the critical floodwater levels, and let them waiting for the rescuers' arrival in safe conditions (see Section 3.3.2).

Thus, two related *risk reduction scenarios* are defined and described as follows, while their implementation layout is offered in Figure 10. **In addition to the aforementioned solutions**, signs could be installed in the riskiest areas to inform people about the possible threads (e.g. in terms of possible flood depth) during the normal use of the outdoor built environment [27].



**Figure 9.**  $R_{street}$  representation by considering the river-overflow conditions in the original scenario. Light grey blocks are the buildings, while safe area codes are supplied. The KPI scale is shown by the colour map involving a 0.2 ranges discretization.



**Figure 10.** Proposed risk reduction strategies and their positioning in the related scenarios: a) handrails implementation (dashed lines); b) handrails+raised platforms (rectangles, to qualitatively represent their areas; identification codes defined as in Table 6). Safe areas are pointed out.

### 3.3.1 Strategies proposal: handrails implementation

Handrails are placed along the sidewalks. They help evacuees maintaining stability while moving towards a safe area [17,21,37]. In most cases, this solution maintains a low impact on the existing built environment because the handrails could be implemented on the existing fences or building walls.

In the related simulations, we assumed that evacuees supported by handrails could not lose their stability but they could not also increase their speed (conservative approach in respect to the total evacuation time) [21,35,37,44,45]. This assumption was contemplated in some modelling approaches concerning flooded environments [17,46,47] and it can be considered valid within the floodwater conditions provided by the simulations ( $D(x,y,t) < 1.2\text{m/s}$  and  $V(x,y,t) < 3.2\text{m/s}$ ) [38].

Handrails are hence placed at the street boundaries (building walls, fences), where floodwater speeds are reduced due to the no-slip condition at the wall. Safe areas positions and identification codes are the same as in the *original scenario*.

Figure 10-A shows that handrails are mainly placed along upstream streets (i.e. streets B, E, J, M, S) because of their critical  $DV$  levels. Meanwhile, evacuees moving along the other downstream street (e.g. N and F) could be limitedly supported by handrails because no stability loss phenomena are detected in the river-overflow scenario. Anyway, handrails could be implemented in a widespread manner into the outdoor built environment to support evacuees in other floodwater conditions with higher  $DV$  levels.

### 3.3.2 Strategies proposal: handrails+raised platform implementation

Raised platforms or sidewalks should be easily reached by the evacuees so as to wait for rescuers in safe conditions, thus being considered safe areas. Thus, in this scenario, we assumed that the position of these elements was associated with additional safe areas in the outdoor layout. Each platform should be also marked by clear and visible (in terms of legibility and aesthetics) identification signs, which could inform the community about the use of the areas also in non-disaster conditions (to be seen by both residents and visitors) [27].

These platforms are placed along upstream streets (i.e. streets E, J, M) and in the main layout areas where *spontaneously gathering evacuees* are noticed (i.e. streets F and N), according to the simulation results of the original scenario (see Figure 7). Thus, nine safe areas are proposed by: (a) maintaining safe areas 1, 2 and 3 and removing safe area 0 (which is the less used); (b) introducing six safe areas on raised platforms. Their position is shown in Figure 10-B. Anyway, handrails are still implemented along the streets B, E, M and S to avoid individuals losing their stability because of critical floodwater levels, and so to allow them to reach the raised platform. Table 6 quantitatively describes the raised platforms and their implementation according to the identification codes (as safe areas) in Figure 10-B. Table 6 also provides details concerning: (a) the location; (b) the average number of evacuees to be hosted according to the original scenario results (compare to, e.g., Figure 7); (c) the related minimum wait area; (d) the possible width (orthogonal to the street) and length (parallel to the street) of the area; (e) the height of the platform from the ground; (f) additional notes on the possible implementation in the considered scenario.

In particular, each platform dimension (area [m<sup>2</sup>]) should be great enough to host the average number of gathering individuals (estimated according to  $P_O$  values in original scenario simulation) in proper density conditions (3pp/m<sup>2</sup>, to allow them to wait without contact phenomena [82,83]). Their height from the ground should avoid the possibility that floodwaters interfere with evacuees while they are waiting (railings should be always provided). Moreover, their implementation in the outdoor layout should guarantee:

- adequate access points to ensure the individuals reach the top of the platform (stairs or ramps). In our proposal, the stairs have a tread and a rise of 21cm, while ramps have a slope of 8% to guarantee access by wheelchairs;
- their overall dimension compatible with the surrounding outdoor layout without consistent modifications to it (i.e. to the exiting sidewalks and car lanes);
- possible use of the space under the platforms in ordinary conditions.

In the following simulations, the two designed raised sidewalks placed along the street F are considered as a single safe area because of their proximity in a space with low  $DI$  levels.

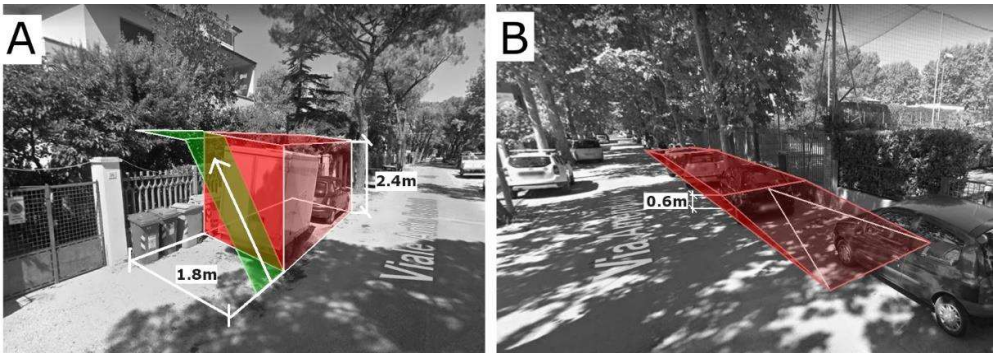
Figure 11 shows a couple of possible schematic examples of the raised platform implementation in the case study. In Figure 11-A a street-level parking lot along the street might be removed to introduce the platform on one street side (view of scheme for street J – saJ1). The access is guaranteed by stairs while the underlying spaces can be normally used as bus shelters or waste disposal facilities. In Figure 11-B, a raised sidewalk might be created by removing a couple of street-level parking lots, accessible by a ramp to guarantee the normal use as a sidewalk (view of scheme for street F - saF). Similarly, continuously raised sidewalks can be implemented.

**Table 6** Data on the raised platforms implementation. Platforms with “\*” are split into two equal parts (on each street side), and the shown dimensions refer to each of the raised sidewalks (thus hosting half of the evacuees’ number).

Street	Safe area code	Evacuees to be hosted	Minimum area [m <sup>2</sup> ]	Possible width [m]	Possible length [m]	Height from the ground [m]	Notes
E	saE	20	8	1.8	4.5	2.4	removing a street-level parking lot along the street to introduce the platform on one street side; the space under the platform can be normally used as a bus shelter or waste disposal facilities
J	saJ1	10	4	1.8	2.3	2.4	
J	saJ2	10	4	1.8	2.3	2.4	
F	saF*	53	10*	1.8*	5.6*	0.6*	raised sidewalks with removing of a couple of street-level parking lots, accessible by a ramp to guarantee the normal use as a sidewalk
M	saM	19	8	3.2	2.4	2.4	raised area within the public square spaces (e.g. garden area)

P	saP	17	6	2.0	3.0	1.0	not currently used vehicle access point; the space under the platform can be normally used as bus shelter or waste disposal facilities
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**Figure 11.** Examples of the possible implementation of raised platforms in the case-study, according to the positions identified by Table 6: a) removing a street-level parking lot along the street to introduce the platform on one street side, with access by stairs (e.g. saJ); b) raised sidewalks with access by ramp (e.g. saF).

### 3.4 Effectiveness of the risk reduction strategies

Table 7 offers the simulation results for the river-overflow scenario by considering the *original scenario* versus the ones concerning the implementation of handrails and handrails+raised platforms. The number of arrived evacuees, the related evacuation times and the evacuation flows are provided. Figure 12 compares the evacuation curves of these scenarios.

From a general point of view, according to Figure 12, the overall evacuation curves **concerning** the risk reduction strategies always demonstrate an improvement in respect to the *original scenario* (also considering maximum and minimum curves). Data and KPIs **are** outlined for the overall simulation area and for each considered safe area. Table 8 shows data on *out-of-time evacuees*, by including the characterization of the areas and the causes that prevent them from reaching a safe area within the simulation time.

Results of the handrail implementation scenario are quite similar to the ones of the original scenario, both for the overall evacuation process and for each safe area. The main similarities concern  $P_e$  and  $F_{e,0.50}$  (see Table 7), the general evacuation trend (see Figure 12) and the choice of the safe areas (see supplementary material: S4). The effects of handrails

are beneficial, especially if considering the possibility to avoid casualties because of body stability loss, as shown by  $P_{0,ca}$  [%] in Table 8. Nevertheless, the critical floodwater conditions in the upstream streets still slow down the evacuees located in streets B, E, M and S. In fact, some of these individuals can reach a safe area (as shown by increasing  $P_e$  in Table 7), but they represent the last arrived evacuees.  $T_{e,0.95}$  and  $F_{e,0.95}$  slightly increase because of such phenomena. Similarly to the original scenario, 31% of the evacuees change their target because of group motion criteria and surrounding critical  $DV$  levels retrieved along the path initially selected. They were too limitedly supported by the handrails while moving. Thus, evacuees still try to spontaneously gather along the street F because of the local beneficial floodwater conditions, as for the original scenario (compare, e.g., with Figure 13).

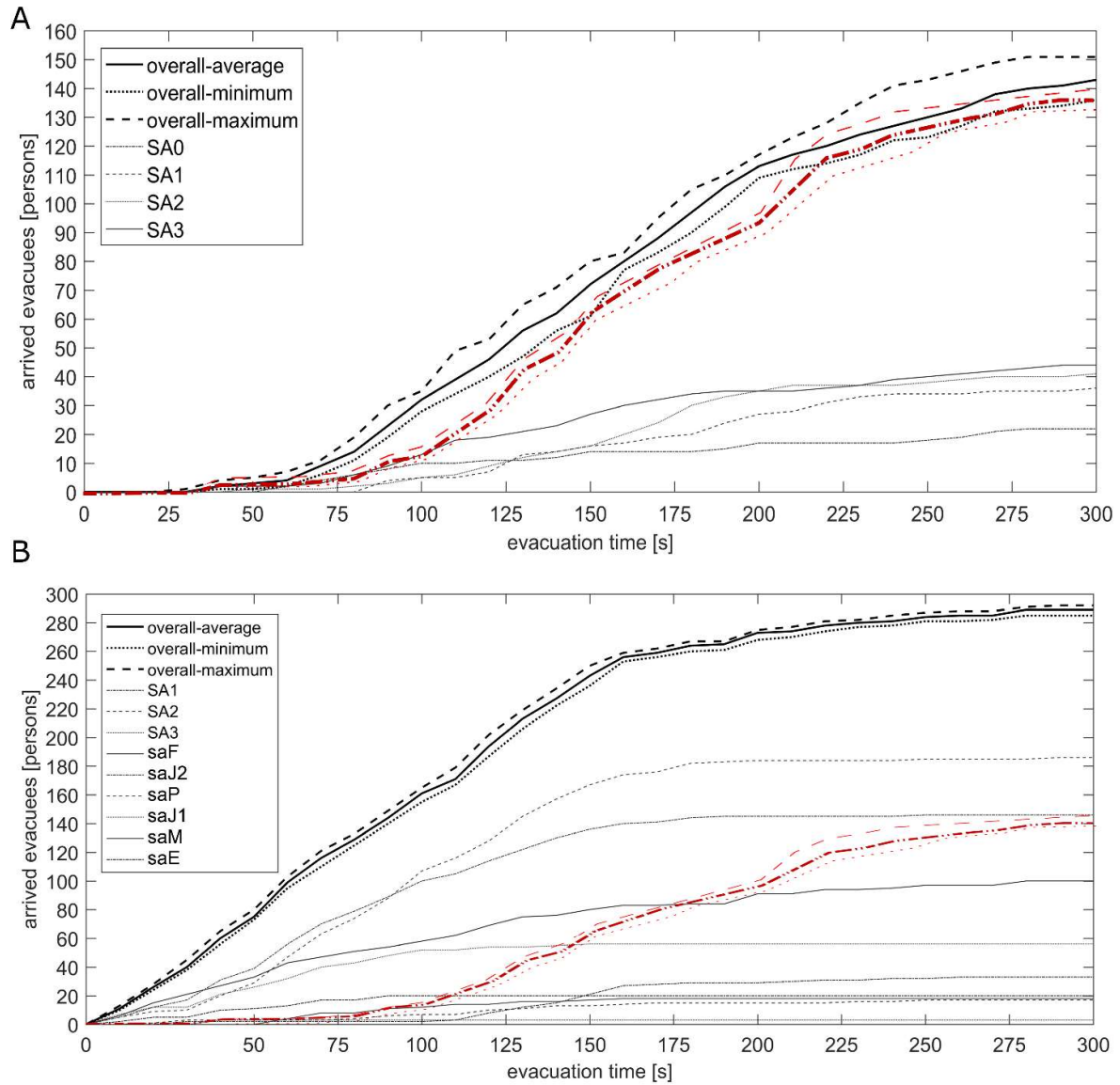
On the contrary, the handrails+raised platform implementation significantly decreases the risk conditions for the evacuees. Firstly,  $P_e$ ,  $F_{e,0.50}$  and  $F_{e,0.95}$  increase, as displayed by Table 7. It is worth noticing that the evacuation flows are 3 times the ones in the original scenario (see also the slope of the evacuation curves in Figure 12). The combination of handrails in the upstream streets and raised platforms avoids the presence of casualties as well as limits the number of latecomers and *spontaneously gathering evacuees* (see also Figure 13). In fact, the evacuees located upstream can use the handrails to reach the nearest safe areas on the raised platform (i.e. saE, saM, saJ1 and saJ2). According to experimental analysis on evacuation behaviours [37], evacuees who cannot reach one of these safe areas prefer to wait near the buildings and spontaneously gather while being supported by the handrails. The time needed to reach the platforms is essentially affected by the floodwater levels and by the distances of the arriving evacuees from the raised platform (see  $T_{e,0.95}$  in Table 7).

The introduction of raised platforms along the street F and the square P-p1-p2 reduces the number of evacuees arriving at the safe areas placed downstream, and in particular to the safe area 3. In this sense, please also see the supplementary material: S4, i.e. “Difference in arriving evacuees (“initially choosing” minus “reaching”)” data. In fact, evacuees try to minimize their distance from a safe area by using saF and saP. Finally, let comparing the number of evacuees used to evaluate the dimension of the safe areas (according to the *original scenario* simulations, see Table 6) and the number of evacuees who arrived at the raised platforms according to the simulation results (see Table 7). The most significant differences are retrieved for saF (+86%) and saP (+347%). Anyway, a possible increase of saF and saP surface is still possible in the outdoor built environment. Both sidewalks of street F can be turned into raised elements, while the platform saP can be enlarged since it is placed in a square with gardens.



**Table 7** Simulation results for river-overflow scenario, in the original scenario and in the ones with risk reduction strategies implemented (handrails; handrails+raised platform), according to Section 2.2.1 KPIs. Safe areas positions are shown in Figure 10.

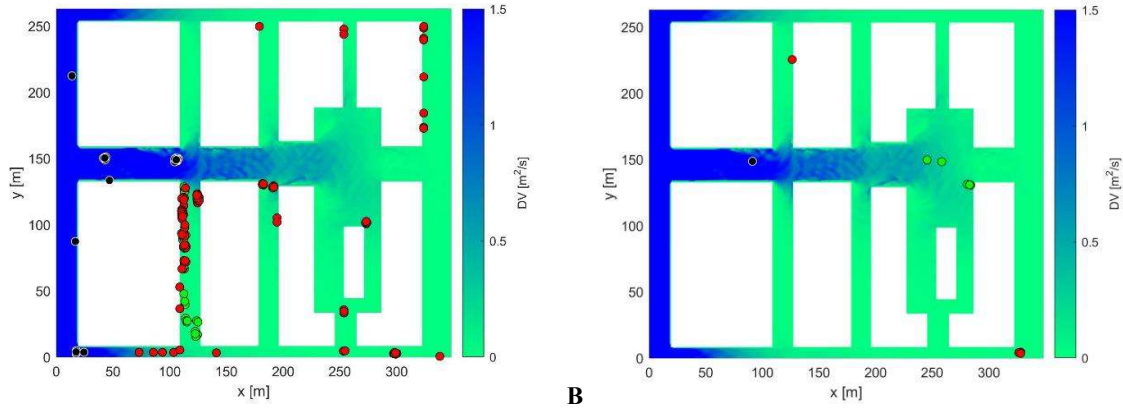
<b>Scenario</b> <b>(max sim. time</b> <b>[s])</b>	<b>Reference</b> <b>safe areas</b>	$P_e$ (st. dev.) [persons]	$P_{e,\%}$ (st. dev.) [%]	$T_{e,0.05}$ [s]	$T_{e,0.50}$ [s]	$T_{e,0.95}$ [s]	$F_{e,0.50}$ [persons/s]	$F_{e,0.95}$ [persons/s]
<i>Original scenario</i>	all	137 (2)	46 (2)	85	159	265	0.50	0.44
	safe area 0	20 (1)	15 (1)	73	158	279	0.06	0.07
	safe area 1	36 (2)	26 (2)	111	151	230	0.13	0.15
	safe area 2	35 (2)	26 (1)	108	208	251	0.08	0.13
	safe area 3	46 (2)	33 (1)	45	126	237	0.16	0.18
<i>Handrails imple- mentation</i>	all	143 (6)	48 (4)	69	153	270	0.50	0.53
	safe area 0	22 (5)	7 (3)	60	133	259	0.08	0.07
	safe area 1	36 (6)	25 (4)	89	163	253	0.11	0.13
	safe area 2	41 (3)	28 (2)	90	160	246	0.13	0.16
	safe area 3	44 (5)	30 (3)	60	129	258	0.16	0.16
<i>Handrails+raised platform imple- mentation</i>	all	289 (3)	96 (1)	13	91	217	1.60	1.27
	safe area 1	33 (3)	12 (1)	62	143	229	0.31	0.34
	safe area 2	17 (1)	6 (<1)	21	113	194	0.07	0.08
	safe area 3	3 (1)	1 (<1)	33	35	37	0.05	0.06
	saE	20 (1)	7 (<1)	6	40	86	0.25	0.22
	saM	18 (1)	6 (<1)	42	72	138	0.12	0.12
	saJ1	9 (1)	2 (<1)	4	36	90	0.14	0.10
	saJ2	12 (1)	4 (<1)	19	38	67	0.16	0.16
	saF	99 (1)	34 (<1)	10	78	235	0.65	0.40
	saP	76 (2)	27 (1)	50	107	173	0.36	0.42



**Figure 12.** Evacuation curves for the whole process and for each safe area in the river-overflow scenario considering: a) handrails implementation; b) handrails+raised platform implementation. The whole process evacuation curve for the original scenario is shown (line-two dots evacuation curve, in red, by including: minimum curve, as a dotted line; average curve, as line-two dots line; maximum curve, as a dashed line).

**Table 8** Out-of-time evacuees  $P_O$  (and their characterization) in case of the implementation of handrails (H) and handrails+raised platform (H+P), according to the KPIs in Section 2.2.1. Percentage values are calculated with respect to the main or secondary related conditions.

Main condition	Secondary conditions	$P_O$ (st. dev.)[persons]		$P_{O,\%}$ (st. dev.) [%]		$P_{O,la} - P_{O,sp} - P_{O,ca}$ [%]	
		$H$	$H+P$	$H$	$H+P$	$H$	$H+P$
all		157 (3)	11 (3)	52 (1)	4 (1)	69-31-0	67-33-0
evacuees who stop upstream (streets E and M) because of floodwater conditions (e.g. stability loss)		16 (1)	1 (1)	10 (1)	9 (9)	100-0-0	100-0-0
total number of evacuees located downstream		141 (2)	10 (2)	90 (1)	91 (18)	65-35-0	64-36-0
	evacuees who stop in the main street (streets K, L, A0)	25 (1)	6 (1)	18 (1)	60 (10)	32-68-0	17-83-0
	evacuees who stop near safe area 3	8 (0)	0 (0)	6 (0)	0 (0)	0-0-0	0-0-0
	evacuees who stop near a downstream safe area	9 (1)	7 (1)	6 (1)	70 (10)	100-0-0	100-0-0
	evacuees who stop in the square (square P-p1-p2)	15 (0)	5 (0)	11 (0)	50 (0)	0-0-0	0-0-0



**Figure 13.** Position of out-of-time evacuees at the end of the river-overflow simulations in case of: a) handrails implementation; b) handrails+raised platform implementation. Latecomers (red circles), spontaneously gathering evacuees (green circles), casualties (black circles) are shown on the DV map (scale on the right coloured bar).

$R_{area,scen}$  and  $R_{street,scen}$  proposed in Table 9 and Figure 14 are evaluated for the *original* and *risk reduction scenarios*. The floodwater conditions are the same in the three scenarios (see  $R_{DV,area,scen}$  in Table 9). The handrails+raised platform implementation scenario is the best solution since it:

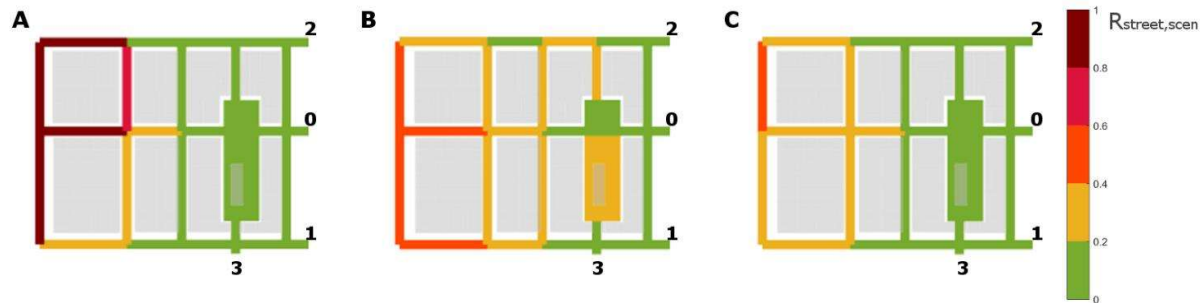
1. is the less affected by data on *out-of-time evacuees* (see the lowest  $R_{O,area,scen}$ );
2. shows an increase in the crowding-related factor because the majority of evacuees can reach a safe area (see the highest  $R_{cr,street,scen}$ );
3. is characterized by a  $R_{area,scen, red-pre}$  reduction up to -54%.

**Table 9** Risk index for the whole area ( $R_{area,scen}$ ) and the related influencing factors, by comparing river-overflow conditions in the original scenario with the handrails implementation and handrails+raised platform scenarios.

Scenario	$R_{O,area,scen}$	$R_{DV,area,scen}$	$R_{cr,area,scen}$	$R_{area,scen}$
Original scenario	0.85	1.00	0.64	0.89
Handrails implementation	0.26	1.00	0.69	0.53
Handrails+Raised platform implementation	0.02	1.00	1.00	0.41

Figure 14 graphically summarizes the risk of each street in the reference scenarios.  $R_{DV,street,scen}$  values are always equal because of the same flood scenario (compare to supplementary material: S5 data). The results confirm the same conclusions offered for  $R_{area,scen}$ . Some downstream outdoor spaces (e.g. square p2) are affected by the presence of *out-of-time*

evacuees also in the *risk reduction scenarios* (see Figure 13). As a result, the overall risk of such spaces increases, but casualties are not noticed here.



**Figure 14.**  $R_{street,scen}$  representation by considering the river-overflow conditions in: a) the original scenario; b) handrails implementation; c) handrails+raised platform implementation. Buildings (light grey blocks) and safe area codes are supplied. The KPI scale is shown by the colour map (0.2 ranges discretization). Raw data are shown by supplementary material: S5.

## 4 Discussion

The methodology application and the analysis of simulation results underline the general capabilities of the behavioural design-based methodology and some rules to design risk reduction strategies for the outdoor built environment against flood risk. For each of these key findings, specific case study outcomes are also provided.

The following capabilities of the simulation-based methodology could be highlighted:

- *Providing simulations on the current probable scenarios by including evacuation representation is useful to understand the dynamics of the emergency conditions over space and time from a holistic perspective.* According to the proposed KPIs, the different flood scenarios are useful to individuate the best risk-reduction strategy to be implemented. In fact, the proposed KPIs account for most of the effects of evacuation behaviours. Meanwhile, they focus on the outdoor built environment and its composing parts, which are pivotal elements for the evacuees' safety during urban floods. Such approach could be integrated into models based on Life Safety and Hazard or AHP-based risk rating metrics (e.g. [10,11,22,34,54,62]) to include aspects such as (a) the evacuation curve/flows, (b) the use of open spaces, and (c) the presence of spontaneous gathering areas. Thus, the assessment of each part of the built environment could be performed. Concerning the specificities of the case study, the simulation results show that the river-overflow scenario is riskier for the evacuees in the outdoor built environment if compared to

the considered levee-failure scenario. The main causes are due to the combination of the initial critical conditions in floodwaters levels and their related quick-spreading in the urban layout, which brings evacuees to stop moving (i.e. provoking casualties);

- *Effects of evacuees' attraction and gathering towards the nearest "safe" area is useful to identify where the rescuers' action should be focused to support the exposed evacuees.* In a regular urban environment, evacuees should tend to move towards the outdoor areas that are orthogonally placed in respect to the main floodwater flows, because of the local safer conditions in terms of floodwater levels. Thus, solutions aimed at collecting them in such areas are recommended. Handrails can increase the safety of evacuees while moving towards these areas. Anyway, handrails cannot completely improve the number of evacuees arriving at the safe areas themselves. Concerning the case study, the majority of evacuees gathers in the upstream orthogonal streets instead of in the downstream ones because of the specific domain conditions.

Furthermore, from a modelling perspective, the adopted approach takes advantage of micro-scale and behavioural design-based modelling criteria to firstly consider both pedestrian traffic and fatalities estimations [22,62]. It also seems to overcome current limitations on experimental-based behaviours shown by many existing models (e.g. [10,11,18,22,34,54,62]). In particular, the proposed evacuation model includes rules for: (a) spontaneous path selection (moving towards areas with lower floodwater levels) and gathering behaviours; (b) coming-and-going behaviours; (c) attraction towards immobile objects such as buildings, fences, handrails. Furthermore, the effects of such behaviours are innovatively investigated at the micro-scale, that is considering each individual and each street or square in the built environment. The related overall impact at the macro-scale can be hence assessed.

Nevertheless, some limitations concerning individual features exist because the model relies on average adults' evacuation simulation to demonstrate the methodology capabilities. Future works should model evacuation speeds and human body stability issues inducing fatalities according to the specific individual characteristics, such as mass, height, age, gender, and other motion abilities, also thanking specific experimental works [21,22,38,49]. This work adopts insights of handrails use in evacuation conditions, by homogeneously considering that evacuees cannot lose stability while using them [21,35,37,44,45]. Future works to estimate the effective support of handrails for evacuees moving on foot in floodwaters will hence enrich the simulation of individual speeds while using handrails. Considering body stability issues, a generic form of water depth versus velocity curve in the Life Safety Model could be adopted to represent the related additional uncertainties, by pursuing, for instance, a probabilistic approach [22,25,54]. Further evaluations concerning different human body stability loss phenomena (buoyancy; body failure), also in the view of the other stability-affecting factors (e.g. age, gender, weight, height) [22,35,50,51], should be provided. Based on local census databases or in-situ

surveys [24,42], probabilistic distributions of the exposed people will be used in future works, thus including all uncertainties which concern individuals' features and positions within the built environment over the time.

About the application context, this work is mainly centred on a limited built environment (a square and the nearby streets), although the proposed framework could be applied to wider urban areas, both in existing and new urban contexts. Nevertheless, splitting the domain into sub-areas could be preferred to analyse homogeneous areas in terms of built environment or hazard or exposure conditions, also depending on the position of the reference gathering areas. At the same time, **other built** environments, such as underground ones, can take advantage of this behavioural design-based methodology. In this case, the composing elements of the underground spaces (e.g. corridors, staircases, platforms in case of underground stations) can be assessed in terms of floodwater characterization and evacuation process **through** the same simulation rules and KPIs proposed by this work.

Considering risk reduction solutions, for the first time at the authors' knowledge, this work focuses on the effectiveness analysis of architectural interventions in the outdoor built environment to support exposed individuals during the flood emergency [35,37,45]. In this sense, the work provides insights on a solution that is less investigated than traditional ones, such as those relating to the positioning of gathering areas, implementation of early warning systems, and modifications to the emergency path configurations [22,54]. Simulation results highlight the following rules for risk reduction strategies considering their design by technicians of Local Authorities and Civil Defence bodies:

- *handrails implementation in the scenario can effectively reduce the overall risk of the whole area as a consequence of no casualties in the number of evacuees* (human body stability effects are avoided since evacuees can be supported by handrails). Concerning the specificities of the case study, this reduction is equal to about -40% if assuming that evacuees supported by handrails cannot lose their stability under any floodwater conditions;
- *raised **platforms** can be distributed in the urban fabric to create safe areas where evacuees can gather and wait for the rescuers' arrival.* Their position can be defined according to the simulation results in the *original scenario*. Anyway, some general rules can relate to concentrating them in upstream streets and in orthogonal streets where evacuees tend to spontaneously gather. More data on the effective dimension of raised platforms can be provided according to the related scenario simulations. Concerning the specificities of the case study, the reduction of the overall area risk is up to about -54% while combining the raised platform with the implementation of handrails along the upstream streets.

Handrails and raised platforms can be architecturally integrated to provide new spaces and activities in the outdoor built environment. **In this work, the** case study application **would like** to depict the general capabilities of such architectural micro-scale interventions, giving some preliminary and not-exhaustive examples. Although the possible efforts for

their implementation in the outdoor built environment, the integration of handrails and raised platform into the emergency plan could reduce the residual risk due to possible lacks in warning systems implementation and functioning [84–86], such as those due to lacks in the system organization or in the data operation or possible failures of the systems. They could support also evacuees who could perform unsafe behaviours also if they are warned about the flood arrival (e.g. time-wasting activities, selection of the wrong evacuation paths) [37].

Finally, the demonstration of the methodology capabilities underlines how stakeholders and planners can take advantage of **behavioural design-based** outcomes. **They can analyse** different event scenarios and **test** the effectiveness of other kinds of risk reduction strategies, such as:

1. *macro-scale interventions*, e.g.: (a) early warning systems to alert the population and speed up the evacuation before the critical conditions are reached; (b) drainage systems to limit the floodwater impacts on the evacuation process;
2. *micro-scale solutions*, e.g.: (a) re-shaping of urban spaces to include architectural elements to support the individuals; (b) evacuation guidance systems to point out the correct evacuation direction to the safer areas in the urban fabric; (c) intervention on spaces that can host mass-gathering events; (d) urban spaces requalification **using** architectural elements that could improve safety but could be also used in normal fruition conditions<sup>2</sup>;
3. *emergency management strategies*, i.e.: (a) evacuation plan communication to people to improve their preparedness and awareness; (b) gathering areas location according to micro-scale solutions.

The model could be modified to represent specific aspects and behavioural issues altering the decision model, the pedestrian traffic model or the fatalities model depending on the considered solution.

## 5 Conclusions

Increasing the resilience of our communities against flood risk in the built environment should take advantage of the evaluation of evacuees' behaviours and choices, especially if considering the initial phases of a flood emergency, i.e. evacuation. In this sense, analyses on the outdoor built environment are key elements for evacuees' safety, **considering** that evacuees can move in flood-affected scenarios. Simulation-based tools and methods can effectively evaluate the risk for the exposed evacuees and the built environment from a holistic perspective. On this basis, **successful** risk reduction strategies can be proposed to increase the resistance and resilience of the existing built environments **as long as they can:**



(a) effectively support evacuees to be safe during the emergency; (b) avoid additional threats; (c) lead evacuees to “correctly” behave in these critical emergency phases; (d) be easy-to-implement; (e) be integrated with the normal fruition of the built environment also in non-disaster conditions.

Starting from this standpoint, this work proposes a micro-scale and behavioural design-based methodology to assess the risk in outdoor built environments. The methodology is used to propose effective risk reduction solutions and then to evaluate their effectiveness. It is holistic since it: (a) is based on the joint representation of floodwater hydrodynamics and evacuation process; (b) combines critical descriptors of these two aspects into merged KPIs for risk assessment.

An existing experimental-based flood evacuation simulator is used to represent the emergency conditions and then to provide data for the KPIs. The application to a case-study demonstrates the method capabilities in: (a) identifying risks for evacuees due to the individual-floodwater-built environment interactions starting from the micro-scale behavioural phenomena; (b) assessing the risk at the micro (i.e. street, square) and macro (i.e. whole outdoor built environment)-scales; (c) comparing different flood scenarios, both including hydrodynamic and evacuation.-related standpoints; (d) proposing and evaluating risk reduction actions, by mainly focusing the attention on architecturally-integrated elements (e.g.: platforms, handrails) in high-risk outdoor spaces.

Risk evaluations and safety levels comparisons are possible through the proposed KPIs. Finally, simulation results also trace some general remarks by focusing on the methodology (and KPIs) application, and on general criteria for implementing the proposed architecturally integrated elements in the outdoor layout.

The methods and tools proposed by this work focus on evacuees’ behaviour and on the floodwater dynamic representation, but it does not consider the damages induced on the built environment itself. Thus, future activities should involve the inclusion of the “built environment damage”-related factors (i.e. buildings, infrastructural elements, roads, and so on, by also including drainage systems and sewers) as a function of floodwater spreading over the simulation time and space. Moreover, the method should be applied to different typological scenarios to derive the related “typical” risk assessment configuration, depending, for instance, on: the layout features; the possible flood events; the characterization of exposed people in terms of emergency behaviours and risk awareness levels. Such application results will also encourage the definition of best practices for increasing communities’ safety in the related outdoor built environment scenarios.

## 6 Acknowledgement

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## Appendix A: FlooPEDS model description

The Flooding Pedestrians' Evacuation Dynamics Simulator (FlooPEDS) was adopted in this work for joint hydrodynamic and evacuation simulation purposes [17]. All the notations of the model are reported and described in Table A.1.

The hydrodynamic model is based on the solution of the Nonlinear Shallow Water Equations [87]. The NSW solver has been validated during the last decades over very different shallow-water contexts (e.g. [64,87]). Its verification in an urban environment during a historical event (in combination with the evacuation/behavioural model) is reported in the original work about FlooPEDS [17]. NSWs consist of a continuity equation and two momentum-conservation equations along  $x$  and  $y$ , as shown in Equations 1, 2 and 3:

$$D_t + (uD)_{,x} + (vD)_{,y} = 0 \quad (2)$$

$$u_t + uu_{,x} + vu_{,y} + gD_{,x} = gh_{,x} - B_x \quad (3)$$

$$v_t + uv_{,x} + vv_{,y} + gD_{,y} = gh_{,y} - B_y \quad (4)$$

These are used for the description of depth-averaged flows, where: commas represent partial differentiation,  $(x,y,z)$  are the orthogonal Cartesian coordinates;  $(u, v)$  is the depth-averaged velocity vector, with modulus  $V$  [m/s]; the total water depth  $D$  is made of the bed level  $h$  and the instantaneous water surface level  $\eta = D - h$ ; the Chezy-type bottom friction is represented by  $B_x$  and  $B_y$  [64]. The simulated scenarios are represented using a 3D mesh with a given constant spatial resolution. For the case study of Section 2.3, the mesh covers an area of 350m by 265m as shown in Figure 2, in which each rectangular cell is characterized by a spatial resolution of  $(\Delta x, \Delta y) = (0.8, 0.5)$ m. Each building block is represented as a discrete rectangular-shaped obstacle. For each cell not covering the building blocks, the hydrodynamic simulator

provides the time evolution of water depth  $D(x,y,t)$  and depth-averaged flow speed  $V(x,y,t)$ . These both provide the specific force per unit width  $M(x,y,t)$  [ $\text{m}^3/\text{m}$ ] and the human body stability conditions  $DV(x,y,t)$  [ $\text{m}^2/\text{s}$ ] as discussed in Section 2.1 [18,35,48].

The micro-scale evacuation model combines: (a) an Agent-Based Model (ABM) to describe intentional issues of the evacuees in terms of behavioural patterns [37]; and (b) a Social Force Model (SFM) [65] to describe the motion process as the combination of attractive and repulsive forces connected to the behavioural patterns of the ABM. Each simulated pedestrian moves in the designed 2D continuous space and tries to reach a safe area. His/her motion is influenced by the surrounding  $D(x,y,t)$ ,  $V(x,y,t)$  and  $M(x,y,t)$  values, that are calculated by the hydrodynamic simulator. The evacuation motion is solved within a maximum evacuation time, which is fixed according to the hydrodynamic simulation conditions.

It was assumed that all the individuals know the position of the safe area. Thus, each simulated agent selects its evacuation path to minimize the distance towards the safe area and the risk due to floodwater conditions (i.e., in terms of  $M$ ). Paths selection decision can be performed at the initial position point and at the crossroads or in other decisional points (e.g. plano-altimetric variations of the urban layout). To this end, in such positions, he/she evaluates the local conditions of the possible paths to be selected (in terms of  $M$  and distance to the safe area). If the shortest path is the one with the lower  $M$  value, he/she moves toward this path. Otherwise, he/she moves towards another path. As a result, a difference can exist between the safe area **selected at the start of the evacuation**, and **the safe area gained at the end of the process**.

The path selection influences the evacuation direction since it steers the individual's SFM-based drive-to-target force  $\vec{O}_g$  [N]. Then, his/her preferred evacuation speed  $v_{pref,i}(x,y,t)$  varies over time and space depending on  $M(x,y,t)$ , as shown by Equation 5 which is based on previous experimental results [37].

$$v_{pref,i}(x,y,t) = 0.52 M(x,y,t)^{-0.11} \quad (5)$$

$\vec{O}_g$  is the result of attractive and repulsive forces that modify his/her final local evacuation direction. Attractive forces are activated towards [17]: unmovable obstacles (i.e. buildings, fences and other street furniture, handrails) that can support the individual's motion in floodwaters (see  $\vec{F}_{attr,w}$  [N] in Equation 6); other surrounding individuals, because of social identification and group phenomena [65]. Repulsive forces  $\vec{F}_{rep,w}$  [N] are aimed at avoiding individual-individual and built elements-individual overlapping [65].

$$\vec{F}_{attr,w}(t) = F_w \frac{d_w - R_i}{d_{w,max}} \vec{t}_w \quad \text{if } d_w < d_{w,max} \quad , \quad F_w \vec{t}_w \quad \text{elsewhere} \quad (6)$$

Finally, Equation 7 summarizes the SFM-based equation to solve the motion of each evacuee, step by step during the simulation time. Some random variations in the behaviours could be described by the term  $\overrightarrow{\varepsilon(t)}$  [N] [65].

$$m_i \frac{d\overrightarrow{v_i(t)}}{dt} = \overrightarrow{O_g(t)} + \sum \overrightarrow{F_{rep,i}(t)} + \sum \overrightarrow{F_{re,w}(t)} + \sum \overrightarrow{F_{attr,i}(t)} + \sum \overrightarrow{F_{attr,w}(t)} + \overrightarrow{\varepsilon(t)} \quad (7)$$

The evacuation ends if the individual:

- reaches a safe area (*arrived evacuees*) or at the end of the simulation time, if the individual is still moving and he/she is not able to reach a safe area within the maximum simulation time because of his/her evacuation path or speed. Such *latecomers* can be affected, for instance, by the interactions with other pedestrians and/or with speed-decreasing floodwaters conditions;
- moves along the same path more than 1 time, since  $M$  values of surrounding paths are worse than the ones of the selected path. According to this experimental-based behaviour, he/she can spontaneously gather with surrounding individuals because of  $\overrightarrow{F_{attr,i}}$  (*spontaneously gathering evacuees*);
- stops moving because of critical surrounding conditions, i.e. in case of body stability loss ( $DV > 1.20 \text{ m}^2/\text{s}$ ) [31,38]. Such conditions could eventually provoke life threats by considering adult pedestrians (*casualties*). In addition,  $D(x,y,t) < 1.2 \text{ m/s}$  and  $V(x,y,t) < 3.2 \text{ m/s}$  are considered as limiting values for adults in good conditions having a height ( $h_i$ ) and mass ( $m_i$ ) product  $h_i m_i > 50$  [38].

Equation 6 is solved for  $dt=0.1\text{s}$ , by using the Euler's method in a separate way for  $x$  and  $y$  axes, to update each simulated individual's position. According to Equation 6 and Equation 7, the following main variables setup was used for the evacuation simulator [17]:  $m_i=80\text{kg}$  (however,  $h_i m_i > 50$ ) and  $R_i=0.35\text{m}$  (to represent an average adult evacuee);  $F_w=300\text{N}$  and  $d_{w,max}=9\text{m}$ ;  $\varepsilon(t)=0\text{N}$ .

**Table A.1** Modeling notations.

Symbol	Measure	Description
$B_x, B_y$	$\text{ms}^{-2}$	Bottom friction terms
$D$	m	Total water depth
$d_w$	m	Actual distance between pedestrian $i$ and obstacle $w$

$d_{w,max}$	m	Maximum distance of activation for attractive forces between the pedestrian and the unmovable obstacle
$\overrightarrow{F_{attr,i}}, \overrightarrow{F_{attr,w}}$	(modulus) N	Attractive forces for group interactions and for fixed obstacles influence
$\overrightarrow{F_{rep,i}}, \overrightarrow{F_{rep,w}}$	(modulus) N	Repulsive force from other pedestrians and from obstacles
$F_w$	N	Constant parameter for maximum attraction force between a pedestrian and the unmovable obstacle
$g$	9.81 m/s <sup>2</sup>	gravity acceleration
$h$	m	Bottom vertical position
$i, j, w$	-	Subscripts for: the pedestrian subject of valuation; other pedestrians; an obstacle
$\overrightarrow{l_w}$	-	Versor between the current pedestrian $i$ position and the unmovable obstacle which attract the pedestrian
$M(x,y,t)$	m <sup>3</sup> /m	specific force per unit width, which varies over space ( $x$ and $y$ coordinates) and time ( $t$ )
$m_i$	kg	Pedestrian mass
$\vec{O}_g(t)$	(modulus) N	Drive-to-target force
$R_i$	m	Radius of pedestrian $i$ , that is the distance between his/her barycentre and his/her shoulder, thus considering an ideal circle circumscribing the individual on a plan view
$t, dt$	s	Time in motion simulation evaluation, gap between two different motion simulation evaluation
$u$	m/s	Depth-averaged streamwise ( $x$ -directed) velocity
$v$	m/s	Depth-averaged crossflow ( $y$ -directed) velocity
$V$	m/s	Modulus of the Depth-averaged velocity vector
$v_{pref,i}(x,y,t)$	m/s	Preferred individuals' speed for isolated pedestrian $i$ in floodwaters (in "those" conditions and without considering other pedestrians)
$\vec{v}(t)$	(modulus) m/s	Actual velocity of the pedestrian
$\vec{\varepsilon}(t)$	(modulus) N	Gaussian error due to possibility of different evacuees' behaviours and features

$\eta$	m	Instantaneous water surface level
$\vec{\eta}_{iw}$	-	Unit vector pointing from $i$ to $w$ used for repulsive forces calculus

1112

## Appendix B: KPIs notations

KPI symbol	Measure	KPI Description
<i>difference in arriving evacuees</i>	[%]	percentage difference between the number of evacuees reaching the safe area at the simulation end and the one of evacuees “initially choosing” the safe area
$F_e : F_{e,0.05}, F_{e,0.50}, F_{e,0.95}$	[persons/s]	effective average flow of evacuees arrived in a safe area: flows for $P_e=5\%$ , $P_e=50\%$ and $P_e=95\%$
$P_O, P_{O,street}$	[persons]	number of out-of-time evacuees (including casualties); number of out-of-time evacuees (including casualties) for a certain street
$P_{O,\%}, P_{O,street,\%}$	[%]	percentage of out-of-time evacuees (including casualties) in respect to number of exposed people in the outdoor built environment; value referred to a certain street
$P_{O,la}, P_{O,la,street}$	[%]	percentages of latecomers in respect to $P_O$ ; value for a certain street
$P_{O,sp}, P_{O,sp,street}$	[%]	percentages of spontaneously gathering evacuees in respect to $P_O$ ; value for a certain street
$P_{O,ca}, P_{O,ca,street}$	[%]	percentages of casualties in respect to $P_O$ ; value for a certain street
$P_e$	[persons]	number of evacuees arrived in a safe area within the simulation time
$P_{e,\%}$	[%]	percentage of evacuees arrived in a safe area within the simulation time in respect to the number of exposed people in the outdoor built environment
$P_{cr,street}, P_{cr,street,\%}$	[persons]	street crowding (how many evacuees go through a given street in the urban layout while evacuating); percentage value calculated in respect of the maximum $P_{cr,street}$ value within the simulated area
$R_{area,scen}$	-	the risk of the whole <i>area</i> in a given scenario <i>scen</i>
$R_{street,scen}$	-	the risk of a single <i>street</i> (or square) in a given <i>scen</i>
$R_{street}$	-	the risk of a single <i>street</i> (or square) in comparison to other streets (squares) in a given scenario

$R_{O,area,scen}$ $, R_{O,street,scen} , R_{O,street}$	-	risk for out-of-time evacuees: for the whole area in the given scenario, for the given in the considered scenario, on the given street
$R_{DV,area,scen} ,$ $R_{DV,street,scen} ,$ $R_{DV,street}$	-	risk due to the floodwater level: for the whole area in the given scenario, for the street in the given scenario, on the given street
$R_{cr,area,scen} ,$ $R_{cr,street,scen} , R_{cr,street}$	-	<i>crowding risk index on the area</i> : for the whole area in the considered scenario, for the street in the considered scenario, on the considered street
$T_e : T_{e,0.05} , T_{e,0.50} ,$ $T_{e,0.95}$	[s]	evacuation time: evacuation time for $P_e=5\%$ , $P_e=50\%$ and $P_e=95\%$
<b>Weights in AHP</b>	<b>Measure</b>	<b>Weights Description</b>
$w_O$	-	out-of-time evacuees-related weight in the level 1 AHP application (related to $R_{O,area,scen} , R_{O,street,scen}$ and $R_{O,street}$ )
$w_{DV}$	-	DV-related weight in the level 1 AHP application (related to $R_{DV,area,scen} ,$ $R_{DV,street,scen}$ and $R_{DV,street}$ )
$w_{cr}$	-	crowding-related weight in the level 1 AHP application (related to $R_{cr,area,scen} ,$ $R_{cr,street,scen}$ and $R_{cr,street}$ )
$w_{sp} , w_{la} , w_{ca}$	-	weights related to spontaneously gathering evacuees, latecomers, casualties to be applied in the level 2 AHP application for the components of $R_{O,area,scen} ,$ $R_{O,street,scen}$ and $R_{O,street}$

## 1113 Appendix C: Risk indices relating to the built environment

1114 The following paragraphs describe the definition of the area risk-related KPIs, which represent the overall risk condi-  
1115 tions for the whole simulation area or for a part of it:

- 1116 • the risk of the whole area  $R_{area,scen}$  [-] considers different scenarios to compare the risks of the whole area in  
1117 each of them (section C.1);
- 1118 • the risk of a single street (or square)  $R_{street,scen}$  [-] considers different scenarios to compare the risks of the street  
1119 in each of them (section C.2);
- 1120 • the risk of a single street (or square) in comparison to other streets (squares)  $R_{street}$  considers the conditions  
1121 within the same given scenario [-] (section C.3).

All these KPIs were based on a **two-level** Decision Hierarchy, as shown by Table C1. The weight estimation was performed through the open-source tool AHP Online System<sup>5</sup>. The first level is **composed of** factors (in order of importance):

- (a) related to the *out-of-time evacuees* (“how many evacuees cannot reach a safe area?”). The associate weight is  $w_o$  [-]. This factor was associated with 3 second-level variables, depending on the reasons inducing the evacuees to stop out of a safe area (compare to Section 2.2.1). In order of importance, they are: *casualties* ( $w_{ca}$ ), because they represent evacuees who cannot be saved at the end of the emergency; *latecomers* ( $w_{la}$ ), since they can still move at the end of the simulation; *spontaneously gathering evacuees* ( $w_{sp}$ ), since they are located in areas where  $DV$  conditions are not critical at all;
- (b) related to the floodwater risk levels (“how much the flood is critical?”), in terms of  $DV$ , since it affects the human body stability. This factor has no second-level variable. The associate weight is  $w_{DV}$  [-];
- (c) related to the use of the urban layout and of the paths (“where evacuees move?”), or rather on the overall crowding conditions along the streets. This factor has no second-level variable. It is the least relevant because it just outlines the possibility of individual-individual interactions along the paths and the probable exposure to particular  $DV$  levels during the whole **evacuation** process<sup>6</sup>. The associate weight is  $w_{cr}$  [-].

**Table C1** Decision hierarchy overview for the risk indices, by including principal eigenvalue and Ratio of Consistency evaluated through the AHP application, for each level.

	Level 1	Level 2
Relative Risk Index	out-of-time evacuees-related: $w_o=0.604$	spontaneously gathering evacuees: $w_{sp}=0.073$
		latecomers: $w_{la}=0.200$
		casualties: $w_{ca}=0.727$
	$DV$ -related: $w_{DV}=0.326$	-
	crowding-related: $w_{cr}=0.07$	-
Principal eigen value	3.006	3.009
$RC$	0.60%	1.00%

<sup>5</sup> <https://bpmmsg.com/ahp/ahp-hierarchy.php> (last access: 19/09/2019)

<sup>6</sup> e.g.  $DV$ -related factors being equal in two parts of the same scenario, the less riskiest is the one with the lowest crowding level since evacuees can more freely move.



### C.1 $R_{area,scen}$

Let consider different comparable scenarios to measure the risks of the whole area in each of them. For each scenario,  $R_{area,scen}$  was calculated according to Table C1 decision hierarchy, as shown by Equation C.1:

$$R_{area,scen} = R_{O,area,scen} \cdot w_O + R_{DV,area,scen} \cdot w_{DV} + R_{cr,area,scen} \cdot w_{cr} = \left( \frac{P_{O,ca}}{P_{O,ca,max,scen}} \cdot w_{ca} + \frac{P_{O,la}}{P_{O,la,max,scen}} \cdot w_{la} + \frac{P_{O,sp}}{P_{O,sp,max,scen}} \cdot w_{sp} \right) \cdot w_O + \frac{DV_{area,max}}{DV_{area,max,scen}} \cdot w_{DV} + \frac{P_{cr,area,max}}{P_{cr,area,max,scen}} \cdot w_{cr} \quad (C.1)$$

where  $max$  refers to the maximum value in the area in the given scenario, and  $max,scen$  refers to the maximum value in all the comparable scenarios.

### C.2 $R_{street,scen}$

Let consider different comparable scenarios to measure the risks of a given street in each of them. For each scenario,  $R_{street,scen}$  was calculated according to Table C1 decision hierarchy, as shown by Equation C.2:

$$R_{street,scen} = R_{O,street,scen} \cdot w_O + R_{DV,street,scen} \cdot w_{DV} + R_{cr,street,scen} \cdot w_{cr} = \left( \frac{P_{O,ca,street}}{P_{O,ca,street,max,scen}} \cdot w_{ca} + \frac{P_{O,la,street}}{P_{O,la,street,max,scen}} \cdot w_{la} + \frac{P_{O,sp,street}}{P_{O,sp,street,max,scen}} \cdot w_{sp} \right) \cdot w_O + \frac{DV_{street,max}}{DV_{area,max,scen}} \cdot w_{DV} + \frac{P_{cr,street}}{P_{cr,street,max,scen}} \cdot w_{cr} \quad (C.2)$$

where, where  $max$  refers to the maximum value for the considered street in the given scenario, and  $max,scen$  refers to the maximum value in all the comparable scenarios.

### C.3 $R_{street}$

Let consider a certain scenario to compare the risks of the open spaces in the built environment (i.e. streets, squares). For each open space (i.e. street) in the simulation area,  $R_{street}$  was calculated according to Table C1 decision hierarchy, as shown by Equation C.3:

$$R_{street} = R_{O,street} \cdot w_b + R_{DV,street} \cdot w_{DV} + R_{cr,street} \cdot w_{cr} = \left( \frac{P_{O,ca,street}}{P_{O,ca,street,max}} \cdot w_{ca} + \frac{P_{O,la,street}}{P_{O,la,street,max}} \cdot w_{la} + \frac{P_{O,sp,street}}{P_{O,sp,street,max}} \cdot w_{sp} \right) \cdot w_O + \frac{DV_{street,max}}{DV_{area,max}} \cdot w_{DV} + \frac{P_{cr,street}}{P_{cr,street,max}} \cdot w_{cr} \quad (C.3)$$

where  $max$  refers to the maximum value in the given scenario.